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Relativistic Heavy-Neighbor-Atom Effects on NMR Shifts: Concepts and Trends Across the Periodic Table

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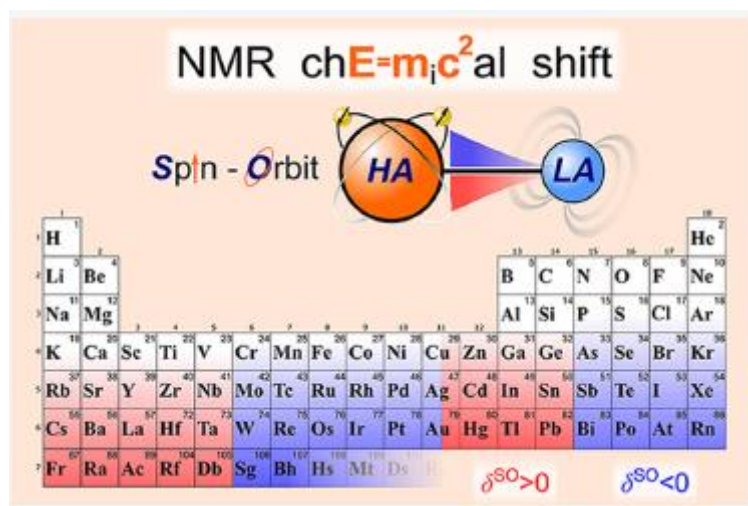
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ABSTRACT

Chemical shifts present crucial information about an NMR spectrum. They show the influence of the chemical environment on the nuclei being probed. Relativistic effects caused by the presence of an atom of a heavy element in a compound can appreciably, even drastically, alter the NMR shifts of the nearby nuclei. A fundamental understanding of such relativistic effects on NMR shifts is important in many branches of chemical and physical science. This review provides a comprehensive overview of the tools, concepts, and periodic trends pertaining to the shielding effects by a neighboring heavy atom in diamagnetic systems, with particular emphasis on the “spin-orbit heavy-atom effect on the light-atom” NMR shift (SO-HALA effect). The analyses and tools described in this review provide guidelines to help NMR spectroscopists and computational chemists estimate the ranges of the NMR shifts for an unknown compound, identify intermediates in catalytic and other processes, analyze conformational aspects and intermolecular interactions, and predict trends in series of compounds throughout the Periodic Table. The present review provides a current snapshot of this important subfield of NMR spectroscopy and a basis and framework for including future findings in the field.



1. INTRODUCTION AND HISTORICAL OVERVIEW

The NMR chemical shift, the resonant frequency of a particular nucleus relative to a standard in an NMR spectrum, provides crucial information about the molecular and electronic structure of the given system. In order to optimize the information obtainable from an NMR spectrum, a qualitative and quantitative understanding of the shift values expected for a given substance is fundamentally important. In this review we will lay out the current level of understanding of the relativistic effects of one or more heavy atoms (HAs) on the NMR shifts of its neighboring atoms. The term “heavy-atom effect”, coined by Pyykko,¹ initially referred to the nuclear shielding of the heavy atom itself, i.e., the “heavy-atom effect on the heavy-atom shielding” (HAHA effect).² The effect of a heavy atom on a neighboring light atom was subsequently termed “heavy-atom effect on the light-atom shielding” (HALA effect), even though we now know that this effect also applies when the NMR nucleus probed is itself a heavy atom. Keeping this fact in mind, we will use the established HALA label throughout this review. Many HALA effects are due to spin-orbit (SO) coupling, but there are also scalar relativistic (SR, also known as spin-free relativistic, SFR) HALA effects.³ Because it useful qualitative chemical concepts for the relativistic effects of a heavy atom on its own shielding,⁴ we will not cover the HAHA effects in any detail here, but will mention the relevant literature toward the end of this section. Moreover, while crucial for the absolute shielding of the heavy atom, HAHA effects mostly cancel out in the relative shifts that NMR spectroscopy typically focuses on (with some exceptions, see refs **2-16**). We also restrict our coverage to formally diamagnetic systems.

As this review will largely focus on the progress in understanding achieved since the last extensive reviews in 2004^{3,13} (reviews including the topic as part of a wider discussion have appeared occasionally in the meantime¹⁵⁻¹⁸), it seems appropriate to start with a brief overview of the state of the field prior to 2004. Much of what is summarized in this section is explained in much more detail in **ref 3**.

The potential importance of the effects of special relativity in describing the magnetic-resonance parameters, including NMR chemical shifts, was recognized early on. The inner core-shells of the atoms are often crucially involved and, in many instances, the important role of the electronic spin introduces spin-orbit coupling contributions. Because this applies to NMR shifts, the effects of SO coupling will be the central focus of this work, but we will also discuss the influence of SR effects on the NMR shifts of neighboring atoms.

The first attempts by Nakagawa and co-workers to use perturbation theory (PT) to extend the theory of nuclear shielding in diamagnetic systems beyond the nonrelativistic (NR) Ramsey equation (see also **section 2**) were published in an organic chemistry journal¹⁹ (and in the proceedings of a domestic Japanese NMR conference).²⁰ Note also that these ideas were preceded by the first theories of pseudocontact shifts in paramagnetic systems,²¹⁻²⁵ which are also known to have an SO origin. Nakagawa et al. laid out the third-order perturbation-theory (PT3) framework that resulted from including SO coupling as an additional perturbation in Ramsey's theory and pointed out the important analogy of the SO-induced HALA effects with the Fermi-contact mechanism of indirect spin-spin coupling constants, which was further exploited based on quantitative computations almost 30 years later.^{26,27} The first explicit computations within such a third-order perturbation scheme in the 1970s and 1980s relied on semiempirical approximate molecular-orbital (MO) theory.²⁸⁻³² The perturbational treatment has been extended to accurate post-Hartree-Fock wave functions as well as to Kohn-Sham DFT, and it has been used for various applications and for detailed analyses.³ We will present the PT framework in **section 2** and exploit it extensively in **section 3**.

The extension of the second-order perturbation theory (PT2) Ramsey equations to a variational treatment of SO coupling in a four-component framework (see **section 2**) dates from 1983, when three independent research groups published pro-positals.³³⁻³⁵ The limited computational resources available at the time forced initial implementations of such relativistic PT2 theories to use even more qualitative MO schemes (of the extended-Huckel type) than those used for PT3. Some crucial understanding of the HALA effect on, e.g., the ¹H shielding in HI in terms of the spin and spatial symmetry of four-component spinors was extracted even at this early stage, many years before more quantitative ab initio or DFT four- or two-component relativistic schemes were introduced to compute NMR shieldings.¹ We note in passing that the first studies of the SR neighbor-atom effects in the 1990s used effective-core potentials (ECPs) on the heavy atom, typically at DFT levels, to efficiently incorporate the SR effects of the heavy atom on the overall electronic structure and thus on the NMR shielding of the neighboring atoms (e.g., ligand atoms in a heavy-metal complex).³⁶⁻³⁹ While comparison of relativistic and non-relativistic ECP computations is still an efficient way to study the SR effects on the neighbor-atom NMR shieldings, in the years since the 2004 review, relativistic all-electron methods of one-, two-, or four-component types (see **section 2**) have evolved to offer easy access to similar information.

Methodological aspects will be described in detail in **section 2**. Here we summarize the qualitative understanding of HALA effects on nuclear shieldings as of 2004. The analogy between SO-HALA effects and the Fermi-contact (FC) mechanism of indirect spin-spin coupling, implied qualitatively by Nakagawa et al.,²⁰ was computationally tested in detail in a 1998 paper.²⁶ DFT calculations on a series of organoiodine complexes showed closely parallel behavior of the SO-HALA contributions to ¹³C and ¹H NMR shieldings for different positions in iodobenzene and the corresponding I-C and I-H reduced spin-spin coupling constants, an enhancement of both quantities with carbon s-character in the C-I bond in iodoethane, iodoethene, and iodoethyne, as well as the Karplus-type dependence of the three-bond SO-HALA effects on the ¹H NMR shieldings on the I—C—C—H dihedral angle in iodoethane. These findings clearly established the validity and usefulness of Nakagawa's analogy and have been confirmed by subsequent studies (see **section 3**). The dominance of an FC-type mechanism for the SO-HALA effects can best be understood and appreciated using the third-order-perturbation framework (PT3) presented in **section 2**; therefore, detailed explanations will be presented in **section 3**.

The dependence of the FC-mechanism on the s-character of the bonding at the spectator NMR atom²⁶ is shown by the fact that (a) ¹H NMR shieldings LA effects because the hydrogen 1s-orbital predominates in bonding, (b) ¹³C SO-HALA effects increase, e.g., from sp³ to sp² to sp hybridization of

carbon atoms, (c) for p-block elements as LA, SO-HALA effects on the shifts tend to be largest for their highest oxidation state, where the participation of the s-orbital in bonding is maximized,^{3,13,40} (d) SO-HALA effects thus tend to be small for fluorine and oxygen, where p-orbitals dominate the bonding,⁴¹ (e) SO-HALA effects are also small for the early transition-metal elements Ti, Zr, Hf, V, Nb, Ta, Cr, Mo, and W as LA in d⁰ halide complexes because the metal—halogen bonds in such systems are dominated by the metal d-orbitals,³ but (f) SO-HALA effects increase for the NMR shieldings of the metal in late transition-metal halide complexes where the metal s-character is again more significant in the bonding.³ These considerations explain the predominance of the normal halogen dependence (NHD) of shifts for p-block nuclei (in particular those in their maximum oxidation state), the inverse halogen dependence (IHD) for early d⁰ systems (and the closely related lanthanum⁴²), and a return to NHD for the late transition metals. NHD shows a decrease in the shifts (increased shielding) from chloride to bromide to iodide substituent(s), whereas IHD indicates the opposite behavior. NHD is most often, but not always, caused by shielding SO-HALA effects, whereas IHD tends to arise from the trend of the paramagnetic shielding contributions when the SO-HALA effects are small. Many examples of NHD induced by SO-HALA effects have been studied (see **section 4**), and some mistakes in the interpretations of NHD have been exposed, for example, for the ¹³C NMR shifts in trihalomethyl cations (CX₃; X = Cl, Br, I).⁴³ Other observations related to the s-character in bonding such as the enhancement of hybridization defects^{44,45} (caused by the size mismatch between the valence s- and p-orbitals)⁴⁶ and thus of s-character and SO-HALA effects, whereby more electronegative substituents withdraw charge from the spectator NMR atom, have been discussed in the 2004 review.³ This last aspect explains why the halomethanes CH_{4-n}X_n (X = Br, I) exhibit a “nonlinear NHD” with increasing n, whereas the corresponding mixed complexes CY_{4-n}X_n (e.g., Y = Br, X = I) show an essentially linear decrease.³ We note in passing that two computational studies have shown that the dependence of SO-HALA effects on the bond length in systems like HX (X = halogen) differs from that of nonrelativistic shifts. As a consequence, SO-HALA effects may alter the ro-vibrational corrections to these shifts and give rise to unusual isotope effects and temperature dependencies.^{47,48}

The importance of π -type lone electron pairs (LPs, or nonbonding pairs, n) for shielding SO-HALA effects (see **sections 2 and 3**) had received substantial attention by 2004: MO analyses showed that such n-LPs are important for shielding SO-HALA effects. A comparative study of the ¹³C shifts in the series CF₃IF_n (n = 0, 2, 4) demonstrated that the two iodine LPs in CF₃I dominate the ¹³C SO-shifts. The latter are about halved with one LP in CF₃IF₂ and essentially vanish in the absence of π -LPs in CF₃IF₄.⁴⁹ Similarly, chalcogenide substituents, which tend to feature only one π -type LP, give rise to only about half of the SO-HALA effects provided by halides.^{3,50-52} Shielding SO-HALA effects have also been identified for the ¹³C NMR shifts in transition-metal carbonyl complexes and related systems.^{39,53,54}

In contrast, high-lying c-bonding MOs in systems like XHgCH₃ or InCH₃ have been found to cause deshielding SO effects on the ¹³C NMR shifts.^{38,39,55} The overall observations as of 2004 are summarized as follows: high-lying occupied nonbonding orbitals with π -symmetry relative to the bond between the NMR-active LA and the HA substituent(s) provide shielding SO-HALA effects, while high-lying σ -bonding orbitals have deshielding SO-HALA effects. Already in 1987, the 4-component extended-Huckel computations on HI showed that π -type iodine LPs make a shielding ¹H HALA contribution while a c-bond causes deshielding.¹ We will discuss in **section 3** how a consistent interpretation within a third-order-perturbation theory framework allows us to place these observations, and particularly the sign of SO-HALA effects, into a more general picture.

SR-HALA effects are easily evaluated computationally using an ECP or all-electron approach, but their interpretation is not as direct as that for the SO-HALA effects discussed above. They are not governed by one dominant and distinct mechanism^{56,57} like the SO/FC mechanism for SO-HALA effects that we

will describe in detail in **section 2**. The SR effects also originate in the core—shells of the HA(s), but it is their effect on the overall electronic structure of the valence shell that matters for the NMR shifts of neighboring atoms. This may happen via relativistic changes in the shapes of MOs that involve both the relativistically modified AOs of the HA and those near the LA. The paramagnetic shielding contributions may also be affected by relativistically modified energy denominators. These SR effects tend to become important somewhat lower in the Periodic Table than SO-HALA effects, typically in the sixth period and beyond. They also tend to obey shell-structure effects known for SR effects on other properties, such as structures or energetics. Thus, we expect to see a “coinage-metal maximum” around group 11, related to the famous “gold maximum”.⁵⁸ Initial studies carried out in the 1990s and early 2000s included the 17O NMR shieldings of oxo complexes,^{36,39} ¹³C and 17O NMR shieldings of carbonyl complexes,^{39,53,54} as well as ¹³C and ¹H NMR shieldings of organomercury complexes and mercury hydrides.^{38,39} Both indirect SR effects due to relativistic structure changes and direct effects were analyzed. The relativistic contraction of the bond length and the direct SR effects at a given structure increased the 17O NMR shielding in oxo complexes. However, for organomercury complexes the ¹³C NMR shieldings were still increased by the relativistic bond-length contraction but reduced by the direct SR effects at a given structure (SO effects on structures tend to be smaller and have not been studied as much⁵⁹). These differences were attributed to the difference in bonding character at the metal center, a dominant 5d-expansion in the oxo complexes vs a dominant 6s contraction in the mercury species. Further examples studied included the ¹⁹F NMR shifts of mixed uranium halide complexes.^{9,10,41} In this case the SO-HALA effects were rather small because of an inefficient SO/FC mechanism, whereas the SR effects were sizable. We should also mention that SR- and SO-HALA-effects are not additive. SR-induced changes in the electronic structure (e.g., contraction/expansion of MOs, modification of the radial nodal structure, or changes in the energy spectrum) may alter the SO effects.⁶⁰⁻⁶²

Finally, we mention in passing the so-called HAAA effects. These relate largely but not exclusively to the core-shells of the relativistic HA.^{2,3,5-16} Made up of both scalar and spin-orbit contributions, they are generally included in full four-component treatments but are less well described in some quasi-relativistic treatments like the ZORA (zeroth-order regular approximation) approach.⁶³ While analyses based on Breit-Pauli (BP) perturbation theory yield a number of terms, it often appears that a cross term between the Fermi-contact operator and the kinetic spin-Zeeman term dominates the HAAA effects.¹⁴ Such contributions seem not to occur for spin-rotation constants, and a historical approach frequently used to extract the paramagnetic contributions to NMR shifts from spinrotation constants (**see section 2**) breaks down for heavier ⁶⁴⁻⁶⁹ atoms.

In the following, we will first summarize the theoretical and computational background of relativistic effects on NMR shifts (**section 2**) and then provide a general conceptual framework for analyzing the SO-HALA effects (**section 3**) before embarking on a journey of the SO-HALA effects through the Periodic Table, concentrating on work published since the 2004 review³ (**section 4**).

2. THEORETICAL BACKGROUND FOR THE ANALYSIS OF SO-HALA SHIFTS

As a basis to better understand our analyses in the following sections, we need to introduce some theoretical formalism based on relativistic quantum chemistry and perturbation theory. While we strive to keep matters simple, some key equations are required. Relativistic effects in computational quantum chemistry are defined as the difference between results obtained by relativistic and nonrelativistic levels of theory.¹ As such, the relativistic contribution to a particular molecular property is a purely theoretical concept that we can probe only by computations. However, the study of

relativistic effects is crucial for our understanding of the molecular properties of systems containing heavy atoms and for relating these properties to electronic structure or chemical bonding. The inclusion of relativistic effects in computations always entails a compromise between accuracy and efficiency. A more accurate description of the relativistic effects usually requires a more demanding computational methodology. Potentially relevant aspects of quantum electrodynamics notwithstanding, relativistic four-component (4c) theory based on the Dirac-Coulomb-Breit Hamiltonian is considered^{70,71} the gold standard for calculating molecular properties, but because of its large computational demands, more approximate quasi-relativistic two-component (2c) theories have been developed. These theories include both scalar and spin-orbit (SO) relativistic effects variationally, i.e., up to an infinite order of Taylor expansion. Further down the ladder are so-called one-component (1c) theories that neglect spin-orbit effects, significantly reducing the computational demand. In areas where the spin-orbit effects are negligible, such more expedient one-component treatments (SR or NR) are the obvious choice. One-component approaches may contain, to various degrees of accuracy, scalar-relativistic (SR) effects or no relativistic effects at all. In the latter case, a nonrelativistic (NR) theory featuring the well-known Schrödinger Hamiltonian is obtained. Finally, at any level of Hamiltonian (1c-NR, 1c-SR, 2c, or 4c), various corrections can be added perturbatively, including, for example, SO effects on top of 1c (NR or SR) computations.

From the computational point of view, all of the above relativistic methods can be formulated at the all-electron or ECP (effective core potential) level of theory, provided the coreshells of the spectator NMR-active atom are covered, and the full core nodal structure of its valence orbitals is thus treated correctly. Of course, all-electron calculations are more computationally demanding because they take into consideration all of the degrees of freedom for every electron variable. On the other hand, ECP theory excludes core electron variables from the computation. This approximation is based on the observation that core electrons are not involved in chemical bonding and therefore can be included in the calculation as an effective potential. This technique leads to computationally efficient approaches, but because the number of electrons treated by the ECP influences the final accuracy of the results, it requires additional validation.⁴¹ Moreover, any relativistic effects can be included in the ECP as well. For example, it is popular to include SR effects in the ECP but to treat the remaining valence electrons at the NR level of theory. In this way the relativistic effects are also included for the valence shell through the action of the ECP. As relativistic all-electron approaches have become more efficient over the years, the need to use ECPs has diminished to some extent.

2.1. Nuclear Magnetic Shielding and NMR Shift

With some exceptions (see below), an analysis of the effects of the electronic structure on relative isotropic NMR chemical shifts for diamagnetic species containing only light elements typically requires consideration of only the paramagnetic contribution. In the following, we will rationalize this statement in a nonrelativistic framework using a relation suggested by Flygare and Goodisman⁷² and discuss why it cannot be transferred to relativistic theory.

The isotropic NMR chemical shift of the “light atom” of interest (herein labeled LA) is defined as the difference between the isotropic nuclear shielding of a reference system and the shielding of the system of interest the isotropic nuclear shielding of a reference system and the shielding of the system of interest

$$\delta(\text{LA}) = \sigma_{\text{ref}}(\text{LA}) - \sigma(\text{LA}) \quad (1)$$

The shielding constant and, thus, the chemical shift can be broken down into diamagnetic and paramagnetic contributions

$$\sigma(\text{LA}) = \sigma^{\text{d}}(\text{LA}) + \sigma^{\text{p}}(\text{LA}) \quad (2)$$

$$\delta(\text{LA}) = \delta^{\text{d}}(\text{LA}) + \delta^{\text{p}}(\text{LA}) \quad (3)$$

Flygare and Goodisman⁷² pointed out an important relation for the diamagnetic shielding

$$\sigma^{\text{d}}(\text{LA}) \approx \sigma^{\text{FA}}(\text{LA}) + C^{\text{nuc}}(\text{LA}) \quad (4)$$

where $\sigma^{\text{FA}}(\text{LA})$ is the diamagnetic shielding of the free LA and $C^{\text{nuc}}(\text{LA})$ represents the nuclear contribution to the nuclear spin-rotation constant (in ppm). When the results from eqs 1-4 are combined, $\sigma^{\text{FA}}(\text{LA})$ cancels out, which gives us the following simple expression:

$$\delta(\text{LA}) \approx C_{\text{ref}}^{\text{nuc}}(\text{LA}) - C^{\text{nuc}}(\text{LA}) + \delta^{\text{p}}(\text{LA}) \quad (5)$$

As C^{nuc} depends only on the structure of the molecule, it is clear that the electronic structure influences isotropic NMR chemical shifts solely via the paramagnetic contribution.

Unfortunately, this result is not transferable to the calculation of SO-HALA shifts. There is some indication that relation 4 (and by extension relation 5) is applicable in the relativistic domain when the gauge origin is placed on the spectator atom LA. However, in the presence of one or more HAs, this leads to inaccurate results for any practical finite basis set.⁷³ Fortunately, the diamagnetic contribution to NMR shifts depends only weakly on the electronic structure (usually by up to 2 ppm); therefore, it is often sufficient to analyze only the paramagnetic contribution to understand trends in NMR shifts. ¹H NMR shifts are an exception, due to their small shielding range (i.e., 2 ppm is a large effect in this case) and the absence of a core—shell in hydrogen. A small shift range may cause lithium shifts to be borderline cases, where one should not a priori disregard changes in the diamagnetic terms.

In the above discussion we assumed the use of common gauge origin (CGO) methodology for calculation of the NMR shielding. While the CGO is typically not used for practical calculations, due to poor convergence of the basis set, the analysis within a CGO picture is more transparent than, e.g., with the frequently used London orbitals (gauge-including atomic orbitals, GIAOs).^{74,75} This is mostly because GIAO expressions are more complicated than those for CGO, while the dependence of the GIAO and CGO diamagnetic contributions on the electronic structure remains approximately the same. Nevertheless, GIAO-based analyses can be found in the literature,^{76,77} usually in cases where the higher precision of the GIAO methodology is mandatory and in-depth MO analysis is less crucial.

2.2. MO Analysis in the Nonrelativistic Domain

In view of the above description, we will focus further on the analysis of the isotropic paramagnetic shielding contribution, $\sigma^{\text{p}}(\text{LA})$, or shift, $\delta^{\text{p}}(\text{LA})$. In the nonrelativistic (NR) domain within Hartree—Fock

or density functional theory, the $\sigma^p(\text{LA})$ contribution has a Ramsey-like form⁷⁸ (we will use Hartree atomic units throughout **section 2**)

$$\sigma^{\text{NR,p}}(\text{LA}) = \frac{2}{3c^2} \sum_{u=1}^3 \sum_{i=1}^{\text{occ}} \sum_{a=1}^{\text{vac}} \frac{\langle \varphi_i | \hat{l}_u^G | \varphi_a \rangle \langle \varphi_a | r_{\text{LA}}^{-3} \hat{l}_u^{\text{LA}} | \varphi_i \rangle}{\varepsilon_i - \varepsilon_a} \quad (6)$$

where ε_i (ε_a) are occupied (vacant) one-electron energies, φ (φ_a) are occupied (vacant) molecular orbitals (MOs), r_{LA} is the electron position operator relative to the position of the LA nucleus, r_G is the electron position operator relative to the position of the gauge origin, c is the speed of light, and

$$\hat{l}^{\text{LA}} = r_{\text{LA}} \times p, \quad \hat{l}^G = r_G \times p \quad \text{and } p \text{ represent the electron momentum operator. In eq 6, the}$$

angular-momentum operator, l^G represents the interaction with an external magnetic field, and the paramagnetic spin-orbit (PSO), $r_{\text{LA}}^{-3} \hat{l}_u^{\text{LA}}$, operator arises from the interaction with the magnetic moment of the LA nucleus. Note that PSO describes the (nuclear-)spin-(electron-)orbit interaction and should not be confused with the (electron-)spin-(electron-)orbit interaction discussed throughout this work.

In the basis-set limit, the position of the gauge vector can be chosen arbitrarily. However, for the MO analysis to be practical, the size of the basis must be within reasonable limits. If there is no HA in the system, the gauge vector is usually placed at the position of the LA nucleus. This choice simplifies the analysis considerably, and at the same time, the size of the basis set can be kept moderately large. In contrast, to keep basis requirements reasonable for systems with one HA, the gauge vector must be placed at the position of this HA, see **eqs 8, 18, and 19** below.⁷⁹ Finally, if there is more than one HA in the system, it is not possible to keep the basis-set requirements sufficiently low, and methods employing GIAOs (or related approaches) must be used. In the following, we will discuss systems containing just one HA.

Equation 6 has been used for decades to successfully analyze NMR shifts of “non-relativistic cases”, i.e., for systems without HA(s). Molecular-orbital analysis based on **eq 6** is performed in three steps: first, identify the frontier MOs (other MOs are insignificant because they bring in larger energy denominators), then select MOs which have nonzero contributions from atomic orbitals of the LA (the function r_{LA}^{-3} enhances contributions from these MOs), and finally, find the most significant occupied-vacant MO-MO* magnetic couplings using the angular-momentum operator, \hat{l}_u^{LA} . A textbook example of this procedure is the $n \rightarrow n^*$ coupling in nitrogen heterocycles such as pyridine, shown in **Figure 1**.

2.3. Theory of Relativistic NMR Chemical Shifts

Given the central role of SO-HALA effects throughout this review, we will concentrate the following discussion on relativistic SO effects.

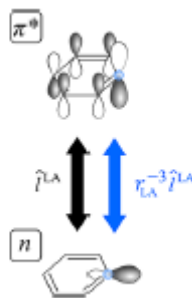


Figure 1. Schematic graphical representation of the Ramsey-type $n \leftrightarrow \pi^*$ coupling in pyridine, which dominates the isotropic ^{15}N NMR shift.⁸⁰ Angular-momentum and paramagnetic spin-orbit operators are shown in black and blue, respectively.

SR effects are briefly discussed below. Each subsection starts with a brief description of the underlying methodology followed by a more detailed discussion focused on the analysis of SO-HALA NMR shifts.

There are two conceptually different approaches to considering SO effects when calculating NMR shifts: two- or four-component methods that describe SO effects variationally and methods that include leading-order SO effects by using perturbation theory.⁸¹⁻⁸⁵

2.3.1. Variational Inclusion of SO Effects

Over the last two decades, the development of new theoretical and numerical techniques has allowed the practical application of relativistic methods that include both SR and SO effects variationally. Aided by growing computational power, these methods have become increasingly popular because of their accuracy and increasing efficiency. The most rigorous methods capable of treating relativistic effects on an equal footing across the Periodic Table of Elements use the four-component Dirac-Coulomb(-Breit) Hamiltonian.⁸⁶ These methods^{73,87-89} were long considered to be too computationally expensive, but it has now been demonstrated that using modern computational techniques, four-component methodology can be applied on a regular basis to systems with more than 100 atoms,⁹⁰⁻⁹² or in an extreme case with more than 300 atoms,⁹³ when combined with Kohn-Sham density-functional theory (DFT). Two-component quasi-relativistic methods⁸⁵ introduce various approximations at different levels of theory to provide a more computationally efficient framework. Therefore, in an ideal situation, two-component methods are first validated against their more accurate four-component counterparts on a particular class of systems and are subsequently used in similar applications to provide, hopefully, an improved compromise between efficiency and accuracy (examples of such comparisons range from halogenated organic compounds⁹⁴ through transition metals^{95,96} to actinide systems⁹⁷). We can distinguish roughly approximate two-component (A2C) and exact two-component (X2C) methods. While in the former the transformation of the one-electron Dirac equation is done only approximately, in the latter it is done to machine accuracy. In both cases, the treatment of the two-electron contributions in the transformation, in particular for the SO effects, is still a matter of development and is usually neglected in practical applications. While X2C-type methods for nuclear shieldings have very recently begun receiving attention,⁹⁸ most practical 2c computations of nuclear shieldings have been done with the zeroth-order regular approximation (ZORA),⁶³ which is an A2C

ansatz. Such SO-ZORA computations and related approaches are currently being applied, with reasonable approximations, to systems containing hundreds of atoms, and they have become the most popular methods for including SO effects variationally into computations of NMR shifts (note that the approximations involved in the ZORA treatment give rise to substantial errors in calculated absolute shieldings).⁶⁷

Detailed analysis of the NMR shifts within a 2c or 4c framework is somewhat complicated, primarily by the complex structures of both the magnetic moment operators and the molecular spinors. Unlike nonrelativistic molecular orbitals, molecular spinors consist of two (four) complex functions in the case of 2c (4c) calculations. For simplicity, we will focus on 2c theory. The isotropic paramagnetic NMR shielding can be written formally as

$$\sigma^{2c,p}(\text{LA}) = \frac{2}{3} \mathcal{R} \sum_{u=1}^3 \sum_{i=1}^{\text{occ}} \sum_{a=1}^{\text{vac}} \frac{\langle \varphi_i^{2c} | \hat{m}_u^{\text{B},2c} | \varphi_a^{2c} \rangle \langle \varphi_a^{2c} | \hat{m}_u^{\mu,2c}(\text{LA}) | \varphi_i^{2c} \rangle}{\varepsilon_i^{2c} - \varepsilon_a^{2c}} \quad (7)$$

Here φ_i^{2c} (φ_a^{2c}) are 2c occupied (vacant) molecular spinors (MSs), ε_i^{2c} (ε_a^{2c}) are 2c occupied (vacant) one-electron energies, $m_{\text{B},2c}$ is a 2c magnetic-moment operator corresponding to the external magnetic field, $\hat{m}^{\mu,2c}(\text{LA})$ is the 2c nuclear magnetic-moment operator of the LA nucleus, and the symbol \mathcal{R} specifies the real part of the following expression. To make the analysis of **eq 7** feasible and tractable but still meaningful in most cases, it is best to use semilocal (nonhybrid) DFT potentials and to omit DFT kernel. For a more detailed discussion of the necessary approximations, see refs **99** and **100**.

Thanks to the time-reversal symmetry of the perturbation-free Dirac-Coulomb Hamiltonian, all MSs are at least doubly degenerate. In the following, we will refer to two MSs with the same one-electron energy as a molecular spinor pair (MSP), also known as a Kramers pair.¹⁰¹ Note that in addition to the complex structures of MSs and magnetic moments, their form differs significantly depending on which 2c theory is used. A pragmatic way to circumvent this problem in the analysis of **eq 7** and provide a conceptual link to the PT3 approach based on the NR wave functions described further below is to focus on only the leading-order effects in a perturbation expansion, which are the same for all 2c theories. These contributions can be expressed as¹⁰⁰

$$\sigma^{2c,p}(\text{LA}) \cong \sigma^{\text{NR},p}(\text{LA}) + P^{\text{AB}} \frac{4\pi}{9c^2} \mathcal{R} \sum_{u=1}^3 \sum_{i=1}^{\text{occ}} \sum_{a=1}^{\text{vac}} \left[\frac{\langle \varphi_i^{\text{SO}} | \hat{l}_u^{\text{HA}} | \varphi_a^{\text{nr}} \rangle \langle \varphi_a^{\text{nr}} | \hat{\delta}^{\text{LA}} | \varphi_i^{\text{nr}} \rangle}{\varepsilon_i - \varepsilon_a} + \frac{\langle \varphi_i^{\text{nr}} | \hat{l}_u^{\text{HA}} | \varphi_a^{\text{SO}} \rangle \langle \varphi_a^{\text{nr}} | \hat{\delta}^{\text{LA}} | \varphi_i^{\text{nr}} \rangle}{\varepsilon_i - \varepsilon_a} \right] \quad (8)$$

where $\delta^{\text{LA}} = \delta(r_{\text{LA}})$ is the Dirac delta function centered on the LA, $\mathbf{1}$ is the two-by-two identity matrix, \mathbf{a} is a vector composed of Pauli matrices,¹⁰² φ_i^{SO} (φ_a^{SO}) are occupied (vacant) linear-response MSs perturbed by the SO interaction

$$\begin{aligned}\varphi_p^{2c} &\cong \varphi_p^{\text{nr}} + \varphi_p^{\text{SO}} \\ &= \varphi_p^{\text{nr}} + \frac{Z^{\text{HA}}}{4c^2} \sum_{\substack{q \neq p \\ q \neq p \pm 1}}^{\text{all}} \frac{\langle \varphi_q^{\text{nr}} | r_{\text{HA}}^{-3} \hat{l}^{\text{HA}} \cdot \boldsymbol{\sigma} | \varphi_p^{\text{nr}} \rangle}{\varepsilon_p - \varepsilon_q} \varphi_q^{\text{nr}}\end{aligned}\quad (9)$$

Z^{N} is the atomic number of nucleus N and φ_i^{nr} , φ_a^{nr} and φ_p^{nr} denote occupied, vacant, and general (occupied or vacant) spin orbitals, respectively. P^{AB} is the permutation operator acting on the operators in the brackets, leading to two additional terms in brackets on the right-hand side (RHS) of **eq 8** (AB+BA). The linear SO correction to the one-electron energies is zero thanks to the symmetry of the SO operator. Therefore, **eqs 8** and **9** are formulated only in terms of the nonrelativistic one-electron energies, ε_p (we refrain here from trying to start from an SRwave function, as this would generate further ambiguities regarding the nature of the perturbation operators). Note that each φ^{nr} can be either an alpha or a beta spin orbital with the same one-electron energy. In **eq 9** we assume that the one-electron energy level ε_p is doubly degenerate and that the corresponding alpha and beta spin orbitals (φ_p^{nr} and $\varphi_p^{\text{nr} \pm 1}$) are excluded from the summation. Furthermore, in the case of one heavy atom in the system, we approximate the SO operator in **eq 9** as

$$\sum_{N=1}^{\text{nuc}} Z^{\text{N}} r_{\text{N}}^{-3} \hat{l}_{\text{N}}^{\text{N}} \cong Z^{\text{HA}} r_{\text{HA}}^{-3} \hat{l}_{\text{HA}}^{\text{HA}}$$

operator couples only states with identical total spin, whereas both $\hat{\delta}^{\text{LA}} \boldsymbol{\sigma}_u$ and $r_{\text{HA}}^{-3} \hat{l}_{\text{HA}}^{\text{HA}}$

$\boldsymbol{\sigma}$ are triplet operators and thus couple states with different total spin. Note also that after some tedious algebraic manipulations with the terms in brackets on the RHS of **eq 8**, we can recover the third-order perturbation theory **eqs 18** and **19** given below. All necessary approximations to make the analysis at the 2c (**eqs 8** and **9**) or 1c (**eqs 18** and **19**) level of theory feasible are given below, and can be found in more detail in refs **99** and **100**.

To analyze the SO corrections to the isotropic paramagnetic NMR shielding, the second term on the RHS of **eq 8**, we use the following guidelines:

- The energy denominator in **eqs 8** and **9** restricts significant contributions to frontier molecular spinors.
- Thanks to the double degeneracy of the MSPs, each energy denominator in each of the four terms in brackets of **eq 8** corresponds to four possible combinations of spin orbitals φ^{nr} and the molecular response spinor φ^{SO} . Fortunately, in most cases, only two of these are nonnegligible, as illustrated in **Figure 3**.
- Thanks to the shortsightedness of the function r_{HA}^{-3} , we can assume atomic-like SO splitting of the nonrelativistic spin orbitals centered primarily on the HA when a single HA is present. However, there are exceptions to this rule. In general, these exceptions occur when the SOC mixes in spin orbitals on neighboring atoms, see, e.g., the description of the trans-ligand influence in section **3.2**.
- Because of the energy denominator in **eq 9** and a usually large HOMO-LUMO energy gap, the SO operator mixes effectively either only occupied or only vacant molecular spinors. In the case of small HOMO-LUMO gaps or large SO-coupling integrals, there can be SO mixing between occupied and vacant spin orbitals, as illustrated by the TIH example in **section 3 (Figure 19b)**.

- The operator $\delta^{LA}\sigma_u$ couples only functions with s-character on the LA. These functions are usually σ -bonding and σ -antibonding orbitals. They can enter **eq 8** as the stand-alone spin orbital φ^{nr} or as part of the SO correction to the MS, φ^{SO} . **Figure 3** below depicts the former case.

To illustrate these points, in **Figures 2** and **3** we deal with a hypothetical system with one occupied σ -bonding MO, two nonbonding MOs and one vacant σ -antibonding MO. **Figure 2** represents **eq 9**, i.e., the construction of the occupied MSP, φ_i^{2c} and φ_{i+1}^{2c} , from NR orbitals. The NR spatial MOs depicted on the left side of both figures are used to construct alpha/beta spin orbitals, $q > nr$, in **eqs 8** and **9**. Each MS then is composed of alpha and beta spin orbitals, φ_i^{nr} and φ_{i+1}^{nr} (left gray box in **Figure 2**), and molecular response spinors, φ_i^{SO} and φ_{i+1}^{SO} (right gray box in **Figure 2**), respectively. For localized SO mixing at the HA, the SO correction φ^{SO} generally contributes to the opposite spin channel (α/β) of the total MS compared to the zeroth-order correction $\langle \Delta nr$. **Figure 3** illustrates the first term in brackets on the RHS of **eq 8**, i.e., one part of the SO correction to the isotropic paramagnetic nuclear shielding.

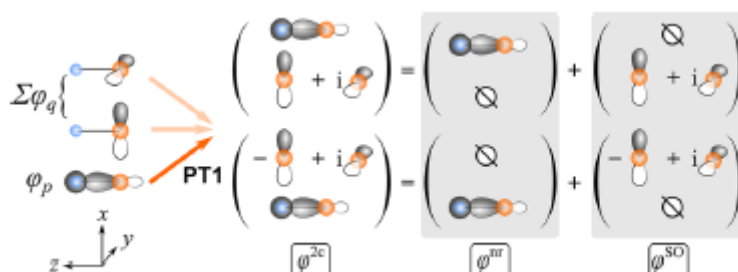


Figure 2. Graphical representation of the composition and creation of a 2c MSP from NRMOs. Every MS φ_p^{2c} is composed of an NR spin orbital and an SO correction φ_p^{SO} . The SO correction to is constructed from the NR spin orbitals φ_q^{nr} by SO mixing within PT1 theory (see **eq 9**).

Here only two out of four possible combinations composed of doubly degenerate spin orbitals φ^{nr} and molecular response spinors φ^{SO} give nonzero contributions. Since the MOs that make up φ^{SO} and φ^{nr} are orthonormal, the angular-momentum operator along the z-direction in **Figure 3** gives zero couplings. The vanishing couplings then explain why the SO correction to the NMR shielding makes a small contribution to the tensor component parallel to the HA-LA bond.⁹⁹

2.3.2. Perturbational Inclusion of SO Effects

As the efficiency of variational 2c and 4c methods has improved over the years, a perturbational inclusion of SO coupling has become less popular for practical calculations. A perturbational treatment does not provide quantitative accuracy for systems with atoms from the sixth period or below, and depending on the type of perturbation theory, various numerical difficulties arise (e.g., variational instabilities and singular operators).⁸⁴ On the other hand, PT treatment constitutes an excellent interpretational tool when it is based on an NR wave function. In contrast to the complex relativistic 2c or 4c MSs (see above), the use of nonrelativistic (real) molecular orbitals results in a natural language to discuss chemical phenomena. Therefore, in practice, 2c or 4c methods are used to obtain quantitative NMR shift data. Then, provided a perturbational treatment of the SO effects reproduces these results sufficiently well, one can use it to analyze the data in the more convenient framework of NR (or SR) MOs. In order to avoid any ambiguities in the nature of the perturbation operators in different SR frameworks, we will, as in the 2c case above, not use SR wave functions as a starting point

in the following discussion. However, it is worth pointing out that in principle the SR wave function can also be a valid starting point for the perturbation analysis of SO effects only.

Within a single-determinantal Hartree-Fock or DFT treatment of a closed-shell singlet system, the nonrelativistic Fock (or Kohn-Sham) equations have the form

$$F^{\text{NR}}\varphi_p = \varepsilon_p\varphi_p \quad (10)$$

where the index \mathbf{p} denotes both occupied and vacant orbitals and energies and φ_p and ε_p are the NR scalar MOs and one-electron energies, respectively, as used also in **eq 6**. In the nonrelativistic theory for closed-shell systems, no operator mixes the alpha and beta parts of a given spin orbital. Therefore, the alpha and beta MOs come in pairs with the same spatial part φ_p . The one-electron part of the Fock operator F^{NR} is a well-known nonrelativistic Schrodinger operator h^{NR} . To take into consideration the lowest-order ($\sim c^{-2}$) relativistic corrections in the absence of the magnetic fields, it is necessary to include three corrections to h^{NR} . The so-called Pauli Hamiltonian then has the form⁸²

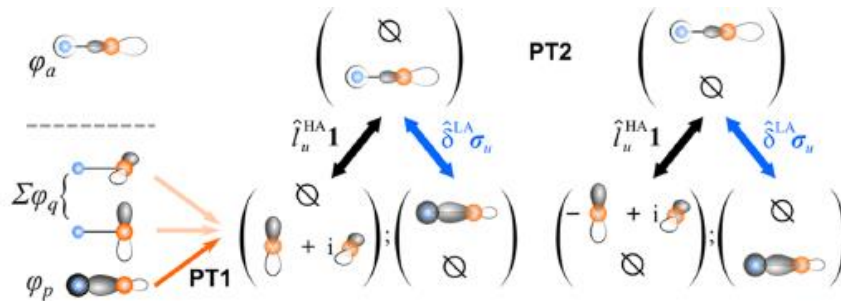


Figure 3. Graphical representation of the SO correction to isotropic paramagnetic NMR shielding at a LA in the framework of 2c relativistic theory. As an example, we schematically visualize the first term in brackets on the RHS of **eq 8**. The NR spin orbitals and the SO correction to the MS are coupled using PT2 theory with 2c Fermi contact $\delta^{\text{LA}}\sigma_u$ (in blue) and angular-momentum ($i_u^{\text{HA}}\mathbf{1}$ (in black) operators.

$$h^{\text{Pauli}} = h^{\text{NR},2c} + h^{\text{MV}} + h^{\text{DW}} + h^{\text{SO}} \quad (11)$$

$$h^{\text{MV}} = -\frac{1}{8c^2}P^4\mathbf{1} \quad (12)$$

$$h^{\text{DW}} = \frac{\pi}{2c^2} \sum_{N=1}^{\text{nuc}} Z^N \delta^N \mathbf{1} \quad (13)$$

Here $\delta^N = \delta(r_N)$ is the Dirac delta function centered on atom N and r_N is the electron position operator relative to the position of nucleus N. The Pauli Hamiltonian (**eq 11**) has a two-component structure in contrast to the scalar form of **eq 10**. This difference is emphasized in a slightly different definition of the Schrodinger operator, $h^{\text{NR},2c} = h^{\text{NR}}\mathbf{1}$. Two of the relativistic operators, the mass velocity h^{MV} and Darwin h^{DW} terms, are clearly SR operators. As they contribute via the identity matrix on the diagonal of the Pauli Hamiltonian, they change only the scalar part of the two-component MOs. In other words, SR operators do not contain spin variables and are sometimes also referred to as “spin-free relativistic” operators. Examples of the well-known SR effects are the (direct) contraction of s-type core orbitals

and the (indirect) expansion of valence orbitals having higher angular momentum.¹⁰³ On the other hand, the spin-orbit operator h^{SO} depends on the Pauli matrices (i.e., on spin variables) and therefore mixes the alpha and beta parts of the MOs and causes the SO splitting.

In the presence of magnetic fields, there are additional relativistic corrections to the Pauli Hamiltonian that we do not list here for the sake of brevity.¹¹ Within perturbation theory, the resulting isotropic paramagnetic NMR shielding can be written formally as

$$\sigma^p(\text{LA}) = \sigma^{\text{NR},p}(\text{LA}) + \Delta\sigma^{\text{REL},p}(\text{LA}) \quad (15)$$

where $\sigma^{\text{NR},p}$ is defined in **eq 6** and $\Delta\sigma^{\text{REL},p}$ contains in total 19 relativistic contributions (up to order c^{-4}) as defined in **ref 11**. Traditionally, the contributions containing h^{MV} or h^{DW} (h^{SO}) are termed SR (SO) relativistic corrections. The remaining contributions cannot be classified easily as SR or SO, but they can be characterized by their (in)dependence on the spin operators.⁵⁶ Fortunately, the majority of the relativistic contributions have negligible effects on the paramagnetic part of the isotropic (relative) NMR chemical shift.^{56,57} One reason is that many of the SR contributions cancel out since they depend only on the core electronic structure around the LA, which is very similar for reference $\sigma_{\text{ref}}(\text{LA})$ and spectator $\sigma(\text{LA})$ isotropic NMR shielding (note the dependence of the Darwin operator, **eq 13**, on the Dirac delta function).^{54,55}

They can nevertheless be sizable, at least for HAs from the sixth period downward (see section 4 for examples). In such cases, both SR and SO effects must be analyzed.^{36-39,104} For the paramagnetic NMR shift we can write

$$\delta^p(\text{LA}) = \delta^{\text{NR},p}(\text{LA}) + \Delta\delta^{\text{REL},p}(\text{LA}) \quad (16)$$

If the system contains only one HA with directly bonded LA, then there are five non-negligible relativistic contributions to $\delta^p(\text{LA})$.¹⁰⁵ Two of them (arising from the mass-velocity and Darwin terms) are SR contributions, which are discussed separately (see **Section 1** and below). Among the remaining three terms, fortunately in most cases only one has a major trend-defining effect on the isotropic shifts. This is the so-called spin-orbit/Fermi-contact contribution, $\sigma^{\text{SO/FC}}$.^{56,60,105} The SO/FC term arises from the contact interaction (represented by the Dirac delta function) between the nuclear and electron spins, and therefore only s orbitals of the spectator LA make nonvanishing contributions to this mechanism (the analogous SO/SD term can also be sizable but does not control the main trends¹⁰⁶). For the chemical concepts arising from this mechanism, see **section 3**. As this term depends on the SO contribution of the nearby HA, it typically will not cancel for relative shifts. Therefore, we can express the dominant relativistic contribution to the paramagnetic isotropic NMR shift as

$$\begin{aligned} \Delta\delta^{\text{REL},p}(\text{LA}) &\cong \delta^{\text{SO}}(\text{LA}) \cong \delta^{\text{SO/FC}}(\text{LA}) = -\sigma^{\text{SO/FC}}(\text{LA}) \\ &= -\frac{1}{3} \sum_{i=1}^3 \sigma_{iii}^{\text{SO/FC}}(\text{LA}) \end{aligned} \quad (17)$$

The term $\delta^{\text{SO}}(\text{LA})$ is referred to as the SO-HALA shift and is usually dominated by the SO/FC contribution, $\delta^{\text{SO/FC}}(\text{LA})$. In **sections 3** and **4**, the SO-HALA shift, $\delta^{\text{SO}}(\text{LA})$, is calculated as the difference between the fully relativistic and scalar relativistic values as described in **section 6.3**. The quantitative analysis of the approximate relation $\delta^{\text{SO}}(\text{LA}) \cong \delta^{\text{SO/FC}}(\text{LA})$ is discussed, for example, in **ref 100**.

2.3.3. Third-Order Perturbation Analysis

Here we discuss the dominant SO/FC contribution to the SO-HALA shift in more detail, to provide the mathematical basis for the MO analysis described in the following sections. In the third-order perturbation theory (PT3) formalism, we can split $\sigma_{uu}^{\text{SO/FC}}$ into two contributions (for example, see refs **106** and **107**):

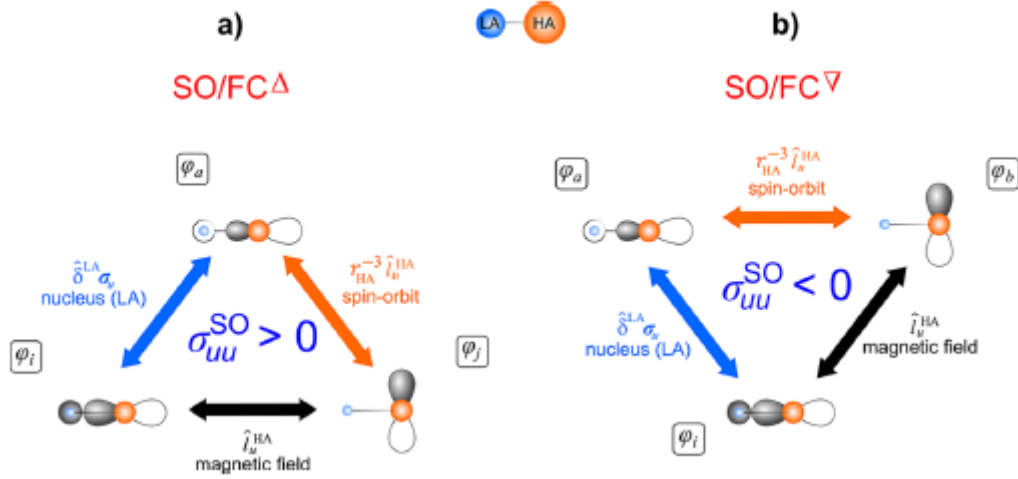


Figure 4. Example of the nonlocal nature of the SO/FC contribution to the LA shielding, which originates at the HA and propagates to the LA via either (a) the SO/FC^Δ mechanism involving two occupied MOs: $\delta_i \leftrightarrow \delta_i \leftrightarrow \delta_a$ (see eq **18**) or (b) the SO/FC^∇ mechanism involving two vacant MOs:

$$\sigma_{uu}^{\text{SO/FC}^\Delta}(\text{LA}) \cong -P^{\text{ABC}} \frac{2\pi Z^{\text{HA}}}{3c^4} \sum_{i=1}^{\text{OCC}} \sum_{j=1}^{\text{OCC}} \sum_{a=1}^{\text{VAC}} \frac{\langle \varphi_a | \hat{\delta}_a^{\text{LA}} | \varphi_i \rangle \langle \varphi_i | \hat{l}_u^{\text{HA}} | \varphi_j \rangle \langle \varphi_j | r_{\text{HA}u}^{-3} \hat{l}_u^{\text{HA}} | \varphi_a \rangle}{(\epsilon_i - \epsilon_a)(\epsilon_j - \epsilon_a)} \quad (18)$$

$$\sigma_{uu}^{\text{SO/FC}^\nabla}(\text{LA}) \cong P^{\text{ABC}} \frac{2\pi Z^{\text{HA}}}{3c^4} \sum_{i=1}^{\text{OCC}} \sum_{a=1}^{\text{VAC}} \sum_{b=1}^{\text{VAC}} \frac{\langle \varphi_i | \hat{\delta}_i^{\text{LA}} | \varphi_a \rangle \langle \varphi_a | \hat{l}_u^{\text{HA}} | \varphi_b \rangle \langle \varphi_b | r_{\text{HA}u}^{-3} \hat{l}_u^{\text{HA}} | \varphi_i \rangle}{(\epsilon_i - \epsilon_a)(\epsilon_i - \epsilon_b)} \quad (19)$$

Here P^{ABC} is the permutation operator acting on the operators in brackets; thus, each of the two eqs **18** and **19** has three contributions (ABC + CAB + BCA). Assuming there is only one HA in the system, we have approximated the SO operator as $\sum_{N=1}^{\text{nuc}} Z^N r_N^{-3} \hat{l}_u^N \cong Z^{\text{HA}} r_{\text{HA}u}^{-3} \hat{l}_u^{\text{HA}}$. We have made other approximations, such as neglecting the two-electron SO interaction, as well as first- and second-order kernels, and using a point-charge model of the charge distribution (for more details, see refs **99** and **100**), which in a semilocal DFT framework makes the analysis of the HALA effect simultaneously feasible and meaningful. Note that eqs **18** and **19** are mathematically equivalent to the second term on the RHS of eq **8**.

Three simple observations from **eqs 18** and **19** are

- A The energy denominator restricts significant contributions to frontier MOs. This restriction is even stronger for energy differences >1 au than in the nonrelativistic case (**eq 6**) due to the square-dependence of **eqs 18** and **19** on these energy differences. In addition, the energy denominator is always positive, and thus it will not influence the sign of **eqs 18** or **19**.
- B Thanks to the function r_{HA}^{-3} , MOs δ_i and δ_a must contain contributions from atomic orbitals centered at the HA.
- C Similarly, thanks to the Dirac delta function δ^{LA} , MOs δ_i and δ_j in **eq 18**, and MOs δ_a and δ_b in **eq 19** must include a contribution from s-type atomic orbitals centered on the LA.

These observations are used to analyze the NMR shifts of hydrogen and 2p atoms in the following sections.

2.4. HALA Effects on ^1H NMR Shifts

Considering that hydrogen as a LA uses almost exclusively its 1s orbital in bonding, and taking the above three observations into account, there are only four types of MOs making significant contributions to the summations in **eqs 18** and **19** in the case of ^1H NMR shifts: the bonding $\sigma_{\text{HA-LA}}$ and the antibonding $\sigma^*_{\text{HA-LA}}$, AO^*_{Ha} , and AO^*_{HA} . Here AO^*_{HA} (AO^*_{HA}) denote occupied (vacant) molecular orbitals containing appreciable contributions from atomic orbitals at the HA. An example of AO^*_{HA} is a nonbonding orbital at the HA (η_{HA}), often denoted lone pair (LP), or a bonding orbital with other ligand atoms (HA-L bond). However, the latter type is typically lower in energy, and the energy denominator thus diminishes its effect. In the following, we abbreviate the sigma HA-LA orbitals as σ and σ^* , when appropriate.

Equations 18 and **19** give rise to six different terms, each of which contains three integrals. Of these, one includes a delta function, and two contain an angular-momentum operator. Two examples of such terms are visualized in **Figure 4**. The vertices of the triangle represent the involved MOs, while the orientation of the triangle corresponds to their energy (higher-lying vacant orbitals at the top and lower-lying occupied orbitals at the bottom). Each edge of the triangle coincides with an operator that couples the MOs across the corresponding vertices. The three operators involved in the SO/FC mechanism are the SO-coupling, Fermi-contact, and angular-momentum operators. The role of the SO-coupling term, which in analogy to the PSO term in Ramsey's equation has a rather local character, is to provide a coupling between two HA-based p-, d-, or f-type orbitals. In the following graphical representations this operator

$$\left(r_{\text{HA}}^{-3} \hat{l}^{\text{HA}} \right)$$

The Fermi-contact interaction term σ^{LA} , highlighted in blue, is particularly sensitive to the electronic structure around the LA (also shown in blue). It gives nonzero couplings only for σ -bonding and σ -antibonding orbitals since only these orbitals have a significant s-type contribution at the LA. In contrast to the PSO term (see above), the FC term represents a direct interaction of the magnetically induced electron-spin density with the LA nuclear magnetic moment.

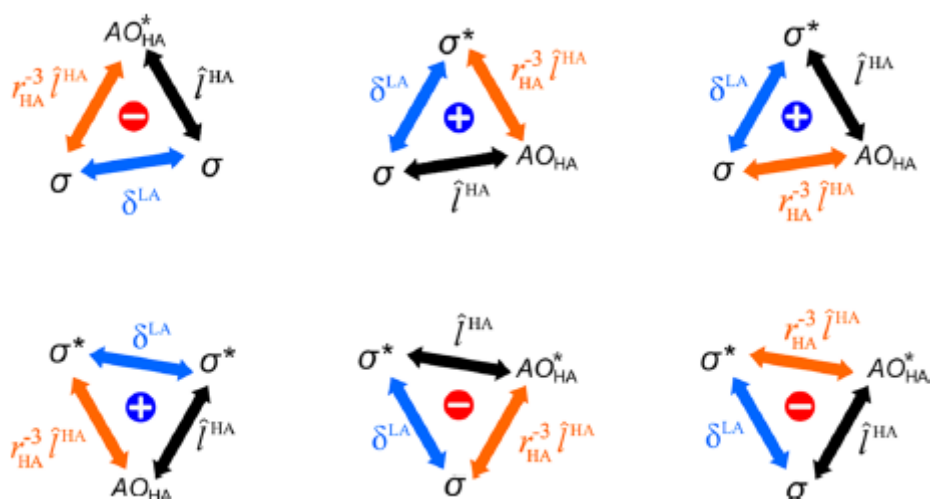


Figure 5. Schematic representation of the six MO coupling terms (triangles) active in the ^1H SO-HALA shielding, **eq 18** (upper three triangles) and **eq 19** (lower three triangles).⁹⁹ Four types of molecular orbitals are involved in the coupling, sigma HA-LA (anti)bonding MOs and occupied (vacant) MOs with significant AO_{HA} (AO_{HA}^*) contribution (examples are nonbonding MOs, η_{HA} , denoted alternatively as LP_{HA}). SO, FC, and angular-momentum operators are shown in orange, blue, and black, respectively.

The remaining coupling term represents the applied external magnetic field through the angular-momentum operator I^{HA} (analogous to the orbital Zeeman term in Ramsey's equation, **eq 6**). The mutual interplay among all three perturbations is shown schematically on an MO triangular diagram in **Figure 4**. Note that, while the FC and SO operators describe local interactions, their interplay results in the nonlocal nature of the SO/FC contribution to the SO-HALA shift. In the PT3 scheme, the SO/FC mechanism involves two occupied MOs and one vacant MO for the SO/FC^Δ term but one occupied MO and two vacant MOs for the SO/FC^Δ contribution, see **Figure 4** and **eqs 18** and **19**.⁹⁹ If the FC operator couples two occupied MOs in SO/FC^Δ or two vacant MOs in SO/FC^Δ , then these MOs can be identical, see the first triangle in each row in **Figure 5**.

To explain trends of SO-HALA NMR shifts across the Periodic Table¹⁰⁰ (**sections 3** and **4**), it is necessary to analyze **eqs 18** and **19** in detail. The signs of all six terms in **eqs 18** and **19** (triangles in **Figure 5**) can be deduced by the following reasoning. The final value of each of the six terms is invariant to the change of the phase (sign) of the molecular orbitals. Therefore, we can fix the sign of the HA AO contributing to the $\sigma_{\text{HA-LA}}$ and $\sigma_{\text{HA-LA}}^*$ MOs to be positive. This choice has two consequences:

1. The hydrogen 1s orbital contributes to $\sigma_{\text{HA-LA}}$ and $\sigma_{\text{HA-LA}}^*$ with opposite sign, which results in the following signs of the integrals involving the Dirac delta function: $(\sigma|\delta^{\text{LA}}|\sigma) > 0$, $(\sigma^*|\delta^{\text{LA}}|\sigma^*) > 0$, $(\sigma|\delta^{\text{LA}}|\sigma^*) < 0$, and $(\sigma^*|\delta^{\text{LA}}|\sigma) < 0$.
2. Second, if we assume that intra-atomic contributions dominate interatomic ones, all four integrals, $\langle X|\hat{l}_u^{\text{HA}}|\sigma\rangle$, $\langle X|\hat{l}_u^{\text{HA}}|\sigma^*\rangle$, $\langle X|r_{\text{HA}}^{-3}\hat{l}_u^{\text{HA}}|\sigma\rangle$, and $\langle X|r_{\text{HA}}^{-3}\hat{l}_u^{\text{HA}}|\sigma^*\rangle$, with X being either AO_{HA} or AO_{HA}^* , have the same sign. This assumption is less general, and we'll discuss some counterexamples below.

The second assumption is well satisfied for the SO integrals ($r_{\text{HA}}^{-3}\hat{l}_u^{\text{HA}}$), as the function r_{HA}^{-3} enhances AO contributions at the HA while those from the other atoms are quenched. Furthermore, it turns out that in practice the angular-momentum integrals (\hat{l}_u^{HA}) follow the same trend, even without the benefit

of such a short-sighted rHA function. The second consequence is also crucial in understanding the final signs in eqs 18 and 19. It is cumbersome to determine the signs of all SO or angular-momentum integrals, but since they always appear in pairs, their signs are not needed, and their joint contribution is always positive. Combining the above arguments, the final signs of the different contributions in eqs 18 and 19 can be easily determined as illustrated in Figure 5. See section 3 for chemical interpretations.

While the determination of the signs of the different triangles described in Figure 5 works surprisingly well, there are still cases where different signs may occur:

- In the less common event that an orbital with c-antibonding character for the HA—LA bond is occupied, i.e., when one sigma bonding orbital is replaced by an occupied antibonding orbital, the corresponding triangle will change sign. This can occur in cases where a given MO has both bonding and antibonding characteristics in nontrivial molecular systems.
- A similar situation may occur when a virtual MO has partial c-bonding character with respect to the HA-LA bond.
- The simpler sign rules also come into question when the interatomic contributions to magnetic couplings are nonnegligible (see point 2 above) as their sign is not governed by simple rules as is the case for intra-atomic contributions. This can occur when the intra-atomic contributions at HA vanish for reasons of symmetry (e.g., coupling of p- and d-atomic orbitals). One such case is the trans-ligand influence described in section 3.

2.5. HALA Effects on the NMR Shifts of 2p Atoms

In the case of NMR shifts of 2p LAs, we must also consider bonding and antibonding π orbitals ($\pi_{\text{HA-LA}}$, $\pi^*_{\text{HA-LA}}$). In this paragraph, we will discuss only arguments that are specific to the chemical shift of 2p elements, since the arguments presented above for ^1H shifts are applicable in this case without any changes. In most applications, we can assume that neither the bonding $\pi_{\text{HA-LA}}$ nor the antibonding $\pi^*_{\text{HA-LA}}$ orbital contain s-type AOs from the light atom LA. Then all π -type orbitals are excluded from couplings with the delta function δ^{LA} , and the only way π -type orbitals can influence the SO contribution to the LA shielding, $\sigma^{\text{SO/FC}}(\text{LA})$, is through AO_{HA} and AO^*_{HA} orbitals. Note also that π -type orbitals are more likely to have non-negligible interatomic contributions as is demonstrated in the discussion on trans-ligand influence in section 3.

2.6. Connection between the SO-HALA Shift and the Electron Density

In this section, we rationalize the connection of the relativistic SO contribution to the LA NMR shift, and the SO-induced electronic charge density. For closed-shell singlet systems, the first nonzero response of the electronic charge density to SO coupling is quadratic. In the following, we will refer to this function as $\rho_0^{\text{SO,SO}}$ or SO-EDD (spin-orbit-induced electron deformation density).⁹⁹ The SO-EDD does not depend on the external magnetic field. Its relation to the SO-HALA shift is thus not immediately obvious.

It has been pointed out¹⁰⁸ that the first-order SO effects on the NMR shielding tensor are generated exclusively by spin currents

$$\mathbf{j}^{\text{spin}} = -\nabla \times \boldsymbol{\rho} \quad (20)$$

Here ρ represents the electron spin density. Focusing on the Fermi-contact mechanism and the fact that $\sigma^{\text{SO/FC}}(\text{LA})$ is expressible as an integral of the spin-current j_{spin} and the vector potential generated by the magnetic moment of the LA nucleus, one arrives at the relation¹⁰⁰

$$\sigma^{\text{SO/FC}}(\text{LA}) = \frac{8\pi}{9c} [\rho_x^{\text{B},\text{SO}}(\text{LA}) + \rho_y^{\text{B},\text{SO}}(\text{LA}) + \rho_z^{\text{B},\text{SO}}(\text{LA})] \quad (21)$$

where $\rho^{\text{B},\text{SO}}(\text{LA})$ denotes the bilinear response of the electron-spin density with respect to the magnetic field and the SO operator evaluated at the position of the LA. We will use the abbreviation SOM-ISD (spin-orbit-and-magnetically induced spin density)¹⁰⁰ for the function $\rho^{\text{B},\text{SO}}$.

In the case where only one HA is present in the system, a simple proportionality connection of SOM-ISD¹⁰⁰ and SO-EDD⁹⁹ can be derived from PT3 theory:¹⁰⁰

$$\frac{Z^{\text{HA}}}{c} [\rho_x^{\text{B},\text{SO}}(\text{LA}) + \rho_y^{\text{B},\text{SO}}(\text{LA}) + \rho_z^{\text{B},\text{SO}}(\text{LA})] \sim \rho_0^{\text{SO,SO}}(\text{LA}) \quad (22)$$

This expression follows from the assumption that angular-momentum and SO integrals are proportional

$$\langle \varphi_p | r_{\text{HA}}^{-3} \hat{l}_u^{\text{HA}} | \varphi_q \rangle \sim \langle \varphi_p | \hat{l}_u^{\text{HA}} | \varphi_q \rangle \quad (23)$$

In practice, this assumption holds when **eq 22** is evaluated at the position of (or in close proximity to) the LA. In this case the MOs involved in **eq 23** arise from the set $\sigma_{\text{HA-LA}}$, $\sigma_{\text{HA-LA}}^*$, $\pi_{\text{HA-LA}}$, $\pi_{\text{HA-LA}}^*$, AO_{HA} , or AO_{HA}^* . When **eq 22** is evaluated closer to the HA, other MOs, for which the proportionality of the integrals in **eq 23** breaks down become involved (see **Figure 13** in **section 3**).

Collecting the results from **eqs 17, 21, and 22**, we arrive at a simple, approximate connection between the isotropic SO-HALA shift, the SOM-ISD, and the SO-EDD at the position of the LA:¹⁰⁰

$$\Delta \delta^{\text{REL},p}(\text{LA}) \cong -\frac{8\pi}{9c} [\rho_x^{\text{B},\text{SO}}(\text{LA}) + \rho_y^{\text{B},\text{SO}}(\text{LA}) + \rho_z^{\text{B},\text{SO}}(\text{LA})] \sim -\frac{8\pi}{9Z^{\text{HA}}} \rho_0^{\text{SO,SO}}(\text{LA}) \quad (24)$$

As a result, the sign of $\Delta\delta^{\text{REL},\rho}(\text{LA})$ can be predicted just by the changes in the SO-EDD.^{99,100} This argument runs parallel to typical (nonrelativistic) arguments in NMR studies that link changes in the electron density near the NMR nucleus to its shielding in different chemical environments. It is well-known,¹³ however, that such correlations may fail when other aspects, such as energy denominators or angular momentum matrix elements, become important. While for the present SO case the link to the SO-EDD can likely explain the signs of the SO-HALA contributions, we anticipate that it will not hold generally when discussing more detailed trends.

3. CHEMICAL CONCEPTS: THE HA-LA INTERACTION

3.1. Mechanism, Factors Involved, and Tools for Interpretation

As has been demonstrated in the previous sections, the NMR chemical shift is intimately connected, albeit in a nontrivial way, to the distribution of electron density in the molecular or supramolecular system. Note that this does not mean just atomic charges, as frequently argued and discussed in the literature, but the full quantum electronic structure. In any case, chemists are taught to work with, and think in terms of, “chemical bonds” which somehow reflect interactions between two or more atoms in real space. A weakness of this broadly defined concept is that there is no quantum-mechanical operator that links the concept of a “chemical bond” to the quantum-mechanically defined NMR shielding constant. Yet, there have been many attempts to formulate links between the character of the HA—LA interaction and the SO-HALA NMR shift at the qualitative or semiquantitative level. In the following we will discuss such links from the perspective of a chemist.

3.1.1. Spin—Orbit/Fermi-Contact (SO/FC) Mechanism of the SO-HALA Shift

a). “The Fermi-contact step” of the SO/FC mechanism: the role of the s-character of the LA in the HA—LA bond. As has been shown in **section 2**, the SO-HALA shift ($\delta_{\text{LA}}^{\text{SO}}$ in **eq 17**) is typically dominated by the Fermi-contact mechanism, SO/FC. While the spin-dipole (SO/SD) term is included in modern two- or four-component computations and thus contributes to the quantitative SO-HALA data, it tends to be less important¹⁰⁶ and is not considered in our qualitative reasoning throughout this review.

The conceptual analysis of the SO/FC mechanism, from the early work of Nomura et al.¹⁹ over semiempirical implementations³⁰ to the first detailed treatment in DFT calculations,²⁶ has been described in the historical pre-2004 overview in **section 1**. While the individual “thought steps” elaborated below are part of one single SO/FC mechanism and thus act simultaneously, we introduce and discuss them separately for explanatory purposes and for the convenience of the reader.

Following the arguments presented in **ref 26**, the close and helpful analogy between the Fermi-contact mechanism of the indirect nuclear spin—spin coupling constant ($J_{\text{LA}}^{\text{FC}}$) and that of the SO-HALA shift ($\delta_{\text{LA}}^{\text{SO/FC}}$) is illustrated in **Figure 6**.

In both cases, the “last step” of the mechanism is linked to the Fermi-contact interaction between the induced electron-spin density surrounding the spectator NMR-active nucleus LA (not necessarily a “light atom”, literally) and its nuclear magnetic moment (**Figure 6**, left). In the FC mechanism of $J_{\text{LA-X}}^{\text{FC}}$, the spin density around x is generated in the “first step” by the nuclear magnetic moment of x (**Figure 6**, top right). In contrast, the spin density around the HA in the “first step” of the SO/FC mechanism of

the SO-HALA NMR shift is induced by spinorbit coupling in the presence of a magnetic field (**Figure 6**, bottom right).

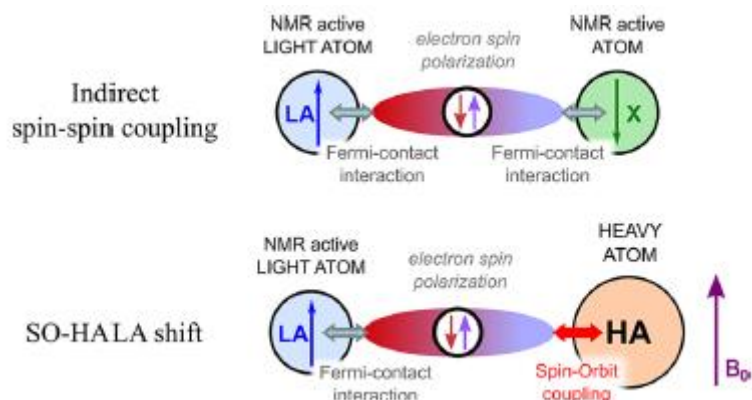


Figure 6. Schematic representation of the analogy between the Fermi-contact mechanism of the indirect spin-spin coupling constant (J_{LA-X}^{FC}) and that of the SO-HALA shift ($\sigma_{LA}^{SO/FC}$) based on the idea of **ref 26**. Note that for consistency with the SO-HALA mechanism, the NMR spectator atom is labeled LA also in the case of indirect spin-spin coupling.

In an “intermediate step”, the induced electron-spin density around the HA (or X) is propagated throughout the system to reach the spectator LA. Here the spin density interacts with the nuclear magnetic moment of the LA via the FA interaction.

Clearly, a larger involvement of the valence *s* orbital of the LA in the HA-LA bond, i.e., a high LA *s*-character of the hybrid orbital employed by the LA for HA-LA bonding and efficient HA↔LA electron sharing, enables the spin-polarization mechanism to induce a larger spin density near and at the LA nucleus, causing a more significant FA interaction and enhancing δ_{LA}^{SO} . The correlation between the LA *s*-character of the HA-LA bond and δ_{LA}^{SO} has been demonstrated widely and for various classes of compounds, see **section 1**. Textbook examples of increasing *s*-character involve sp^3 , sp^2 , and sp -hybridized carbon atoms bonded to heavy halogen(s),²⁶ particularly iodine, as shown in **Figure 7a**.

Note that the effect of multiple-halogen substitution at the carbon atom on the ^{13}C SO-HALA shift is nonlinear as shown in **Figure 7b**. As more electronegative halogens are attached to the LA, increasing hybridization defects enhance the LA *s*-character of the HA-LA bond and thus lead to nonadditive behavior.³ A similar dependence has been demonstrated for hydrides of transition-metals⁹⁵ and actinides.⁹⁷ For various examples of these effects, see **Section 4**.

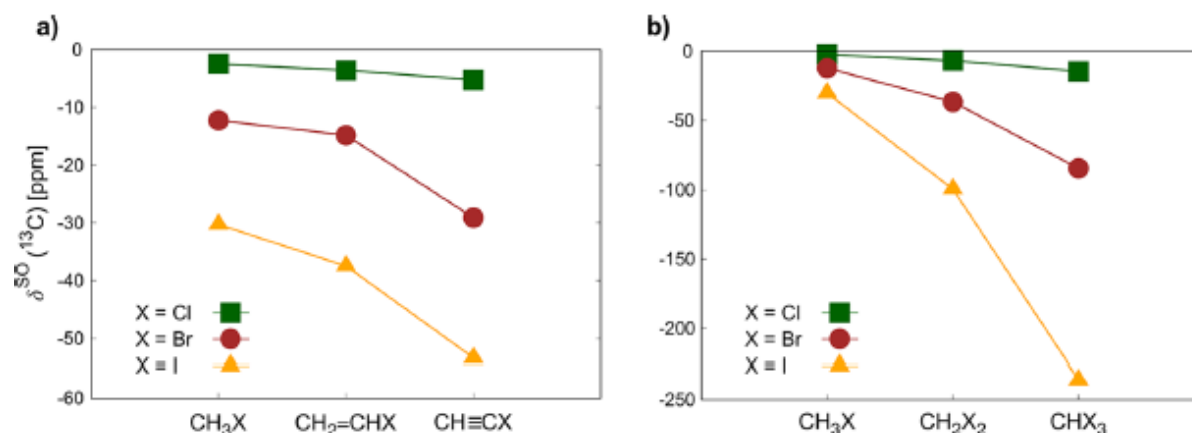


Figure 7. Effect of (a) carbon hybridization (sp^3 , sp^2 , and sp) and of (b) the number of halogen atoms attached (1 -3) on the magnitude of the ^{13}C SO-HALA shift (δ^{SO}). The data were calculated using methods specified in **section 6.1** (method 1) and **section 6.3**. For analogous plots based on perturbational SO treatments, see **refs 3** and **26**.

b). "The spin-orbit step" of the SO/FC mechanism: Involvement of the HA orbitals in the HA-LA bond. In addition to the LA character of the HA-LA bond discussed above, one can look at the SO/FA mechanism from the opposite direction, studying the involvement of the HA valence orbitals in the HA-LA interaction. For example, the HA d-character of the HA-LA bond in transition-metal complexes has been reported to have a significant effect on the electronic structure around the HA, governing the "initial spin-orbit step" of the SO/FA mechanism.¹⁰⁹ This is demonstrated on a set of model PyAu(I)X (Py = pyridine) complexes with various trans substituents X which modulate the Au d-character of the HALA bond in **Figure 8**.

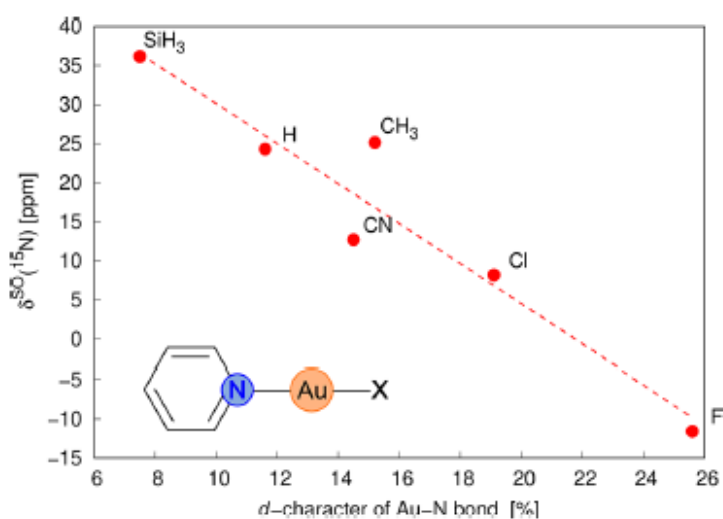


Figure 8. Relationship between the HA d-character¹⁰⁹ of the HA-LA bond in PyAu(I)X and $\delta_{\text{LA}}^{\text{SO}}$. The data were obtained using methods specified in **section 6.1** (method 1), **section 6.2**, and **section 6.3**.

Two main factors influence the magnitude of the SO-based magnetically induced spin density at the HA. They are linked fundamentally to the electron g-factor in the EPR spectroscopy of open-shell systems.^{109,110}

- (i) The nuclear charge (atomic number) of the HA affects the magnitude of the relativistic spin-orbit effects as shown in **eqs 14, 18, and 19**. The dependence of SO splitting on the atomic number Z^{HA} can be easily understood (albeit not quantitatively) using semiclassical physical arguments. In the electron frame, the HA nucleus revolves around the electron and generates an effective magnetic field at the position of the electron.

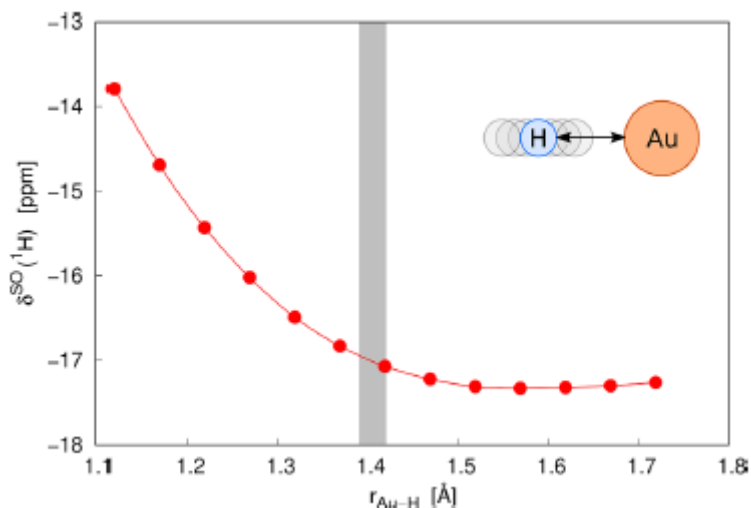


Figure 9. Effect of the interatomic HA-LA distance on the magnitude of $\delta^{\text{SO}}(^1\text{H})$ for AuH. This can be related to a similar effect of the interatomic distance on the indirect nuclear spin-spin coupling.¹¹² The data were obtained using methods specified in **section 6.1** (method 2) and **section 6.3**. The gray bar highlights the optimized equilibrium distance.

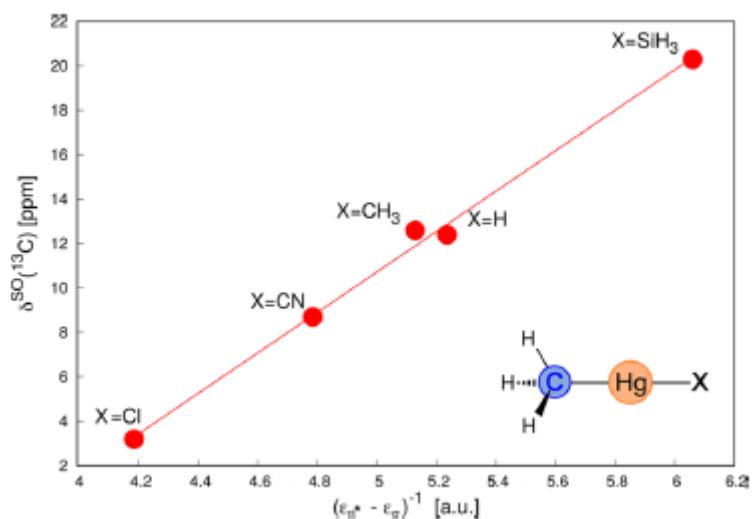


Figure 10. Correlation of $\delta^{\text{SO}}(^{13}\text{C})$ in CH_3HgX compounds with the inverse of the energy difference between the occupied $\sigma_{\text{HA-LA}}$ and vacant HA nonbonding (η^*_{HA}) Kohn-Sham orbitals involved in the dominant $\sigma_{\text{HA-LA}} \leftrightarrow \eta^*_{\text{HA}}$ MO coupling. Data from **ref 38**.

This magnetic field depends linearly on the nuclear charge (ZHA) and, coupled with the spin of the electron, gives the SO interaction (an effective nuclear charge maybe used when also accounting for two-electron SO contributions).

- (ii) The type of frontier MOs at the HA governs their SO splitting. That is, SOC does not directly influence the s orbitals, whereas valence p, d, and f orbitals are affected to different extents, depending also on their principal quantum number, for example, inner ($\eta - 1$)d orbitals vs outer np orbitals.

Considering (i), the nuclear charge is essentially a physical property, not a chemical concept. However, different HAs can exhibit principally different bonding with the LA, or with linking atoms for effects across more than one bond, see **section 3.1.4**. Naturally, larger relativistic effects are expected going down the Periodic Table (albeit energy gaps may counteract this trend for transition metals, see the inverted V-shape dependence below), whereas shell-structure effects cause the largest SO effects in each period to be found toward the right side of the Periodic Table, albeit exceptions do exist in the p-block, see **section 4**. Concerning (ii), the composition of the relevant valence MOs in terms of contributing angular momentum at the HA is crucial. For example, heavier elements of groups 2 (alkaline earth metals) and 12 (zinc group) exhibit notable $(n - 1)d$ - and np -character, respectively, in their chemical bonding. As a result, they share many features with $d(p)$ elements while formally being considered $s(d)$ -block HAs. For examples and effects on δ_{LA}^{SO} , see **section 4**.

c). Link between the FC and SO steps: Covalency of the HA—LA bond. The efficiency with which the electron-spin density induced by SO coupling at the HA in the presence of a magnetic field is propagated to the spectator LA nucleus is tightly connected to the degree of electron sharing between the atomic basins of the HA and the LA, and thus to the covalency of the HA—LA bond.^{104,111,114} This aspect can be considered a third piece of the puzzle in our understanding of the SO-HALA mechanism, in addition to the individual characters of the HA and the LA. Note, however, that the HA and LA character of the HA—LA bonding, and the HA—LA covalency are mutually interconnected. Naturally, the electron sharing for the HA—LA interaction depends on the interatomic HA—LA distance as does δ_{LA}^{SO} ,⁴⁷ but this dependence is clearly nonlinear (see **Figure 9**).

The magnitude of electron sharing between the HA and the LA can be described as follows:

- (i) The covalency of the HA—LA bond is reflected in the relative positions of the frontier-orbital energies, in particular the gap between the occupied MOs dominating the HA—LA interactions and the associated vacant MOs of appropriate symmetry (see PT3 theory in **section 2**). A clear correlation between the energy gap of the “HALA MOs” and δ_{LA}^{SO} has been demonstrated for a series of CH_3HgX complexes,³⁸ **Figure 10**.

The role of the energy gap has also been used to explain the rather striking observation of a counterintuitive “inverted V-shape” dependence^{9,113} of the SO-HALA effect down group 9, an example of which is shown in **Figure 11**. This is due to the generally smaller ligand-field splitting in 3d systems caused by the absence of a radial node in the 3d shell and the resulting stretched-bond situation.⁴⁶ This reduces the (square) energy denominators in the PT3 expressions (**eqs 18 and 19 in section 2**) and renders the SO-HALA effects larger in 3d compared to the analogous 4d complexes.

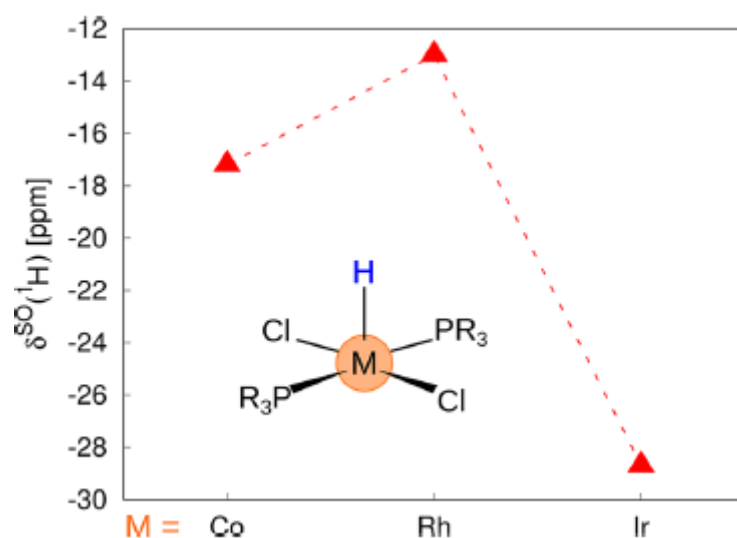


Figure 11. “Inverted V-shape” dependence of $\delta^{\text{SO}}(^1\text{H})$ for a set of group 9 model compounds. Data from ref 95.

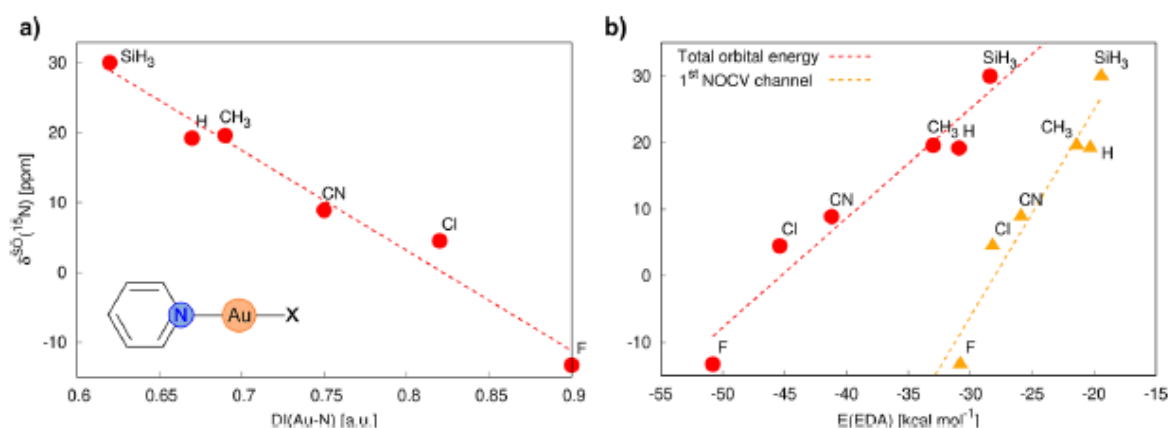


Figure 12. Relationship between the ^{15}N SO-HALA shifts ($\delta^{\text{SO}}_{\text{LA}}$) in PyAuX compounds and (a) the delocalization index (HA \leftrightarrow LA) for the HA-LA bond¹¹⁴ and (b) the orbital contribution to the EDA¹¹⁶ bond energy (red) and ligand donation (orange) as quantified by the first NOCV-channel¹¹⁷ of the EDA/NOCV analysis (see section 6.2).⁹⁹ Data from ref 99.

Indeed, the Rh complex exhibits a less negative $\delta^{\text{SO}}_{\text{LA}}$ than its Co analog (**Figure 11**), as has also been found for smaller three-bond ^1H NMR effects in a series of polyamine complexes. While the energy denominators increase further from Rh to Ir due to the SR expansion of the 5d orbitals, the effect is more than compensated by the larger SO splitting of the 5d element, leading, overall, to the inverted V-shape.

- (ii) Second, the covalency of the HA-LA bond can be quantified by electron sharing between the atomic basins of the HA and the LA as described, for example, by the

delocalization index (DI, HA \leftrightarrow LA)¹¹⁴ of the Quantum Theory of Atoms in Molecules (QTAIM). A larger covalency is reflected directly in a larger DI as has been demonstrated for a series of transition-metal complexes,^{114,115} for which the DI correlates with the SO-HALA shifts, **Figure 12a**.

In a complementary fashion, the covalent character of the HA-LA bond has been investigated by energy decomposition analysis (EDA) and natural orbitals for chemical valence (NOCV) analysis, with the results also linked to δ^{SO}_{LA} , **Figure 12b**. Here, the larger covalency is reflected in both the more negative orbital stabilization energy and the more negative energy of the first NOCV bond channel, which reflects the ability of the ligand containing the LA (pyridine in **Figure 12**) to make a σ -donation to the Au-X unit.

3.1.2. Visualization Tools: SOM-ISD and SO-EDD

The propagation of the spin density induced at the HA by SO and the magnetic field during the “initial SO step” through to the last “Fermi-contact step” at the LA can be visualized by the real-space distribution of the SO-and-magnetically induced spin density (SOM-ISD, eq 24 in section 2)¹⁰⁰ shown in **Figure 13a** for model Au¹H and PhHg¹H systems as examples. These plots clearly demonstrate that the induced α or β spin density around the spectator hydrogen LA is reflected in a negative or positive sign of $\delta^{SO}(^1\text{H})$, respectively.

It has also been shown previously that the SO-HALA shift can be correlated with the SO-induced electron deformation density (SO-EDD)⁹⁹ around the spectator NMR-active nucleus. This is the change in the total ground-state charge density due to SO coupling (section 2) and is shown in **Figure 13b** for the same two systems. Despite the different patterns in electronic structure around the HA, the SO-induced charge density (SO-EDD) surrounding the LA parallels the SOM-ISD patterns.

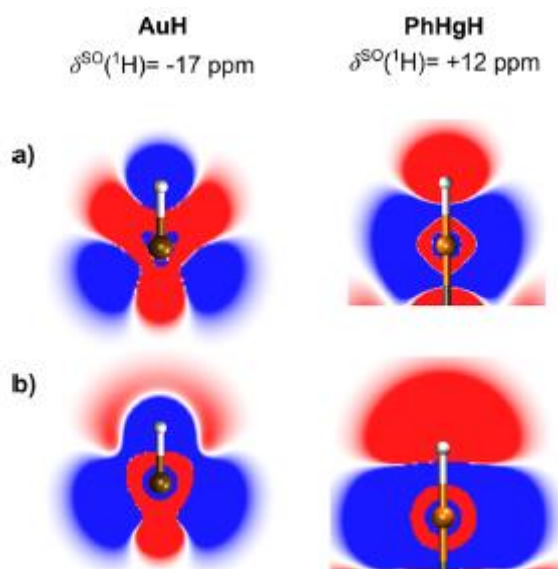


Figure 13. (a) Visualization of the SOM-ISD in Au¹H (left) and PhHg¹H (right). The local spatial predominance of α or β induced spin density is shown in blue and red, respectively. The calculated ¹H SO-HALA shifts (δ^{SO}_{LA}) are also shown for comparison. (b) Visualization of the SO-EDD in Au¹H and PhHg¹H. The accumulation and depletion of electron density

induced by SO coupling is shown in blue and red, respectively. The data were obtained using methods specified in **section 6.1** (method 1), **section 6.3**, and **section 6.4**.

3.1.3. Structural and Electronic Influence of a trans Ligand

Particularly in the case of the HA being a transition metal, the character of the HA-LA bond can be substantially altered by the nature of the substituent or ligand bonded to the HA in the trans-position relative to the LA (labeled as TL or X), as had already been noted early on for d^{10} LA-Hg-TL systems.³⁸ The structural and electronic trans-ligand influence (TLI, also known as thermodynamic trans-effect or structural trans-effect) on the SO-HALA shift can be modeled computationally by changing the HA-TL bond length as has been demonstrated first for an octahedral Ir(III) complex.¹¹⁸ While both scalar-relativistic and spin-orbit contributions to the NMR shifts are affected by the changes in the HA-TL distance, the modulation of the SO-HALA contribution is by far the more significant (see also **section 4**). The effect of the Au-TL distance on the ^1H SO-HALA shift of the trans hydride in $\text{HAu}^{\text{I}}\text{TL}$ is shown in **Figure 14**. Note the reversal of the sign of the SO-HALA shift near the equilibrium distance of about 1.95 Å, highlighted by a gray vertical bar. The structural and electronic TLI is also reflected in an inverted spin density around the LA as shown by the SOM-ISD for the short (left) and long (right) HA-TL distance.

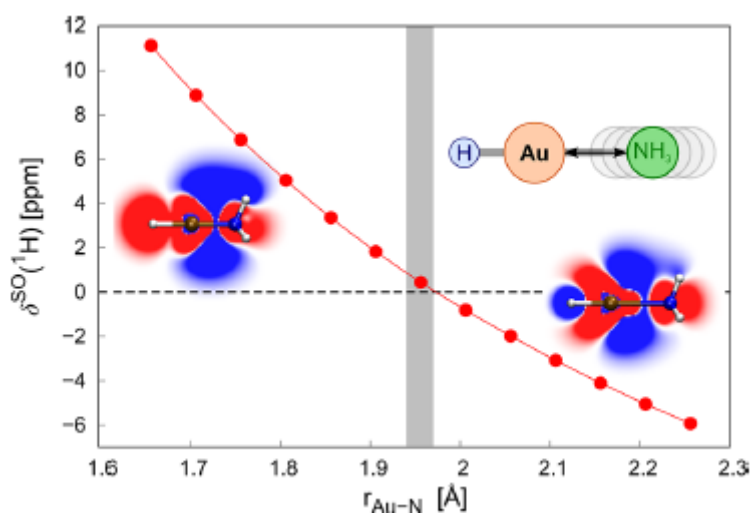


Figure 14. Effect of the HA-TL distance on the SO contributions¹¹⁸ to the ^1H NMR shift in HAuNH_3 . Note the change in the sign of the SO-HALA contribution around the equilibrium distance (indicated by a gray vertical bar). The SOM-ISD calculated for the short and the long HA-TL distances is shown on the left and the right, respectively. Note the change in color (opposite induced spin density) around the hydrogen atom. The data were calculated using methods specified in **sections 6.3** and **6.4**.

The TLI on the SO-HALA shift has been elaborated upon extensively in a series of papers on iridium, platinum, gold, and mercury complexes.^{99,109,114,115,119,120} The electronic TLI has been rationalized by the simultaneous involvement of a central HA orbital with both the TL and the LA. In other words, the two trans-arranged ligands share a single HA atomic orbital (AO) in their bonding. As a result, the polarization of HA-centered AOs by one of the substituents (e.g., the TL) induces a significant repolarization of the same orbital on the side of the second substituent (e.g., the LA)⁹⁹ The two substituents thus mutually influence the character of their bonding with the HA center, where the increasing polarity of the bond to the TL (smaller HA AO character in the HA-TL bond for a weaker

trans-ligand) results in a more covalent bonding with the LA. The effect of the nature of the TL on the SO-HALA shift is shown in **Figure 15**.

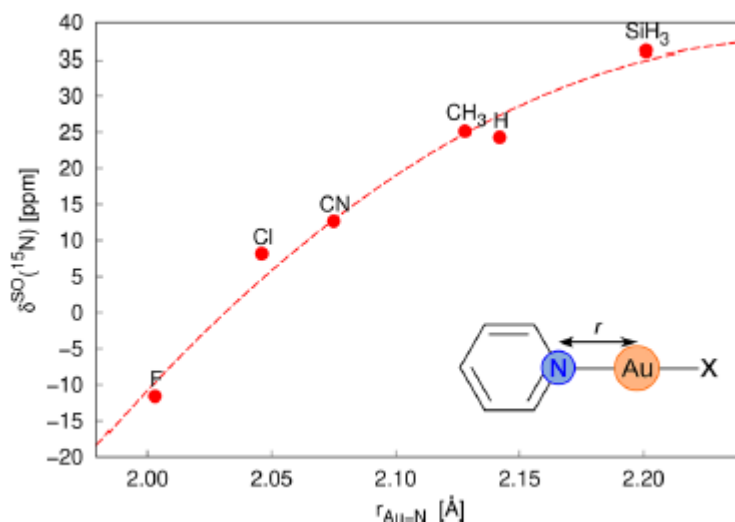


Figure 15. Influence of the trans-ligand (X) on the equilibrium HA—LA distance, r , and the SO contribution to the ^{15}N NMR shift ($\delta^{\text{SO}}_{\text{LA}}$) for a pyridine ligand.⁹⁹ The data were obtained using methods specified in **section 6.1** (method 1) and **section 6.3**.

We note that matters are rather different for actinide systems, where the intrinsically ungerade character of the 5f-AOs, as opposed to the gerade character of d-type AOs in transition-metal complexes, is known to contribute to an inverse TLI for structural and electronic properties.¹²¹⁻¹²⁴ Such an inverse TLI has been found to affect ^{13}C SO-HALA shifts in UVI complexes in a relatively complicated manner.⁹⁷ As the valence p-orbitals are also intrinsically ungerade in nature, substituents in different positions likely affect SO-HALA shifts differently in heavy p-block compounds, although this has yet to be investigated in detail.

3.1.4. Long-Range SO Effects

As shown in Figure 6 above, there is a clear parallel between the FC mechanism of SO-HALA shifts and the FC contribution to indirect nuclear spin—spin couplings (see also Introduction). Thus, the SOM-induced spin density around the HA (see **section 3.1.1**) for the SO-HALA effect and the spin density around the X atom induced by the nuclear magnetic moment in case of J-coupling are propagated similarly by spin-polarization mechanisms, governed by exchange interactions, to generate a spin density at the position of the spectator LA. The schematic representation of the propagation of spin polarization from the HA to the LA via one, two, and three chemical bonds as governed by the Pauli principle and Hund's rule is shown in **Figure 16a**. The SOM-ISD distributions in iodobenzene²⁶ and in PhHgH highlight the local predominance of α (blue) or β (red) induced spin density and its alternation throughout the conjugated system, resulting in alternation of the sign of $\delta^{\text{SO}}_{\text{LA}}$ for different atoms, see **Figure 16b**.

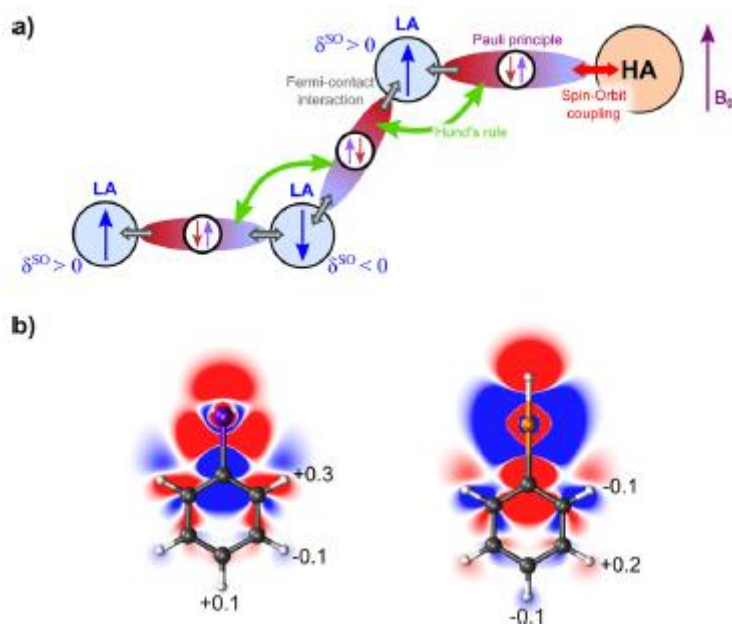


Figure 16. (a) Schematic representation of the propagation of spin polarization from the HA to the LA via one, two, and three bonds using the Dirac vector model, which is also commonly used to rationalize the alternation of the sign of indirect spin—spin coupling constants. (b) DFT-calculated distribution of SOM-ISD in PhI²⁶ (left) and PhHg¹¹H¹³⁰ (right). The spatial predominance of a and p SOM-ISD is shown in blue and red, respectively. The data were obtained using methods specified in **section 6.1** (method 1), **section 6.3**, and **section 6.4**.

We note in passing that a similar analogy applies to the pathways of spin-density propagation in the context of hyperfine couplings.^{21,125,126} This has led to the definition of new 3D quantities termed “coupling electron deformation density”^{127,128} and “hyperfine structure deformation density”.¹²⁹ Further examples of long-range SO-HALA effects are given in **Section 4**.

In analogy to the Fermi-contact mechanism of indirect nuclear spin-spin coupling, the Fermi-contact mechanism of SO-HALA shifts is governed by the electronic structure on the interaction path between the HA and the spectator LA. Thus, the Karplus-like torsion dependence of three-bond δ^{SO}_{LA} effects has also been rationalized by its analogy to nuclear spin-spin coupling pathways.²⁶ An example of the conformational dependence of $\delta^{SO}(^1H)$ for a “three-bond” interaction in Te=CH-CH₃ is shown in **Figure 17**. More examples are provided in **section 4**.

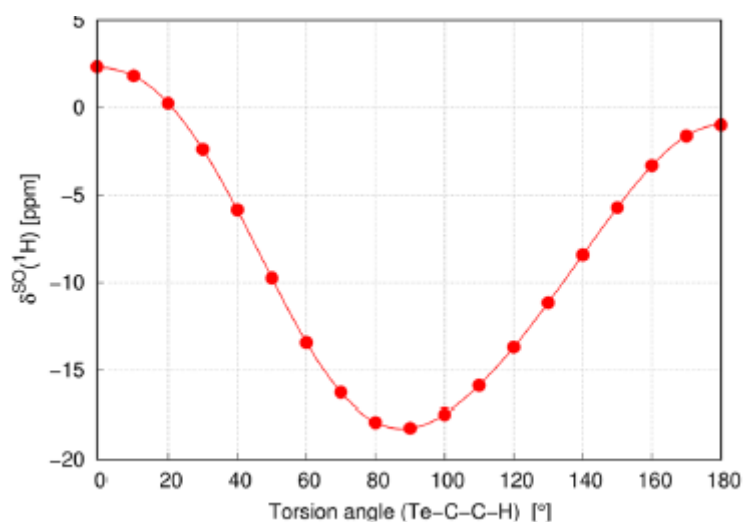


Figure 17. Karplus-like dependence of three-bond $\delta^{\text{SO}}(^1\text{H})$ in $\text{Te}=\text{CH}-\text{CH}_3$ on the rotation of the central C—C bond. The data were obtained using methods specified in **section 6.1** (method 1) and **section 6.3**.

3.1.5. "Through-Space" Supramolecular Effects

The propagation of the spin density induced during the above-mentioned SO step (**section 3.1.1**) toward the LA can also occur in various supramolecular interactions such as hydrogen, halogen, or chalcogen bonding. Note that this requires an uninterrupted pathway of sufficiently large electron density between the HA and the LA that can be polarized. In principle, this can be observed for various supramolecular bonding, nonbonding, and antibonding situations. However, the most efficient currently known examples of this effect are those exhibiting supramolecular covalency (orbital interaction and $\text{HA} \leftrightarrow \text{LA}$ electron sharing),¹³¹ which can also make a significant contribution to the total binding energy. As an example of this phenomenon, we plot (i) $\delta^{\text{SO}}_{\text{LA}}$ (ii) the change in the NMR shift, calculated at the SR level, induced by the formation of a supramolecular bond ($\Delta\delta^{\text{SR/SB}}_{\text{LA}}$), and (iii) the SOM-ISD map in **Figure 18** for a) the hydrogen-bonded (HB) ion-pair complex $\text{NH}_4^+ \cdots \text{I}^-$ and b) the halogen-bonded (XB) complex $\text{NH}_3 \cdots \text{IF}$. We note that in the first case, the SO-HALA effects reduce the overall (positive) complexation shift somewhat, whereas in the second case, the (negative) complexation shift is enhanced by the SO contributions.

3.2. Unifying the Chemical Concepts

3.2.1. PT2 Analysis Based on Molecular Spinor Pairs

A PT2 analysis of SO-HALA effects based on molecular spinors calculated at the two-component (or four-component) level is analogous to the standard NR or SR analysis of paramagnetic contributions to the NMR shift within the Ramsey formalism, except that in the presence of SO coupling the perturbation operators for the nuclear magnetic moment include the FC and SD hyperfine contributions that underlie the SO-HALA effect (see **section 2**).

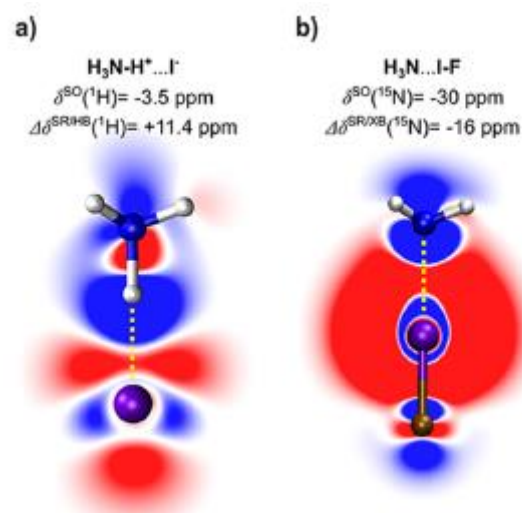


Figure 18. (a) $\delta^{\text{SO}}(^1\text{H})$, $\Delta\delta^{\text{SR/HB}}(^1\text{H})$, and a plot of the SOM-ISD for the hydrogen-bonded complex between NH_4^+ and I^- (for the H atom involved in en bond). (b) $\delta^{\text{SO}}(^{15}\text{N})$, $\Delta\delta^{\text{SR/XB}}(^{15}\text{N})$, and a plot of the SOM-ISD for the halogen-bonded complex between NH_3 and IF . The predominance of α and β induced spin density is shown in blue and red, respectively. The data were obtained using methods specified in **section 6.1** (method 1), **Section 6.3**, and **section 6.4**.

The analysis for diamagnetic (closed-shell) systems is typically done using molecular spinor pairs (MSPs), also known as Kramers pairs. This allows an $\text{MSP} \leftrightarrow \text{MSP}^*$ coupling analysis while accounting for SO effects and provides differences from the analogous SR (or NR) values for the relevant $\text{MO} \leftrightarrow \text{MO}^*$ couplings.

A comparison between the MOs (NR or SR level) and MSPs (2c or 4c level) can be used to estimate the role of mixing MOs of different symmetry by SO coupling for the magnetic response of the system. This mixing in turn can be obtained from the nonrelativistic MOs using first-order perturbation theory (PT1), as demonstrated in **Figure 2**. As an example, we show the SO-induced mixing of occupied σ -bonding and nonbonding (η_{HA}) MOs at the HA for AuH in **Figure 19a**. The resulting MSP (HOMO-3) of mixed σ and π character dominates ($\sum\delta^{\text{SO}} = -16$ ppm) the enhancement of the paramagnetic ^1H NMR shielding by SO coupling (reflected in the $\delta^{\text{SO}}_{\text{tot}} = -13$ ppm relative to the SR data). The efficient and most significant magnetic coupling of the HOMO-3 with the LUMO ($\delta^{\text{SO}} = -14$ ppm) is shown schematically in **Figure 19a**. In contrast to AuH, the SO-induced mixing of vacant (η_{HA}^*) MOs at the HA in TIH results in an extremely efficient deshielding HOMO \leftrightarrow LUMO magnetic coupling ($\delta^{\text{SO}} = +107$ ppm),¹³² which dominates the total SO-HALA shift ($\delta^{\text{SO}} = +122$ ppm), **Figure 19b**.

The advantage of the PT2 analysis is that SO effects are included variationally and thus more accurately and completely. A disadvantage is that the MSPs are complex quantities (see **Figure 2**) that are difficult to visualize and interpret completely, see **section 2**. One needs to transform the data in order to visualize them. For example, within the two-component ZORA implementation in the ADF code,^{133,134} only one real function is typically displayed (**Figure 19**) instead of the required two complex functions. This has been used previously to interpret the roles played by the electronic structure around the metal atom¹¹⁴ and the TLI^{99,119} on the SO-HALA shifts in various transition-metal complexes. To relate the

MSPs to the NR MOs and thus obtain further insight, one would have to apply PT1 to the MSPs (**Figure 2** and **section 2**) and thus to sacrifice the higher accuracy of the two- or four-component treatment.

Figure 19. SO-induced (a) mixing of the occupied σ -bonding (HOMO and HOMO-5) and nonbonding (η_{HA} , HOMO-3, HOMO-4) SRMOs for AuH, and an example of the $\text{MSP} \leftrightarrow \text{MSP}^*$ coupling of the resulting HOMO-3 MSP with a LUMO MSP having significant LA s-character, and (b) mixing of two vacant η_{HA}^* MOs (LUMOs) and the occupied c-bonding HOMO for TIH, and an example of the $\text{MSP}^* \wedge \text{MSP}$ coupling of the resulting LUMO MSP with an HOMO MSP having significant LA s-character. The contributions to are shown for the individual MSPs. The data were obtained using methods specified in **section 6.1**

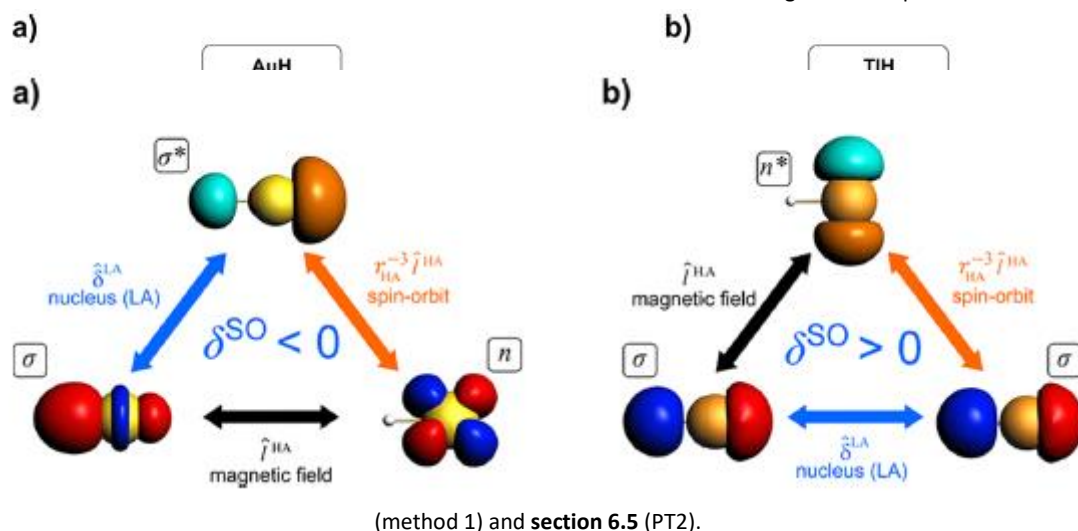


Figure 20. Schematic graphical representation of the SO/FC mechanism involving two occupied MOs (see also **eq 18** and **Figure 4**).⁹⁹ (a) The shielding SO contribution that dominates the negative $\delta^{\text{SO}}(^1\text{H})$ in AuH, and (b) the deshielding SO contribution that dominates the positive $\delta^{\text{SO}}(^1\text{H})$ in TIH. The occupied MO in TIH can be viewed as a superposition of two MOs, antibonding s(TI)-s(H) and bonding p(TI)-s(H). Because s functions of the TI atom have no effect on magnetic and SO coupling integrals, this occupied MO is considered as a σ -bonding orbital in the PT3 analysis. The data were obtained using the method specified in **section 6.5**.

Moreover, the mechanism and sign of the SO-HALA shift are not fully transparent in **Figure 19**. To understand the sign and mechanism of the SO-HALA effect in more detail, we must resort to the PT3-based analysis of $\delta^{\text{SO}}_{\text{LA}}$, which is elaborated in the following section.

3.2.2. Transparent PT3 Analysis Based on Nonrelativistic MOs

The PT3 scheme starts from nonrelativistic (NR) or scalar-relativistic (SR) MOs and adds SO coupling as another perturbation (**section 2**). It provides a particularly transparent and fine-grained interpretation in terms of standard nonrelativistic MOs, decoding their role in the magnetic response of the system.

As described in detail in **section 2**, the three perturbations involved in the SO/FC mechanism are the SO-coupling, Fermi-contact, and angular-momentum operators. The mutual interplay of all three perturbations has been discussed thoroughly in **section 2** and is shown schematically in **Figure 20**, for examples of the triangular diagrams⁹⁹ that dominate the shielding and deshielding SO/FC contributions to $\delta^{\text{SO}}_{\text{LA}}$ in AuH and TIH, respectively. For the convenience of the reader, the interaction of an external magnetic field with the electronic orbital motion, given by the angular-momentum operator \hat{L} , is color-coded in black. The perturbation caused by the nuclear magnetic moment of the spectator atom LA

via the Fermi-contact (FC) interaction is coded in blue, and the SO coupling originating at the HA is coded in orange.

In the PT3 scheme, the SO/FC mechanism involving two occupied MOs and one vacant MO for the SO/FC^Δ term (within the reasonable approximations discussed in **section 2**) results in a shielding SO contribution ($\delta^{\text{SO}} < 0$, **Figure 20a**) unless both occupied MOs are of $\sigma(\text{HA-LA})$ -bonding character, which changes the overall sign ($\delta^{\text{SO}} > 0$, **Figure 20b**).⁹⁹ The two examples shown in **Figure 20** are directly related to the PT2 analysis of AuH and TiH shown in **Figure 19**.

Given the PT3 examples in **Figure 20**, we now proceed to analyze the sign of the SO-HALA contribution to the NMR shift, as it relates to the electronic structure of the HA, which is crucially important to understanding the periodic trends discussed in **section 4**.¹⁰⁰ As discussed in **section 2**, the leading $\text{MO} \leftrightarrow \text{MO}$ couplings must arise from the frontier MOs, i.e., high-lying occupied and low-lying vacant MOs.

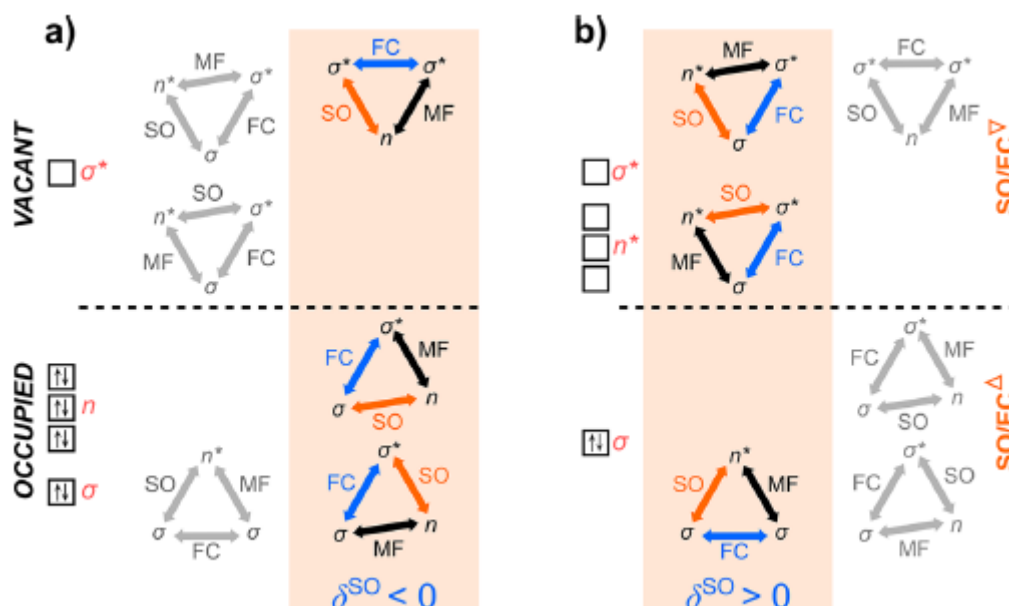


Figure 21. Schematic representation of two limiting electronic configurations at the HA with (a) occupied (n , left) and (b) vacant (n^* , right) HA-based nonbonding orbitals.¹⁰⁰ The sign of $\delta_{\text{LA}}^{\text{SO/FC}}$ is governed by the availability of occupied/vacant HA-based orbitals of suitable energy as shown by the MO coupling triangles for the SO/FC Δ (bottom) and SO/FC ∇ (top) mechanisms.⁹⁹ Triangles shown in gray are not accessible for a given electronic configuration. Note that MF stands for the interaction of an external magnetic field (B_0) with the electronic orbital motion given by the angular-momentum operator \hat{L} (see **section 2**), and σ^* in the text stands for a and σ^* , which are both present in all of the triangles due to the role of the FC operator (shown in blue).

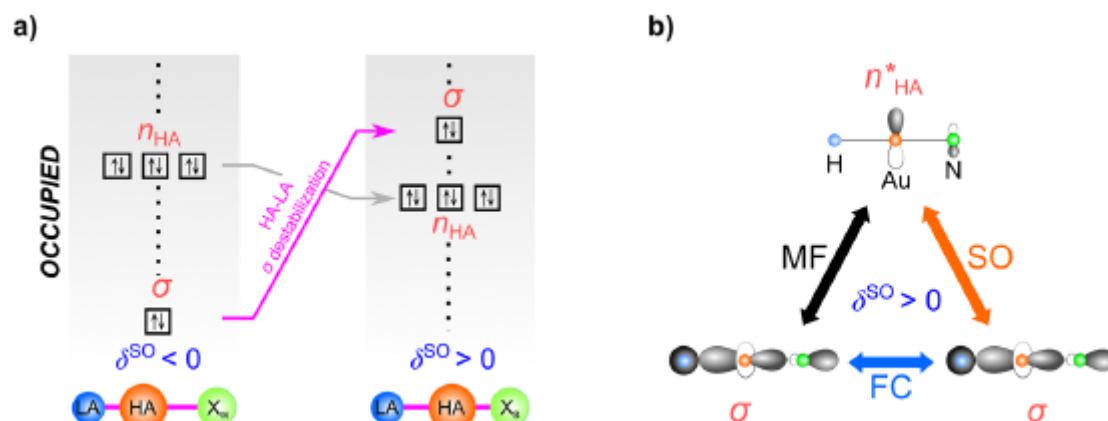


Figure 22. (a) Structural and electronic trans-ligand influence of a weak X_w like F or a strong X_s , like CH_3 on the relative energy of the $\sigma_{\text{HA-LA}}$ MO entering the coupling triangles and affecting the SO-HALA shift as discussed above.^{99,119} (b) The PT3 coupling triangle governing $\delta^{\text{SO}}_{\text{LA}}(^1\text{H}) > 0$ in HAuNH_3 for a short Au-N distance (strong X), which highlights the role of 2p AOs of the trans nitrogen atom (shown in green), cf. **Figure 14**. MF stands for the interaction of an external magnetic field (B_0) with the electronic orbital motion, given by the angular-momentum operator \hat{I} (see **section 2**). The data were obtained using the method specified in **section 6.5**.

Furthermore, the electronic structure around the HA can be analyzed in terms of MOs with significant coefficients from AOs on the HA (AO_{HA}). These AO_{HA} s are represented by nonbonding orbitals at the HA (n_{HA} , or lone electron pair - LP), $\pi_{\text{HA-LA}}$ and $\delta_{\text{HA-LA}}$ bond types, and $\sigma_{\text{HA-L}}$ with another ligand (L). For the sake of simplicity, let us consider the simplest HA-H example with only a $\sigma(\text{HA-H})$ bond and with nonbonding orbitals at the HA (e.g., AuH). Four types of frontier orbitals then play roles in the SO-HALA mechanism: nonbonding orbitals at the HA, including both occupied (n_{HA}) and vacant (n^*_{HA}) MOs, and occupied HA-LA bonding ($\sigma_{\text{HA-LA}}$) and vacant antibonding ($\sigma^*_{\text{HA-LA}}$) MOs. We denote them for simplicity as n , n^* , σ , and σ^* .

The two limiting cases of electronic configurations at the HA are shown in **Figure 21**. A representative electronic configuration with an available occupied nonbonding orbital n at the HA (n_{HA}) but without n^*_{HA} is shown in **Figure 21a**, whereas one without n_{HA} but with an available vacant nonbonding orbital n^*_{HA} is shown in **Figure 21b**. The presence of filled nonbonding MOs in the valence shell of the HA (**Figure 21a**) causes the active shielding contributions ($\delta^{\text{SO}}_{\text{LA}} < 0$) described as $n_{\text{HA}} \leftrightarrow \sigma^*_{\text{HA-LA}}$ in the SO/FC mechanism (examples are transition-metal complexes with d^2 - d^8 configurations and halogen compounds, **section 4**). Note that $\sigma^{(*)}$ in the text stands for σ and σ^* , which are both present in all of the triangles due to the role of the FC operator. In the absence of occupied nonbonding MOs, only deshielding contributions ($\delta^{\text{SO}}_{\text{LA}} > 0$) labeled $\sigma^*_{\text{HA-LA}} \leftrightarrow n^*_{\text{HA}}$ in **Figure 21b** are nonzero, as found, for example, for p^0 , d^0 , and f^0 configurations at the HA in the molecule (not necessarily the atomic ground state of the HA).¹⁰⁰

In general, both the SO deshielding and shielding contributions may be active simultaneously, with the total $\delta^{\text{SO}}_{\text{LA}}$ value governed by the energy separations between the relevant frontier MOs and the coupling MO matrix elements.⁹⁹ Excellent examples representing a delicate balance between two contributions of opposite sign are d^{10} systems (e.g., Au(I) complexes),^{99,119} where the properties of the ligand trans to the LA can modulate or even invert the overall sign of $\delta^{\text{SO}}_{\text{LA}}$, see **Figure 15**. For weak

trans-ligands (X_w) in a linear LA-HA-X complex of gold(I), the HA-LA bond is relatively strong; and the corresponding MO of $\sigma_{\text{HA-LA}}$ character is energetically stabilized and thus plays a marginal role in the SO-HALA mechanism. In this case, the SO-HALA shift is governed by many small shielding SO contributions (negative $\delta_{\text{LA}}^{\text{SO}}$) originating in $n_{\text{HA}} \leftrightarrow \sigma_{\text{HA-LA}}^{(*)}$ type (HA-based $5d \leftrightarrow 5d^*$) couplings. A strong trans-ligand (X_s , covalent HA—X bond) destabilizes the HA—LA bond by a structural and electronic trans-ligand influence (TLI), and the energy of the corresponding $\sigma_{\text{HA-LA}}$ orbital is increased, **Figure 22a**. It therefore contributes significantly, and it typically governs the SO deshielding (positive $\delta_{\text{LA}}^{\text{SO}}$).

The PT3 mechanism of this SO-HALA deshielding particularly highlights the role of the trans ligand as shown for HAuNH_3 in **Figure 22b**. The SO (and angular-momentum) operator couples the occupied and vacant MOs with the following AO contributions: $2p^{\sigma}\text{N} \leftrightarrow 2p^{\pi}\text{N}$, $2p^{\sigma}\text{N} \leftrightarrow 6p^{\pi}_{\text{Au}}$ and $5d^{\sigma}_{\text{Au}} \leftrightarrow 2p^{\pi}\text{N}$, all involving the trans-nitrogen atom and contributing to the SO deshielding. The SO-and-magnetically induced electron-spin density interacts with the magnetic moment of the LA nucleus via the FC operator, acting on occupied MOs with s-character at the hydrogen (LA) atom. Induction and propagation of spin density thus involve AOs of the trans atom X, particularly for strong TLs (**Figure 15**) and short HA-TL distances (**Figure 14**).

The trans-ligand influence shown in **Figure 22b** is a good example of an arrangement where one of the assumptions we used to derive the rules for the sign of the SO-HALA effect (**Figure 5**) does not hold. Specifically, the MO \leftrightarrow MO couplings between the occupied and vacant HA AOs vanish, and the SO ($r_{\text{HA}}^3 r_{\text{HA}}^{\text{HA}}$) and MF (\hat{I}) coupling is dominated by the interatomic contributions. Here, the FC coupling (the occupied MOs are identical) and the product of SO and MF coupling (equal signs) are both positive. The final SO-HALA deshielding (positive $\delta_{\text{SO}}^{\text{LA}}$) is then given by the negative sign in **eq 18**.

The theoretical foundations of the SO-HALA shift summarized in **section 2** and demonstrated in this section on selected examples in terms of chemical concepts allow for a more complete understanding of previously observed trends across the Periodic Table of the Elements (PTE)¹⁰⁰ than had hitherto been possible. In section 4 we will focus on these general trends and selected examples from the time period 2004—2019 to illustrate the usefulness of these concepts and to reveal the broad importance of such effects throughout the Periodic Table.

4. TRENDS IN SO-HALA SHIFTS ACROSS THE PERIODIC TABLE

As shown in **sections 2** and **3**, SO-HALA NMR effects are connected to the electronic structure of the neighboring heavy atom (HA) and its ligand sphere.^{99,100,119} With few exceptions, trends in SO-HALA effects have been investigated using relatively small groups of HA compounds. Recent efforts to understand the phenomenon on a wider scale encompass three large studies^{99,100,119} that have revealed in detail how the sign of the SO-HALA shift relates to the electronic structure at the HA and how the position of the HA within the PTE, its oxidation state, and its bonding environment (e.g., the TLI in transition-metal complexes), influence the sign and magnitude of δ_{SO} . The link between the electron configuration of the HA and the SO-HALA shift was generalized when the triangular PT3 concept⁹⁹ was applied systematically to compounds of the sixth-row to determine whether or not the SO-HALA effect shows periodic trends. A large set of ^1H NMR shifts for compounds containing HAs of the sixth period, ranging from CsI to AtI, has been analyzed, with periodic trends in the sign of $\delta_{\text{SO}}(^1\text{H})$ revealed and rationalized.¹⁰⁰ Most importantly, it has been shown that the sign of $\delta_{\text{SO}}(\text{LA})$ correlates systematically with the presence of occupied/vacant nonbonding orbitals centered at the HA (this is valid also for heavier atoms such as ^{13}C and ^{15}N), as will be discussed in detail in this section. Note that throughout **section 4** we will use the notation LA for light atoms and also for heavier spectator NMR

atoms (e.g., Se or Te) in the vicinity of an even heavier HA. Based on refs 51, 91, 95, 97, 99, 100, 111, 113, 115, 119, and 132–138, the following general rules can be derived for periodic trends in the SO-HALA shifts:

1. A formally empty valence shell at the HA (p^0 , d^0 , or f^0 configuration) gives rise to SO-HALA deshielding of LA(s) bonded directly. This is the case particularly for HAs with $5d^0$ and a positive oxidation state Cs^I–Os^{VIII}, for $6p^0$ Hg^{II}–Bi^{III} (the $6s^2$ shell is present but unimportant in this context), and for $6d^05f^0$ Ac^{III}–U^{VI}.^{51,100,132,137,138} For the corresponding lighter analogs, the effect exists in diminished form (**Figure 23**). (Note that the electronic state relates to the HA bonded in a molecule not its atomic ground state.) In such cases, the SO-HALA deshielding is dominated by the $\sigma^*_{\text{HA-LA}} \leftrightarrow \sigma_{\text{n}^*_{\text{AH}}}$ coupling mechanism (**Figures 5** and **21b**), which requires the presence of a low-lying vacant orbital(s) at HA.^{100,132}
2. Partially filled, energetically high-lying valence subshells (d^2 – d^8 , p^2 – p^4) at the HA induce SO-HALA shielding at the LA, particularly in $5d^{2n}$ (Hf^{II}–Au^{III}) or $6p^{2n}$ (Bi^I–At^I) compounds and, in diminished form, for their corresponding lighter analogs (**Figure 23**).^{51,95,100} The SO-HALA shielding is dominated by the $n_{\text{HA}} \leftrightarrow \sigma^*_{\text{HA-LA}}$ coupling mechanism (**Figures 5** and **21a**) and requires the presence of one or more nonbonding (n_{HA} , or lone electron pair, LP_{HA}) orbitals at the HA. This effect is to a certain extent additive when more than one suitable nonbonding MO is present, for example, along the $5d^2$ through $5d^4$ to $5d^6$ and $6p^2$ to $6p^4$ series of hydride complexes.^{51,95,100,132} A considerably smaller shielding effect is observed when the HA AOs are not LPs but are involved in bonding interactions to ligands other than the LA or the trans ligand (see rule 4), for example, in $\sigma_{\text{HA-L}}$ bonds.¹⁰⁰
3. The oxidation state of the HA is related directly to the occupation of n_{HA} and thus determines $\delta^{\text{SO}}(\text{LA})$, according to rules 1 and 2 above.^{99,100,132} For instance, an LA in a $5d^2$ complex of W^{IV} experiences SO-HALA shielding, i.e., a negative $\delta^{\text{SO}}(\text{LA})$, while SO-HALA deshielding, i.e., positive $\delta^{\text{SO}}(\text{LA})$, would be expected in a $5d^0$ W^{VI} complex.¹⁰⁰ In most cases, the above-mentioned mechanisms act simultaneously, and one usually dominates the other. Sometimes, for example in Bi^{III} ($6p^0$) and Au^I ($5d^{10}$) systems, these two mechanisms are so similar in magnitude that the sign of the SO NMR shift can be dictated by other factors, or the SO-HALA effect can be vanishingly small (see rule 4).
4. Additional factors, such as the trans-ligand influence,^{99,109,115,118,119} (TLI, **section 3.1.3**) and a recently described cis-ligand influence¹²⁰ further modulate the δ^{SO} . The TLI influences the relative energies and compositions of frontier $\sigma^{(*)}_{\text{ha-la}}$ orbitals, thereby affecting the SO-HALA mechanism.

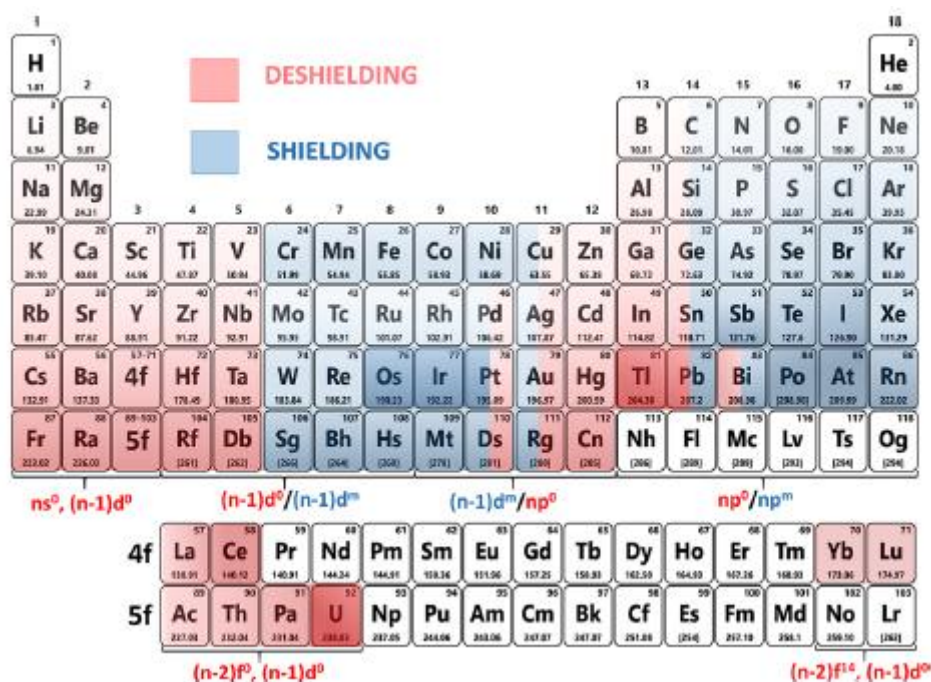


Figure 23. General trends in SO-HALA NMR shifts across the Periodic Table. Red shows SO-HALA deshielding ($\delta^{\text{SO}} > 0$) and blue SO-HALA shielding ($\delta^{\text{SO}} < 0$) for a given HA in its typical oxidation state(s). The relative magnitude of the SO-HALA effect is represented by lighter (less) and darker (more) shading. HAs for which SO-HALA effects have not yet been evaluated or for which closed-shell complexes are unknown, are indicated by a white background. The color-coded configurations presented beneath the 7th period and beneath actinides indicate which of the elements in the groups above can occur in $(n-2)f^0/(n-1)d^0/np^0$ configurations (n is principal quantum number), which may lead to deshielding SO-HALA effects caused by vacant valence p -, d -, or f -orbitals, and which of the more electron-rich situations tend to be more shielded (d^m/p^m configurations, index m represents even-numbered electron configuration).

Strong trans ligands may even invert the sign of δ^{SO} , particularly in d^8 and d^{10} complexes, see below.^{99,115,119} The effects of cis and/or other than trans ligands are typically smaller than the TLI but should be considered, e.g., for Bi^{III} ($6p^0$) and Au^{I} ($5d^{10}$) complexes (see below).

- The vertical trends for HAs of the s - and p -blocks follow the expected dependence of relativistic effects on Z_{HA} (the atomic number of the HA nucleus).⁵⁶ The trend is analogous to the well-known normal halogen dependence (NHD, i.e., the SO shielding increases going down the given group for the HA, **section 1**) observed for groups 14–18, whereas the opposite behavior (growing SO deshielding going down the group) is observed for compounds with HAs of s -block^{100,139} and group 13.⁵¹ The latter trend is analogous to inverse halogen dependence (IHD, **section 1**)⁴² but its origin is different (the SO-HALA effect instead of scalar paramagnetic shielding). For HAs with partially filled d -shells, particularly for octahedral d^6 and square-planar d^8 complexes, the SO-HALA effects generally follow an inverted V-shape trend,^{113,138,140} resulting from competition between the growing SO splittings and the likewise growing energy denominators down the PTE (explained in **section 3** and **Figure 11**).

For convenience, we have collected the available occurrences of typical SO-HALA (de)shielding from the studies reviewed here and presented them schematically throughout the Periodic Table (**Figure 23**). Red and blue are used to show SO-HALA deshielding and shielding effects, respectively, in compounds of a given HA in its typical (closed shell) oxidation state(s). The color-coded description of

electronic configurations located beneath the seventh period has been added to further emphasize the elements which can, at least hypothetically, be found in an $ns^0(n-1)d^0$ or np^0 configuration. In that case, vacant valence p or d-orbitals lead to deshielding SO-HALA effects, while the more electron-rich configurations at the HA feature partially occupied orbitals and thus make shielding SO contributions. For instance, deshielding SO-HALA effects are expected in W^{VI} complexes with a $6s^05d^0$ configuration, whereas SO-HALA shielding is expected in W^{II} ($5d^2$) and W^{III} ($5d^4$) complexes, increasingly so for the latter. The same applies for the majority of early transition-metal complexes. Similarly, transition-metal configurations for which the SO-HALA effects are influenced considerably by the availability of np orbitals^{99,114,119} are denoted $(n-1)d^m, np^0$. Here dm corresponds to an even-numbered d-configuration, i.e., d^6, d^8 , or d^{10} . The influence of a TLI (see **sections 2 and 3**), which can switch the sign of the SO-HALA effect for some HAs, is emphasized by both red and blue stripes for the given element (see, e.g., Pt and Au). The red and blue stripes in group 14 and Bi emphasize the possible large deshielding SO-HALA effects in HA^{II} when the HA is a group 14 element and in Bi^{III} complexes (compared to shielding for higher oxidation states, HA^{IV} and Bi^V).^{91,132} Exceptions to these elaborated general trends may occur in specific cases (e.g., exotic oxidation states, involvement of the atom in a cluster, strong TLI).

More detailed descriptions of the known SO-HALA trends in s-, d-, p-, and f-block compounds are given in **sections 4.1–4.5** below, together with an overview of the individual works dealing with calculating and predicting SO and (where available) SR contributions to LA NMR shifts in heavy-element compounds. As outlined in **section 1**, SR effects have not been investigated extensively, and only a few general concepts have been derived for them, although some basic observations are outlined in the text. Schematic illustrations of the known ranges of SO-HALA shifts for complexes of a given element (group), collected from the works covered in this comprehensive review, are presented at the beginning of each subsection. These are accompanied by examples of applications of SO-HALA effects in the elucidation of molecular and electronic structure and chemical reactivity.

4.1. HAs of the s-Block

4.1.1. General Aspects

SO-HALA effects of HAs of the s-block have scarcely been investigated, likely because the ns valence orbitals themselves do not contribute to SO effects. However, low-lying $(n-1)d$ orbitals of the heavy alkaline earth elements (Ca, Sr, Ba, and Ra) participate in their chemical bonding, making them “honorary d-elements”.¹⁴¹ As a result, the low-lying $(n-1)d$ HA orbitals contribute to the SO-HALA mechanism in a way similar to that for genuine d^0 systems (as well as for the lanthanides), particularly to the $\sigma_{HA-LA}^* \leftrightarrow n_{HA}^*$ deshielding (**Figure 23**).¹⁰⁰ An example of such deshielding orbital magnetic coupling (OMC) involving contributions from $5d$ and $5d^*$ orbitals in BaH_2 is illustrated in **Figure 24**.¹⁰⁰

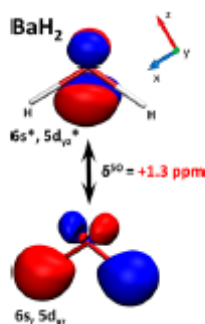


Figure 24. Example of the $5d-5d^* \sigma_{\text{HA-LA}}^* \leftrightarrow n_{\text{HA}}^*$ deshielding orbital magnetic coupling in $5d^06s^0 \text{Ba}^{\text{II}}\text{H}_2$, adapted from ref ¹⁰⁰. Copyright 2018 American Chemical Society.

Because of the d^0 character, weakly deshielding SO-HALA effects are found in heavier, formally ns^0 complexes. The range of currently known $\delta^{\text{SO}}(^1\text{H})$ values¹⁰⁰ for hydrides of these elements is shown in **Figure 25**.

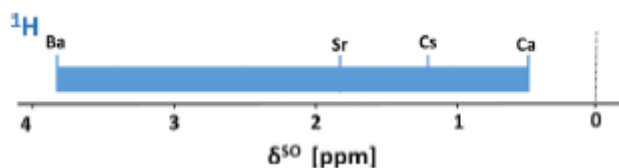


Figure 25. Range of computed ^1H SO-HALA shifts in s-block hydride complexes (LA bonded directly to the HA).¹⁰⁰

We note in passing that alkali anions from Na^- through Cs^- with the electronic configuration ns^2 at the HA have been observed experimentally, including NMR measurements,¹⁴² but no data regarding SO-HALA effects or LA NMR shifts have been reported. We speculate that the SO-HALA effects in such compounds are in any case small, because of the strongly ionic nature of alkali bonding.

4.1.2. Groups 1 and 2: Alkali and Alkaline-Earth Metals

Computational analysis of ^1H NMR shifts in gas-phase s-block hydrides¹⁰⁰ has shown that in group 2 hydrides the SO-HALA effect increases by about 4 ppm from CaH_2 to BaH_2 ,¹⁰⁰ see **Figure 25**. This correlates well with experimental ^1H NMR shifts in the solid-state hydrides, which increase by 4.2 ppm, from 4.5 ppm (CaH_2) to 8.7 ppm (BaH_2).¹⁴³ While earlier attempts to explain this trend using classical arguments, such as the electronegativity of the alkaline earth metal, were not convincing, the SO-HALA effect provides a natural explanation for the observations.

Relativistic deshielding of ^1H NMR resonances can also be found in relatively complex materials. For instance, the hydride signals in hydride-doped strontium mayenite have been found experimentally at Stot up to +6 ppm, a region that is usually associated with the ^1H NMR resonances of OH groups.¹⁴⁴ These results could not be reproduced using scalar relativistic calculations, although the inclusion of scalar-relativistic corrections slightly improved the agreement with experiment.¹⁴⁴ Clearly, the inclusion of SO-HALA effects in the calculations is necessary to reproduce the ^1H NMR spectra of hydride-doped materials of the heavier s-block metals.

Relativistic effects were also calculated for ^{19}F NMR shifts in solid-state Li, Na, Ca, Rb, Sr, Cs, and Ba fluorides.¹³⁹ The reported $\delta^{\text{SO}}(^{19}\text{F})$ values were between -3 ppm (CaF_2) and $+2$ ppm (CsF). The relatively small SO-contributions are likely due to the high polarity and particularly to the low s-character of the fluorine in the M—F bond. That $\delta^{\text{SO}}(^{19}\text{F}) = -3$ ppm for CaF_2 may reflect the numerical uncertainties of

these calculations (differences between SO-ZORA and SR-ZORA data) is suggested in the original work.¹³⁹

4.2. HAs of the d-Block

4.2.1. General Aspects

Due to the high sensitivity of ^1H shifts to SO-HALA effects (efficient SO/FC mechanism, see **section 3**), and the ensuing spectacular ^1H shifts, relativistic contributions to the ^1H NMR shifts in transition-metal hydride complexes have been at the center of various computational analyses of SO-HALA effects.^{95,100,115,120,137,145} Indeed, many general SO-HALA trends in d-block systems have been derived primarily from hydride NMR shifts. While not as spectacular in magnitude, due to the larger “standard” NMR spectral ranges, similar trends are also found for other LAs, such as carbon and nitrogen, provided an efficient SO/FC mechanism is operative.^{96,99,100,109,114,119,130,146,147} Calculated ranges of the SO-HALA shift for ^1H , ^{13}C , and ^{15}N nuclei in transition-metal complexes are summarized in **Figure 26**. The data were collected from the works covered in **section 4.2**.

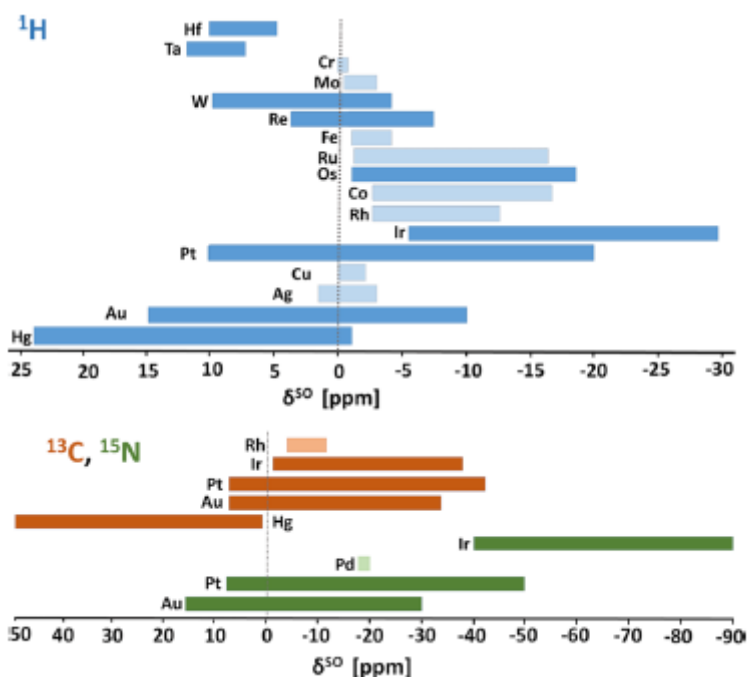


Figure 26. Ranges of the computed ^1H , ^{13}C , and ^{15}N SO-HALA shifts for individual d-block metal HAs (LA bonded directly to the HA). Note that lighter shades are used for ^3d and ^4d to highlight the trend in $\delta^{\text{SO}}(\text{LA})$ for compounds of ^5d elements.

In early transition-metal complexes with d^0 configuration, the deshielding $\sigma_{\text{HA-LA}}^* \leftrightarrow \text{n}_{\text{HA}}^*$ mha orbital coupling dominates the SO-HALA shifts. Hence, positive SO-HALA contributions are found in **Figure 26** for early transition-metal complexes featuring d^0 configurations (mainly from groups 3–8). As the d-shell becomes populated in d^2 , d^4 , d^6 , and d^8 systems, the shielding $\text{n}_{\text{HA}} \leftrightarrow \sigma_{\text{HA-LA}}^*$ coupling mechanism becomes dominant.¹⁰⁰ This trend, together with additional shielding due to the Buckingham-Stephens effect^{148,149} (shielding at the LA, caused by off-center paramagnetic ring currents from the incomplete valence shell of the HA and found particularly in hydride complexes), is responsible for the predominantly low-frequency ^1H NMR signals in d^2 to d^8 d-metal hydrides (**Figure 26**). A local extremum in $\delta^{\text{SO}}(^1\text{H})$ for d-block hydrides is observed for 5d^6 Ir complexes with a computed SSO of—

30 ppm (and even more negative overall shifts).^{95,100} We note that the lowest total ¹H NMR shift ever experimentally observed was -59.1 ppm in a 5d⁶ Irm porphyrin hydride complex.¹⁵⁰

Vacant HA 6p orbitals start to play an important role for SO-HALA effects in 5d⁸ complexes, see Pt and Au in **Figure 26**.¹¹⁴ These orbitals mix into the frontier MOs and thus participate in the deshielding $\sigma_{\text{HA-LA}}^* \leftrightarrow n_{\text{HA}}^*$ mechanism that reduces the overall SO-HALA shielding. The 6p-6p*-based $\sigma_{\text{HA-LA}} \leftrightarrow n_{\text{HA}}^*$ mechanism then typically dominates the SO-HALA effects in d¹⁰ compounds and beyond (particularly in group 12, see Hg in **Figure 26**) causing largely positive $\delta^{\text{SO}}(\text{LA})$ values.^{99,130,151} For borderline cases, such as 5d¹⁰ Au^I complexes, both mechanisms play similar roles and can be strongly modulated by the TLI (**section 3.1.3**).^{99,109,115,118,119} Hence the broad range of SO-HALA shifts in Pt and Au complexes shown in **Figure 26**.

Except for the d⁰ and d¹⁰ configurations, the vertical trends in the SO-HALA shift in the d-block tend to be characterized by an inverted V-shape dependence (**Figure 11**),^{95,113} although this can be affected by TLI when a strong trans ligand is present.^{99,119} The inverted V-shape reflects greater (shielding) SO-HALA contributions for the 3d and 5d compared to the 4d transition-metal complexes, due to the increase in ligand-field splitting with respect to 3d analogs and thus the relevant energy denominators for the 4d case (**section 3.1.1**). A detailed explanation of the V-trend can be found in the discussion of group 9 complexes below.

Before we discuss individual examples for d-block HA systems, it should be noted that a number of the computational studies of SO-HALA shifts in transition-metal complexes mentioned in the following discussion used a higher admixture of exact exchange in the DFT functional (typically 40%), to obtain better agreement with the experimental NMR shifts at the two-component SO-ZORA level, e.g., refs **104, 109, 114, 118, 137, 147, and 152**. However, the need for a higher exact-exchange admixture was later identified as an artifact caused by the absence of an exchange-correlation kernel in the SO-ZORA implementation used.^{96,97,153} Such a high exact-exchange admixtures should be avoided when using computational codes that treat the kernel properly.^{134,154}

4.2.2. Early Transition Metals

The SO-HALA effects in early transition-metal complexes have not been investigated as much as those of the late transition metals but a short overview of relativistic NMR effects in d⁰ complexes of early transition metals was contained in a recently published larger review.¹³⁸ Available data confirm that the SO-HALA effects for d⁰ complexes are uniformly deshielding, in contrast to the increasingly shielding contributions in d² and d⁴ systems.^{100,137,146,155}

An analysis of the relativistic ¹³C NMR shifts in early transition-metal complexes was used to elucidate the link between the NMR shifts and the electronic structure in d⁰ Schrock alkylidene metathesis catalysts based on Mo, Ta, W, and Re.¹⁵⁶ The high-frequency ¹³C signals in these complexes were attributed to the large paramagnetic contributions caused by the small energy separations between the $\sigma_{\text{M-C}}$ and $\pi_{\text{M-C}}$ orbitals. In addition, the orientations of some of the components of the ¹³C shielding tensor were found to be influenced by the angle between the metal atom and the =C-H fragment. These factors are very similar to those responsible for the modulation of SO-HALA effects, particularly the influence of energy denominators. Also, the relevant orbital couplings resemble those of the deshielding $\sigma_{\text{HA-LA}}^* \leftrightarrow n_{\text{HA}}^*$ mechanism, see **Figure 21b**.

4.2.3. Group 8: Ruthenium and Osmium

The hydride ^1H NMR shift in $4d^6$ Ru complexes with N-heterocyclic carbenes increases from -41 ppm to $+5$ ppm with increasing TLI (trans ligand: none, F^- , Cl^- , MeCN, N_2 , H_2 , H^- , P_4 , SO_2 , CO, and O_2).¹⁵⁷ A striking outlying value ($\delta(^1\text{H}) = +5$ ppm) has been experimentally observed for an Ru complex with an $\eta^2\text{-O}_2$ ligand in the trans position. Detailed analysis revealed strong n-type interactions between the O_2 2p and the Ru $5d_{xy}$ orbitals (HOMO) along with substantial destabilization of the Ru $5d_{yz}$ orbital. The Ru $5d_{yz}$ orbital, occupied in other complexes, becomes the LUMO in the O_2 complex. The original LUMO, which is in fact the σ^*_{RuH} MO, thus becomes less available for the shielding $n_{\text{Ru}} \leftrightarrow \sigma^*_{\text{Ru-H}}$ magnetic coupling, which diminishes the SO shielding mechanism (the SO contribution remains negative). Simultaneously, paramagnetic deshielding couplings between the Ru $5d_{xz}$ HOMO and the Ru $5d_{yz}$ LUMO further increase the total NMR shift at the hydrogen nuclei in question.

The SO-HALA shielding contribution to the ^{29}Si NMR signals of $-\text{SiX}_3$ groups ($\text{X} = \text{H}, \text{C}, \text{and Cl}$) in $4d^6$ Ru silyl complexes¹⁵⁸ was found to increase with the electronegativity of substituent X, with the maximum SO-HALA value of -35 ppm for $\text{X} = \text{Cl}$.¹⁵⁸ It has been suggested that this could be due to a smaller energy gap between the occupied and vacant MOs. However, an alternative explanation would be that the electronegative substituents increase the positive charge at Si and thus also the hybridization defects that increase the 3s-character of Si in the Si—M bond,⁴⁶ thereby enhancing the SO/FC mechanism of the SO-HALA effect (**section 3.1.1**).²⁶

A recent detailed study of the effect of TLI on the mechanism of ^1H SO-HALA shifts in a series of transition-metal complexes also included d^6 osmium(II) compounds.¹¹⁹ This study is discussed more thoroughly with groups 10 and 11 below.

4.2.4. Group 9: Cobalt, Rhodium, and Iridium

An experimental solid-state NMR study of ^1H shift tensors in $4d^6$ Rhm and $5d^6$ Irm hydride complexes¹⁵⁹ revealed that the unusual low-field isotropic shifts are accompanied by very large chemical shift anisotropies (CSAs), particularly for the Ir systems, confirming predictions based on large computed SO-HALA anisotropies.⁹⁵ These arise from the tensor components perpendicular to the M—H bond, increasing from Rh to Ir.¹⁵⁹

Four-component relativistic computations of the ^1H NMR shifts of iridium hydride, shifted to a lower frequency by SO-HALA effects, were used to elucidate the mechanism of the hydrosilylation of carbonyl compounds using Brookhart's iridium pincer complex.¹⁶⁰ A detailed comparison of the calculated ^1H NMR shifts of nine different hydride complexes with experimental ^1H NMR data revealed a fast equilibrium between a dihydride-silane Ir^{III} complex and a trihydride silyl Ir^{V} complex formed by oxidative addition of the silane.¹⁶⁰ Similar computational predictions of relativistic ^1H NMR shifts for hydride complexes and intermediates have been reported for Si-H activation across an Ru-S bond.¹⁶¹ These results could not be verified experimentally because of rapid decomposition reactions.

Two-component relativistic calculations of ^1H and ^{13}C NMR chemical shifts in d^8 Ir^{I} and Rh^{I} complexes¹⁴⁵ interacting with methane were performed to provide an insight into the mechanisms of activation of the C—H bond. δ^{SO} has been found to dominate the overall ^1H and ^{13}C NMR shifts, causing considerable shielding (overall shifts exceeding -40 ppm) of both types of nuclei. Only proper treatment of SO-HALA effects and consideration of long-range-corrected DFT functionals enabled identification of the correct structures of methane σ -complex intermediates, assignment of their signals in the NMR spectra, and explanations for the underlying reaction mechanism.¹⁴⁵

Solid-state NMR and relativistic DFT calculations of a hexa-iridium cluster¹⁶² provided explanations for unusually shielded ¹³C NMR resonances of bridging carbonyl ligands resonating at +191 ppm. Analyses showed that this is caused by a $\delta^{\text{SO}}(^{13}\text{C})$ for the bridging carbonyls (−27 ppm) much larger than that for the terminal ligands (−2 ppm). This is likely due to the bonding of the bridging carbon atom to two iridium centers.^{163,164} A higher covalency of the bridging Ir—CO bonds due to stronger back-bonding may also contribute via a more efficient SO/FC mechanism (**section 3.1.1**).^{109,114}

Systematic studies of three-bond SO-HALA effects in group 9 chelates have been carried out^{113,140} to understand experimental ¹H NMR titration results in a series of d⁶ Co, Rh, and Ir polyamine complexes. Upon deprotonation of the aqua, alcohol, or polyalcohol (carbohydride) coligands in these systems, one would have expected better charge donation by the anionic coligand (OH) generated upon deprotonation to enhance shielding of all CH₂ protons within the polyamine ligand. However, for certain methylene positions trans to the deprotonation site, substantial deshielding was observed. This can even lead to a nonmonotonous pH-dependence of the ¹H shift titration curves for multiple deprotonation sites. Computations at NR levels could not reproduce the observations, while inclusion of a PT3 treatment of SO-HALA effects provided the correct trends and insights.^{113,140} Interruption of SO/FC pathways from the metal center to the methylene proton site by the larger TLI of the deprotonated coligand combined with the antiperiplanar M—N—C—H arrangement in the protonated system enabling maximal SO/FC contributions (rationalized by a Karplus-type dependence, **section 3.1.4**) explained the differential SO-HALA effects causing the observed anomalous pH dependencies. Notably, smaller SO-HALA effects were found for the 4d⁶ Rh complexes compared to both the 3d⁶ Co and 5d⁶ Ir analogs, indicating for the first time the inverted V-shape dependence (**section 3.1.1**) of the SO-HALA effects down the group, due to the increased ligand-field splittings (energy denominators) partly counteracting larger SO coupling (cf. **eq 18** in **section 2**).⁹⁸ While the larger energy gap renders the SO-HALA effects smaller for the Rh compared to the Co system, the still much larger SO splitting explains the largest SO-HALA shifts for the Ir complex. This rationalization has been confirmed subsequently in other studies, e.g., for d8 metallasilatrane complexes,¹¹¹ and for d⁶—d¹⁰ transition metal hydrides.⁹⁵

A modulation of $\delta^{\text{SO}}(^{15}\text{N})$ of about 25 ppm caused by changing the metal trans-ligand distance was computed in an octahedral 5d⁶ Ir¹¹¹ complex.¹¹⁸ Notably, SR and NR contributions both changed by only 6 ppm in total. This initiated the first systematic study of the mechanisms of TLI in the SO-HALA effects. It was performed on a set of model d⁶ Ir complexes featuring different oxygen- and sulfur-based trans ligands,¹⁰⁹ and found a linear correlation of $\delta^{\text{SO}}(\text{LA})$ with the Ir 5d-character of the HA—LA bond (**section 3.1.1**). Essentially, covalently bound trans substituents tend to diminish the metal d-character in the HA—LA bond because they compete for the available metal d-orbitals. In contrast, substituents bound more ionically leave a larger fraction of the HA d-orbitals available for HA—LA bonding, thus increasing the metal d-character in the HA—LA bond. The analysis also provided a link between the SO/FC part of the SO-HALA shielding and the g- and A-tensors of EPR spectroscopy, which are known to be modulated by the metal d-character. The role of the metal d-character was later embedded into a more general relationship between covalency and the magnitude of the SO-HALA effects (**section 3.1.1**).¹¹⁴ This concept has been developed further by several studies of the TLI (see below).^{99,115,119,120}

4.2.5. Groups 10 and 11: Platinum, Gold

As discussed above, SO-HALA effects in platinum and, especially, gold complexes are strongly influenced by contributions from the frontier 6p-orbitals participating in the SO/FC mechanism and by TLI. Overall, the LAs are more shielded in Pt complexes than in Au systems, partly due to the predominance of d^8 Pt^{II} in the examples studied (a d^{10} configuration would require Pt⁰ complexes, which tend to be very reactive). However, even for d^{10} Au^I, a weak TLI can lead to shielding SO-HALA effects (see **Figure 26**).

Interest in computational studies of SO-HALA shifts in Pt and Au complexes peaked in 2011 with three independent works. One study used relativistic DFT methods to investigate SR and SO-HALA effects on the ligand atoms of 2-phenylpyridine ligands in related square-planar Pt and Au complexes.¹⁰⁴ Large SR effects on ¹³C and ¹⁵N NMR shifts (δ^{SR}) up to -28 ppm were calculated for the Au system, likely reflecting the well-known “gold maximum” of SR effects.⁵⁸ Relativistic contributions to the ¹³C and ¹⁵N NMR shifts in the Pt system were, in contrast, dominated by the SO-HALA effects. The much smaller ¹⁵N SO-HALA shift in the Au complex (near 0 ppm) compared to the Pt system (-18 ppm) was rationalized by the rather ionic (less covalent) character of the Au—N bonds (due in part to differences in the trans ligand, as was shown later¹¹⁴). Alternating signs of the long-range SO-HALA effects correlating with indirect spin—spin couplings have also been noted (cf. **Figure 16** in **section 3.1.4**).

The unusually shielded ²⁹Si resonances in certain metal-lasilatrane complexes¹⁶⁵ were interpreted in terms of SO-HALA shielding effects influenced by TLI when the trans-ligand was changed from Cl to I. A role for the Si—M bond covalency in the propagation of the SO-HALA was hinted at. The calculated values of $\delta^{SO}(\text{Si}) = -20, -17, \text{ and } -33$ ppm for Ni, Pd, and Pt complexes, respectively, follow the inverted V-shape dependence¹⁶⁵ (cf. **Figure 11** in **section 3.1.1**).

A third study in 2011 focused on the well-known high-field hydride ¹H NMR shifts in heavy transition-metal hydride complexes.⁹⁵ In the 1960s, the shielded hydride resonances had been attributed to off-center paramagnetic ring-current effects in the Buckingham-Stephens model.^{148,149} That model was confirmed by SR-DFT calculations in 1996.⁷⁷ The 2011 work showed that for the heaviest d^6 and d^8 systems, including Pt and Ir complexes, up to two-thirds of these spectacular high-field shifts can be due to SO-HALA effects. This was contrasted to the deshielding SO-HALA effects in d^{10} group 11 and 12 hydride complexes. This work also clearly confirmed the inverted V-shape dependence of SO-HALA shifts for the d^6 and d^8 cases.⁹⁵

Pt and Au complexes were also central to subsequent studies on the importance of the covalency of the HA-LA bond for SO-HALA effects and TLI.^{114,115} Reference¹¹⁴ correlated ¹³C and ¹⁵N SO-HALA shifts with the covalence of the HA-LA bond expressed by the delocalization index of QTAIM (DI; cf. **Figure 12**). This work further established the role of 6p-type HA orbitals (and the effect of decreasing 5d character in bonding) in SO-HALA deshielding contributions in Au complexes, an effect that becomes even more pronounced in group 12 systems. In the second study,¹¹⁵ the ¹H shifts in a series of square-planar $5d^8$ Pt hydride complexes $\text{trans-H-PtL}_2\text{X}$ (L = PMe_3 , X = trans ligand) were studied systematically as a function of the strength of the trans ligand. It was found that, while paramagnetic shieldings also contributed to the experimentally well-known larger shielding with weaker trans ligands, the SO-HALA contributions dominated the trend. While greater shielding also correlates with the Pt-H distances, closer analysis has established that both trends are consequences of the stronger trans ligands competing for the metal 5d orbitals with the hydride bond and thereby weakening it.¹¹⁵

Two independent computational studies from our groups in 2017 used complementary analytical tools to shed more light on the TLI for SO-HALA effects.^{99,119} While ref ¹¹⁹ relied on two-component spinors from ZORA computations and applied PT2 analyses, **ref 99** in addition to PT2 introduced PT3 analysis

of δ^{50} based on NR MOs to understand the electronic-structure origins of the SO-HALA trends (**section 2.3.3**). The systems studied in these two works overlapped to some extent, allowing a comparison of the insights gained from PT2 analysis based on MSPs (molecular spinor pairs, **section 2**) and PT3 analysis based on NR MOs. The generality of the TLI for SO-HALA effects for ^1H , ^{13}C , and ^{15}N shifts all the way from $5d^6$ Os^{II} and Pt^{IV} complexes via $5d^8$ Pt^{II} and Au^{III} systems to $5d^{10}$ Au^I and Hg^{II} compounds with a broad range of trans ligands was demonstrated in $5d^8$ Pt^{II} and d^{10} Au^I, the TLI may even change the sign of the SO-HALA contribution (and even the sign of the total ^1H hydride shifts) from shielding for weak trans ligands to deshielding for strong trans ligands.¹¹⁹ Interestingly, a comparison of linear d^{10} Cu, Ag, and Au complexes showed, that the V-shape dependence of SO-HALA shifts down the group for d^6 and d^8 systems extends to the d^{10} case for weak trans ligands but changes to a monotonous increase for strong trans ligands,¹¹⁹ due to enhanced SO-HALA deshielding contributions. Modulation of the sign of the SO-HALA contributions by the interplay of the metal center and the trans ligand has also been correlated with SO effects on the electron density (SO-EDD,⁹⁹ see **sections 2 and 3**).

A recent study of the interplay between cis- and trans-ligand effects on SO-HALA shifts in a series of square-planar d^8 Au^I hydride complexes explained the broad span of experimentally observed ^1H NMR signals from -8.5 ppm to +7 ppm.¹²⁰ The cis and trans ligands influence the $\delta^{50}(^1\text{H})$ in opposite way. That is, stronger ligands in the cis position stabilize the higher-lying $\sigma_{\text{Au-H}}$ bonding MOs and hence weaken the SO-HALA deshielding mechanism. The largest deshielding due to the cis ligand (up to +5 ppm) was therefore found for neutral weak σ -donors (S-, N-, and O-based ligands and CO). As in previous studies, the ^1H NMR shifts were found to correlate with the Au—H distance and the ionicity of the bond, which in turn correlated with trends in reactivity.

Combined DFT and experimental solid-state NMR investigations were performed for a diphosphacyclobutadiene cobaltate sandwich complex of Au^I.¹¹⁶ Inclusion of relativistic effects (both SR and SO-HALA effects) in the DFT computations was crucial for the correct assignment of the ^{31}P NMR resonances. For instance, the nonrelativistic ^{31}P NMR chemical shift of the Au^I-bound phosphorus atoms was -64 ppm (using an SR-ECP at gold), while the relativistic two-component SO-ZORA value was +23 ppm, indicating substantially deshielding SO-HALA effects. The need to revisit the ^{31}P NMR spectra assignments of similar compounds using relativistic DFT calculations was pointed out by the authors.

A sizable $\delta^{50}(^{14}\text{N})$, -45 ppm, was calculated at the $\text{N}\alpha$ atom of an azide ligand directly bound to Pt.¹⁶⁷ Significant SO-HALA shielding was also predicted for $\text{N}\beta$ (-21 ppm) and $\text{N}\gamma$ (-7 ppm) as a result of the high electron delocalization within the azide ligand. However, in spite of the large $\delta^{50}(^{14}\text{N})$, the $\text{N}\alpha$ and N nuclei have experimental NMR chemical shifts similar to those in free N—. Analysis showed that the SO-HALA shielding contributions at the $\text{N}\alpha$ and $\text{N}\beta$ nuclei partly compensate the paramagnetic deshielding contributions because electron density is withdrawn upon formation of the Pt— $\text{N}\alpha$ bond, including trans ligand effects. The authors suggested the term hidden heavy-atom effect when strong SO-HALA effects are present but are disguised in the spectrum by other contributions.

Probably the most dramatic example of a TLI for SO-HALA shifts can be found in a 2005 computational study,¹⁶⁸ where the unusually low $\delta(^{13}\text{C})$, 135.2 ppm, of a carbon atom trapped inside a phosphine-ligand-stabilized Au₆ cluster was investigated, see **Figure 27**. Signals of interstitial carbon atoms in “non- d^{10} ” transition-metal clusters tend to resonate at rather high frequencies, above +400 ppm.¹⁶⁸

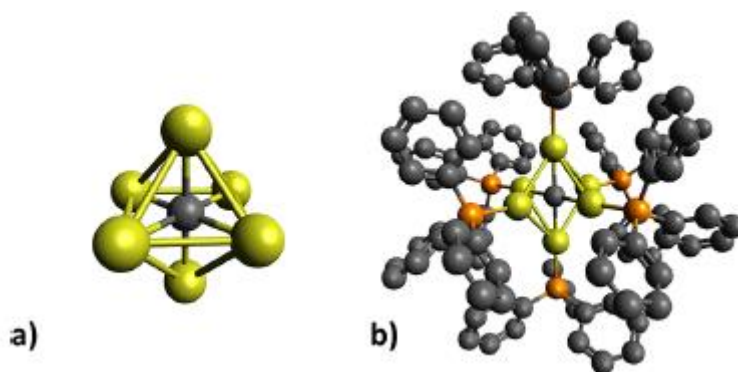


Figure 27. Structures of (a) the central CAu_6^{2+} cluster and (b) the entire cluster stabilized by phosphine ligands. Data from ref ¹⁶⁸.

Computations on the unsubstituted parent CAu_6^{2+} cluster gave $\delta^{\text{SO}}(^{13}\text{C}) = -240$ ppm (**Figure 27a**), which would lead to the even more exotic $\delta^{\text{tot}}(^{13}\text{C})$ of -288 ppm. Inclusion of the phosphine ligands into the model resulted in $\delta^{\text{SO}}(^{13}\text{C}) = +28$ ppm (see **Figure 27b**), which means that more than 300 ppm of the total chemical shift at the interstitial carbon results from the combined TLI of the six phosphine ligands! Inversion of the sign of $\delta^{\text{SO}}(^{13}\text{C})$ due to the presence of strong trans ligands in Au complexes is now well-known,^{99,114,119} but in 2005 it prompted Le Guennic et al. to carefully re-examine their computational methodology. The large SO-HALA effects were confirmed, with a “final” calculated $\delta^{\text{tot}}(^{13}\text{C})$ of $+129$ ppm, in excellent agreement with experiment. While the origin of the large shielding of the interstitial carbon atom was not explained, the observed modulation of SSO is remarkable.

4.2.6. Group 12: Mercury

While we discuss the group 12 elements in the d-block section, we note that they are often viewed as “post transition-metal” or “representative” p elements, as their $(n - 1)d$ -orbital participation in bonding tends to be minor. Indeed, the SO-HALA effects for Hg^{II} complexes are dominated by the np orbitals, leading to considerable SO-HALA deshielding, **Figure 26**, which is due to the $6p \leftrightarrow 6p^*$ -based $\sigma^*_{\text{HA-LA}} \leftrightarrow n_{\text{HA}}$ deshielding mechanism (**Figure 20b**).^{26,99,100,114} Building on the pre-2004 work discussed in **section 1**,³⁸ more recent (experimental and computational) studies of relativistic effects (both SR and SO) on the ^{13}C NMR shielding constants in organomercury compounds have shown deshielding SO contributions up to $+52$ ppm (for sp-hybridized carbon atoms).¹³⁰ Notably, SR deshielding effects were observed at the LA in contrast to the shielding δ^{SR} in Pt and Au complexes discussed above.¹⁰⁴ Alternating signs of Hg-derived long-range SR effects on neighboring atoms were noted,¹³⁰ with $\delta^{\text{SR}} = +28$ ppm, -10 ppm, and $+2$ ppm for C_α , C_β , and C_γ , respectively. While the alternation of the sign of δ^{SR} resembles the oscillations of δ^{SO} that have been linked to FC-based J-coupling mechanisms,²⁶ the SR effects likely operate via inductive effects, polarizing the intervening bonds. Notably, a $\delta^{\text{SR}}(^{13}\text{C}_\alpha)$ of only $+1$ ppm has been calculated at the sp-hybridized acetylide α -carbon in CH_3HgCCH , compared to the much larger $\delta^{\text{SR}}(^{13}\text{C}_\alpha)$ of $+20$ ppm for the sp^3 hybridized methyl group. This is the exact opposite of δ^{SO} (cf. **Figure 7**), which is enhanced by the increasing LA s-character in the HA—LA bond. ATLI on the ^{13}C NMR shifts in $\text{LAHg}^{\text{II}}\text{X}$ complexes was noted earlier³⁸ and has been analyzed in detail in the $\text{PhHg}^{\text{II}}\text{X}$ series⁹⁹ (see discussion of groups 10 and 11 above).

4.3. HAs of the p-Block

4.3.1. General Aspects

The periodic trends of the SO-HALA effect in the p-block are governed predominantly by the occupation or vacancy of $np\ n_{\text{HA}}/n_{\text{HA}}^*$ orbitals, which directly relates to the oxidation state of the HA.¹⁰⁰ Calculated SO-HALA NMR shift ranges in p-block element complexes, based on references discussed in this section, are summarized in **Figure 28**.

The presence of the low-lying vacant $np\ n_{\text{HA}}^*$ orbitals together with a small HOMO—LUMO energy separation maximizes the SO-HALA deshielding mechanism (**Figure 20b**) in group 13 and 14 compounds with the HA in oxidation state I and II, respectively. Maximum deshielding (up to several hundreds of ppm for ^{13}C LAs) has been computed for Tl^{I} and Pb^{II} compounds.^{91,32} Increased deshielding was also calculated for In^{I} complexes.¹⁶⁹

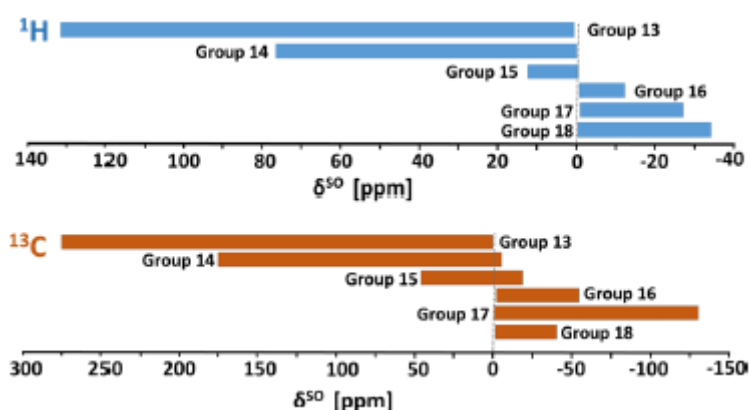


Figure 28. Computed ranges of the ^1H and ^{13}C SO-HALA shifts for individual groups in the p-block (LA bonded directly to the HA).

On the other hand, involvement of the HA ns orbitals in bonding (incomplete hybridization of s and p orbitals of rather different orbital sizes) disrupts the efficient orbital overlaps in the magnetic couplings and increases the HOMO—LUMO separation, which results in SO-HALA effects in Tl^{III} and Pb^{IV} compounds that maybe an order of magnitude smaller than for their $\text{Tl}^{\text{I}}/\text{Pb}^{\text{II}}$ counterparts.

Vertical trends in the p-block using typical oxidation states are compared in **Figure 29** for the $\delta^{\text{SO}}(^{13}\text{C})$ of the sp -hybridized C_α atoms of acetylide substituents bound to different p-block HAs.⁵¹

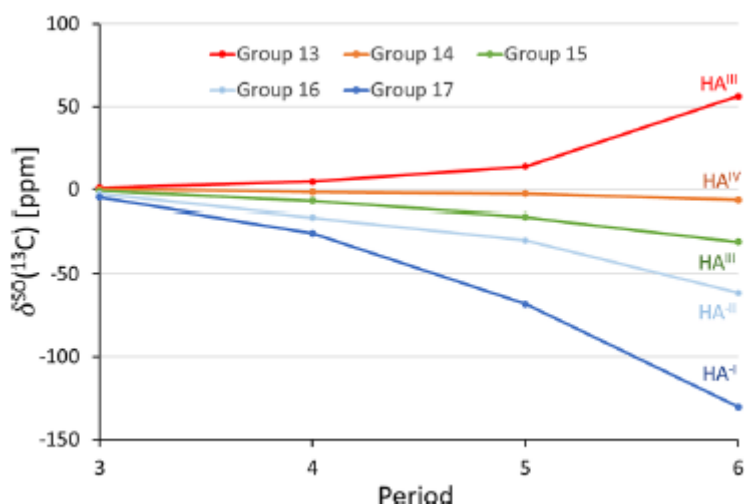


Figure 29. Comparison of trends in $\delta^{\text{SO}}(^{13}\text{C}_\alpha)$ for acetylide substituents bound to heavy p-block elements (with 0, 0, 1, 2, and 3 n_{HA} for groups 13, 14, 15, 16, and 17, respectively). Data from **ref 51**.

Note that nonbonding MOs are absent from the group 13 and 14 examples. In the former, the $\sigma_{\text{HA-LA}}^* \leftrightarrow n_{\text{HA}}^*$ deshielding mechanism (**Figure 21b**) dominates and leads to an inverse dependence, while the group 14 HA^{IV} compounds lack low-lying n_{HA}^* orbitals and thus exhibit small shielding contributions which originate in the $\sigma_{\text{HA-L}} \leftrightarrow \sigma_{\text{HA-LA}}^*$ contributions (see rule 2 in the beginning of this section).

We recall that the absence of larger shielding SO-HALA contributions due to inefficient SO/FC pathways may lead to a trend that is inverse to halogen dependence for certain LAs with small s-character in the HA—LA bond, such as early d-block elements in their halide complexes. In that case the IHD is mostly of paramagnetic origin.⁴² However, for HAs of group 13, the inverse trend (analogous to IHD) down the group is due to increasingly deshielding SO-HALA effects (**Figure 29**). This has been termed a triel dependence.⁵¹

In groups 15—17, the SO-HALA shielding increases with the group number and with decreasing oxidation state of the HA, i.e., with an increasing number of occupied $\text{LP}_{\text{HA}}(\text{s})$. Group 15 compounds actually represent a borderline where the SO-HALA mechanisms of deshielding and shielding largely compensate each other, often resulting in a small overall (in absolute value) δ^{SO} .^{51,100} Maximum SO-HALA shielding at the LA is observed in group 17 complexes in low oxidation states, i.e., halogens in oxidation state +I/-I with two occupied π -type LPs at the Ha.^{49,51,100} Regarding group 18, LA SO-HALA shifts were studied only for Xe compounds and are generally smaller than in group 17 compounds, except the outlier $\delta^{\text{SO}}(^1\text{H})$ in HXeF , which explains the extended ^1H NMR range in **Figure 28**.

4.3.2. Groups 13 and 14: Triels and Tetrels

The SO-HALA-induced ^{13}C chemical shifts in group 13 HA^{III} and group 14 HA^{IV} complexes have been thoroughly investigated using model ethane-, ethene-, and ethyne-substituted systems.⁵¹ Distinct SO-HALA deshielding was noted down the group 13 HA^{III} complexes, ranging from $\delta^{\text{SO}}(^{13}\text{C}) = +0.9$ ppm in $\text{H}_2\text{Al}^{\text{III}}(\text{CCH})$ to $\delta^{\text{SO}}(^{13}\text{C}) = +57$ ppm in $\text{H}_2\text{Tl}^{\text{III}}(\text{CCH})$. Comparatively smaller shielding $\delta^{\text{SO}}(^{13}\text{C})$ was calculated in group 14 $\text{H}_3\text{M}^{\text{IV}}(\text{CCH})$ complexes ($\text{M} = \text{Si}^{\text{IV}}$ to Pb^{IV}) ranging from -0.3 ppm to -6 ppm in $\text{H}_3\text{Pb}^{\text{IV}}(\text{CCH})$.⁵¹ This is not surprising, as the availability of low-lying HA-centered unoccupied MOs,

important for the SO-HALA deshielding mechanism, is diminished as we move from tricoordinated group 13 to tetra-coordinated group 14 systems, and the SO-HALA shielding effects originating in $\sigma^{\text{HA-LA}} \leftrightarrow \sigma^*_{\text{HA-LA}}$ mechanism prevail. Notably, the overall reported relativistic contributions to the ^{13}C NMR resonances in group 14 HA^{IV} systems are deshielding (up to +11 ppm) as a result of dominant deshielding SR effects (δ^{SR} up to +17 ppm for the C_α of an alkyl Pb^{IV} complex), which are only partially compensated by SO-HALA shielding contributions ($\delta^{\text{SO}} = -6$ ppm in the same complex).⁵¹ Similar results had been reported previously for group 14 hydrides ($\text{HA}^{\text{IV}}\text{H}_4$, HA = C, Si, Ge, Sn, and Pb) using complete active space self-consistent field (CASSCF) calculations,¹⁷⁰ where small ^1H SO-HALA shieldings and overcompensating deshielding δ^{SR} contributions were reported. A deeper PT2 analysis of those model Pb^{IV} systems, performed for the purpose of this review, reveals a number of small SO-HALA shielding and deshielding MO couplings balanced by several factors, mostly related to the substituents present.

A delicate dependence of both SR and SO-HALA effects on electronic structure has also been pointed out in a fully relativistic DFT study of $\delta(^{13}\text{C})$ in group 14 (M^{IV}) alkynyl compounds.⁹² For instance, a deshielding δ^{SR} up to +16 ppm and a shielding δ_{SO} up to -13.5 ppm were calculated for C_α in tetra-alkynyl complexes of Pb^{IV} , in good agreement with previous findings.^{51,170} However, when three out of the four alkynyls were replaced by methyl groups, the signs of both the SR and the SO contributions on the remaining alkynyl C_α switched, to $\delta^{\text{SR}} = -7$ ppm and $\delta^{\text{SO}} = +4$ ppm. No explanation for this observation was given in that work, but we speculate that it may be related to a larger covalency of the $\text{Pb}-\text{CH}_3$ than the $\text{Pb}-\text{alkynyl}$ bonds, influencing the energy and composition of the $\text{Pb}-\text{L}$ bonding orbitals (particularly orbitals with n-character relative to the $\text{Pb}-\text{LA}$ bond) and thus also affecting the corresponding orbital magnetic couplings. In summary, the SO-HALA effects in the $\text{M}^{\text{IV}}\text{L}_4$ tetrel complexes of group 14 are relatively small, and their sign depends heavily on the substituents present.

Moving to the lower oxidation states in groups 13 and 14, the recently predicted extremely deshielding $\delta^{\text{SO}}(\text{LA})$ in Tl^{I} and Pb^{II} compounds^{91,132} can be up to +200 ppm for ^{13}C , to +1000 ppm for ^{29}Si , and to +80 ppm for ^1H NMR chemical shifts. The origin of this extraordinarily large SO-HALA contribution relates to the geometrical and electronic structures of Tl^{I} and Pb^{II} compounds. Large deshielding $\sigma^{\text{HA-LA}} \leftrightarrow n^*_{\text{HA}}$ orbital magnetic couplings arise from the interplay of occupied and vacant 6p-based MOs, which are rotated by 90 degrees relative to each other (**Figure 20b**). This results in nearly perfect magnetically induced orbital overlap, further complemented by rather small energy gap(s) between $\sigma_{\text{HA-LA}}$ and n^*_{HA} MOs.¹³²

Extreme deshielding SO-HALA effects readily explain why certain NMR signals were absent in the experimental spectra of some previously studied Tl^{I} and Pb^{II} compounds; such signals lie far outside the typical NMR spectral ranges,¹³² see **Figure 28**. Hence, only a few months after the computational prediction,⁹¹ a record ^1H NMR shift of more than 35 ppm in a dinuclear Pb^{II} hydride was experimentally confirmed.¹⁷¹ Since then, a growing number of new experimental studies have been motivated by the discovery of extreme SO-HALA effects in Pb^{II} compounds, and old attempts to prepare the Pb^{II} hydrides and investigate their chemistry have been revived.¹⁷¹⁻¹⁷³

An analogous but an order of a magnitude smaller deshielding δ^{SO} has been calculated for some Sn^{II} compounds.^{91,132} It should be noted, however, that in certain circumstances, such as the involvement of the HA in clusters, relatively large shielding SO-HALA effects can also be found for Sn^{II} species. In earlier computations on $\text{Sn}-\text{P}$ cages,¹⁷⁴ sizable SO-HALA shielding contributions to the ^{31}P shifts were calculated (-80 ppm at the phosphorus atoms adjacent to three Sn^{II} centers). This is a rather extreme example of the influence of structural aspects on the SO-HALA effect.

The magnitude of $\delta^{\text{SO}}(^1\text{H})$ in both Sn^{II} and Pb^{II} hydrides has been reported to depend on the coordination number of the central atom.⁹¹ This was rationalized by the variable involvement of Sn and Pb np^* orbitals in ligand binding, making them less accessible for the SO-HALA deshielding mechanism in case of higher coordination numbers of the HA. SO-HALA shifts in Sn^{II} and Pb^{II} compounds thus sensitively probe the coordination sphere of the central metal atom. A practical application of the dependence of the SO-HALA effect on electronic structure¹⁷⁵ showed that a sizable decrease of $\delta^{\text{SO}}(^{13}\text{C}_\alpha)$ in cyclic plumbanes from ~ 80 to ~ 20 ppm can be used to probe the formation of adducts with Lewis bases. This decrease results from the involvement of the Pb $6p^*$ orbitals in adduct formation, which increases the energy denominators in the SO/FC formula (**section 2.3.3**).¹⁷⁵

Four-component relativistic DFT calculations of the NMR chemical shifts in a dimeric plumbylene,¹⁷⁶ $[\text{Fe}\{(\text{n5-C}_5\text{H}_4)\text{-NSiMe}_3\}_2\text{Pb}]_2$, which can activate aromatic C—H bonds under normal conditions, revealed a large difference between the $\delta^{\text{SO}}(^{15}\text{N})$ values of the two nitrogen atoms bound directly to the lead center (76 ppm vs 9 ppm). This difference was rationalized based on the covalency of the individual Pb—N bonds, which was in turn used to explain the unexpected shielding of one of the ^{207}Pb resonances.

4.3.3. Group 15: Pnictogens

The SO-HALA effects in compounds with an HA of group 15 are mostly shielding, and the role of the oxidation state of the HA seems less pronounced (so far it is reported to be notable only for bismuth). For instance, the calculated⁵¹ SO-HALA shielding at $^{13}\text{C}_\alpha$ alkynyl atoms ranges from $\delta^{\text{SO}} = -1$ ppm in $\text{H}_2\text{P}^{\text{III}}\text{CCH}$ to $\delta^{\text{SO}} = -31$ ppm in $\text{H}_2\text{Bi}^{\text{III}}\text{CCH}$. A weak ^1H SO-HALA shielding of -0.2 ppm for hydrogen atoms bound to phosphorus has been noted.⁶⁵ The rovibrational, thermal, and relativistic corrections to the ^{19}F shielding constants in group 15 trifluorides (NF_3 , PF_3 , and AsF_3) have been investigated using a combination of nonrelativistic coupled-cluster with single, double, and triple excitations (CCSDT) and relativistic DFT calculations.¹⁷⁷ Weakly shielding $\delta^{\text{SO}}(^{19}\text{F})$ up to -4 ppm was observed. A similarly large SO-HALA ^{13}C shielding down to $\delta^{\text{SO}} = -4$ ppm was calculated at a carbon atom bound to As in a number of naturally occurring organo-arsenic compounds, including a variety of isomers of Arsenicin A, for which an adamantane-like structure has been proposed.¹⁷⁸ Inclusion of SO-HALA effects in the calculations was found necessary in order to distinguish between the individual isomers of Arsenicin A, enabling the confirmation of the adamantane-like structure.

A rather small SO-HALA shielding $\delta^{\text{SO}}(^{13}\text{C}) = -4$ ppm was predicted at $^{13}\text{C}_{\text{ipso}}$ in triphenylbismuth.¹⁷⁹ The C_{ipso} of phenyl (Ph) substituents was later used to study the dependence of the SO-HALA effect on the oxidation state of Bi in $\text{Bi}^{\text{III}}\text{PhCl}_2$ and $\text{Bi}^{\text{V}}\text{PhCl}_4$.¹³² Small SO-HALA shielding at C_{ipso} was predicted in $\text{PhBi}^{\text{V}}\text{Cl}_4$ ($\delta^{\text{SO}} = -2$ ppm), probably resulting from a low availability of low-lying LP^* MOs for the SO-HALA deshielding (compare to Pb^{IV} compounds above) and stabilization of the HA-L MOs, which diminishes the SO-HALA shielding mechanism.¹³² A notably larger SO-HALA deshielding $\delta^{\text{SO}} = +50$ ppm) was calculated for $\text{PhBi}^{\text{III}}\text{Cl}_2$. The latter value is nearly an order of magnitude larger than the one predicted for the same ligand C_{ipso}(Ph) in triphenylbismuth (see above).¹⁷⁹ The reasons for this effect are explained at the bottom of next paragraph.

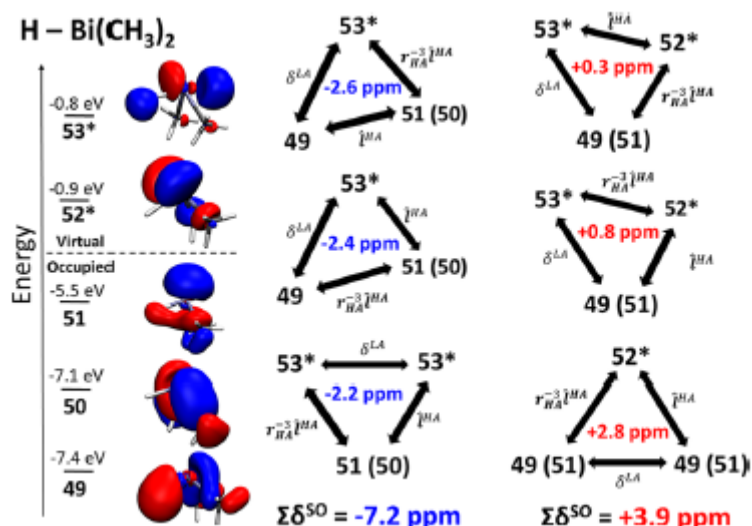


Figure 30. Schematic PT3 visualization of the $\delta^{\text{SO}}(^1\text{H})$ deshielding (top) and shielding (bottom) orbital magnetic couplings computed for $\text{HBi}(\text{CH}_3)_2$. Adapted from ref ¹⁰⁰. Copyright 2018 American Chemical Society.

Another example of the importance of the ligand sphere for SO-HALA shifts can be found for Bi^{III} hydrides. The simple hydride $\text{HBi}^{\text{III}}(\text{CH}_3)_2$ (**Figure 30**) has an ^1H NMR shift of 2.1 ppm,¹⁸⁰ with a small $\delta^{\text{SO}}(^1\text{H})$ of 0.7 ppm.¹⁰⁰ Replacing the methyl groups with a pair of large terphenyl substituents¹⁸¹ results in a total ^1H shift of 19.4 ppm and in $\delta^{\text{SO}}(^1\text{H}) = 14.4$ ppm (presented in this work, calculated at the same level as used in **ref 91**). The delicate dependence of δ^{SO} on the nature of the substituents can be rationalized by a competition between the shielding and deshielding SO-HALA mechanisms in Bi^{III} compounds, which has been explained for a Bi^{III} hydride using PT3 theory,¹⁰⁰ see **Figure 30**. Essentially, differences in the covalency of the Bi—L bonds promote one mechanism at the expense of the other. More electron-donating substituents (i.e., the terphenyl group in these hydrides) stabilize those Bi-L bonding orbitals that contribute most to the SO shielding mechanism. This diminishes the negative, shielding $\sigma_{\text{HA-L}} \leftrightarrow \sigma_{\text{HA-LA}}^*$ SO-HALA contributions, while the positive (deshielding) SO-HALA contributions remain largely unaffected. Hence, considerably larger SO deshielding may be observed at the LA when more charge-withdrawing substituents are present in the molecule. This applies also to the Pb^{IV} compounds, see above.

4.3.4. Group 16: Chalcogens

The SO-HALA effects in heavy chalcogen compounds have been well investigated, at least partly because the favorable spin 1/2 of ⁷⁷Se and ¹²⁵Te nuclei give rise to experimental multinuclear NMR studies that frequently also include the lighter nuclei. Relativistic effects on the NMR chemical shifts in heavy chalcogen compounds have been studied mostly by relativistic DFT methods.^{51,164,182-185} Generally, the SO-HALA shielding increases uniformly with ZHA down group 16 and also increases with the number of occupied LPs at the HA, i.e., for a lower HA oxidation state. Maximal SO-HALA shieldings (>50 ppm) are reached for the heavier chalcogen compounds (Se and Te) in oxidation state — II, when a double bond to the LA is present (as in seleno- and telluroketones).^{164,182,185} This bonding situation clearly favors the propagation of the SO-HALA effects from the HA to the LA in p-block species and additionally involves small energy denominators. Even a relatively “light” HA like sulfur can induce an

overall δ^{50} shielding of -8 ppm at the adjacent ^{13}C nuclei of CS_2 via the $\text{C}=\text{S}$ double bonds.^{164,185} In addition to the two factors mentioned above, a large carbon $2s$ character in the $\text{C}-\text{S}$ bonds (formal sp^2 hybridization) also aids this shielding. A thorough study of the SO-HALA effects in heavy chalcogen complexes at the Coupled-Cluster with Single and Double and Perturbative Triple excitations CCSD(T) and Breit-Pauli Perturbation Theory (BPPT) levels of theory was performed to evaluate secondary isotope effects on nuclear shielding in CSe_2 .^{185,186}

Large SO-HALA effects propagating over several bonds in experimentally known seleno- and telluroketones were calculated using relativistic DFT methods.¹⁸⁷ The long-range SO-HALA effects on the ^{13}C shifts were found to be -23 , $+18$, and -9 ppm for C_α , C_β , and C_γ , respectively. This alternation of the sign reflects the analogy of the SO/FC mechanism with that of J-coupling²⁶ (**section 3.1**). Moreover, $\delta^{50}(\text{C}_\gamma)$ fulfilled the Karplus double-cosine dependence on the $\text{M}-\text{C}_\alpha-\text{C}_\beta-\text{C}_\gamma$ dihedral angle, also known for J-coupling.^{26,140} In a follow-up study,¹⁸⁸ the authors found similar relations (sign alternation and Karplus dependence), for H_β and H_γ nuclei in analogous systems. These results confirm earlier findings^{113,140} that, when sufficiently large, δ^{50} can be used to determine dihedral angles and isomerism.

4.3.5. Group 17: Halogens

The first mentioned^{19,20} and most intensively studied SO-HALA effect is the normal halogen dependence (NHD), which refers to the increasing SO-HALA shielding at the LA with increasing ZHA of an adjacent halide substituent for both organic and inorganic compounds. While we saw analogous dependencies throughout groups 14–17 (see **Figure 29** in **section 4.3.1**), the SO-HALA effects and thus the NHD-type behavior tends to be most pronounced for HAs from group 17. Given that the SO-HALA effect depends on the number of halogen LPs,⁴⁹ NHD has been studied largely for halide substituents, and the number of studies is so large that we do not attempt a comprehensive coverage of the literature in this case. For example, since 2004, computational investigations of NHD for ^1H and ^{13}C NMR shifts have targeted hydrogen¹⁸⁹ and methyl^{135,189} halides, halogen-substituted acetonitrile,¹⁹⁰ cyclohexane,¹⁹¹ pyran,¹⁹¹ purines,¹⁰⁵ and carbazoles.¹⁹² Studies of NHD on the NMR chemical shifts and shielding tensors of ^{11}B , ^{19}F , and ^{29}Si nuclei at various levels of theory¹⁹³⁻¹⁹⁵ led to essentially the same trends and conclusions as for ^1H and ^{13}C nuclei. Higher halogen oxidation states have been mentioned in **Section 1**.⁴⁹

One of the computationally most advanced and detailed studies focused on the ^{13}C and ^1H shift tensors in the methyl halides using combined ab initio and DFT analyses with perturbation theory (PT), complemented by vibrational corrections and thermal averaging.¹³⁵ The SO origin of the NHD was confirmed (the SO/FC term dominates the PT contributions), although SR effects of opposite sign (deshielding) were found important in order to obtain quantitative agreement with experiment. Note that the SR effects do not follow the SO-HALA trends but tend to be generally deshielding for HAs of the p-block. Relativistic DFT and BPPT computational approaches were also applied to the propagation of SO-HALA effects in heteroaromatic 6-halopyridines.¹⁰⁵ The authors concluded that relativity, solvent effects, and the choice of reference compound are important for achieving quantitative agreement between theory and experiment. Long-range relativistic effects were also studied, and the previously discussed sign alternation of the SO-HALA contributions⁴⁷ was also seen in these heterocyclic systems.

Interestingly, the magnitude of the SO-HALA effect induced by heavy halide substituents depends on the conformation of stereoisomers. The propagation of the SO-HALA effect was diminished in halogenated hydrocarbons¹⁹¹ when strong hyperconjugative interactions involving $\sigma^*_{\text{C}-\text{X}}$ orbitals ($\text{X} = \text{halogen}$) were present. The authors calculated various con-formers of halocyclohexanes and 2-halo-

tetrahydropyran and analyzed the SO-HALA effects on the ^{13}C shifts. The SO contribution in the axial conformer of iodo-cyclohexane with stronger hyperconjugative interactions was found to be 7 ppm lower than in the equatorial conformer ($\delta^{\text{SO}} = 15.8$ ppm vs 22.8 ppm), confirming the experimentally observed difference of 8 ppm. Hyperconjugation was shown to stabilize the occupied LPHA orbitals and to thereby increase the relevant energy denominators. The changes in the SO-HALA effect thus determine the observed differences in shift and may be used to distinguish individual conformers. The authors pointed out, however, that this may apply only to structurally similar groups of molecules (conformers, isomers) where other factors influencing the SO-HALA effect (e.g., hybridization at the LA) are comparable. Subsequent work on the influence of stereoelectronic interactions on the SO and paramagnetic contributions to the ^{13}C NMR shielding tensors in dihaloethenes¹⁹⁶ came to similar conclusions: the hyperconjugative interactions involving the halogen LPs and $\text{c}^*_{\text{c-x}}$ antibonding orbitals (X = halogen), together with steric interactions between the halogen atoms, were found to be a major cause of the difference in $\delta(^{13}\text{C})$ between the cis vs trans isomers. These two studies nicely demonstrate the possible use of SO-HALA shifts to investigate isomerism and hyperconjugation in compounds with heavy halogen substituents.

4.3.6. Group 18: Aerogens

For obvious reasons, SO-HALA effects originating from noble-gas (Ng) heavy atoms have been studied less than those for group 17 HAs. A combination of ab initio and relativistic DFT levels for noble-gas hydride cations (NgH^+ ; Ng = Ne-Xe)¹³⁶ found the total relativistic effect on the ^1H shifts (the SO-HALA was not investigated separately) to range from ca. 0 ppm in NeH^+ to ca. -18.1 ppm in XeH^+ . A perturbational treatment of relativistic effects typically gave smaller SO-HALA effects for a series of HXeY ^{197,198} compounds than for HI ,¹⁸⁹ probably due to the lower covalency of the Rg-H bonds. The HXeF system with an extreme value of $\delta^{\text{SO}}(^1\text{H}) = -35$ ppm, probably caused by the TLI of fluorine, was an exception.^{197,198}

While no structure-related applications of SO-HALA effects have yet been reported for Ng compounds, the known correlations between δ^{SO} and the covalency of the HA-LA bond¹¹⁴ can be useful in determining the character of Ng-LA bonds and the oxidation state of the Ng by using a combination of relativistic calculations and NMR studies, as suggested in **refs 197** and **198**.

4.4. HAs of the f-Block

4.4.1. General Aspects

Investigation of the SO-HALA trends in lanthanide and actinide complexes has been limited to the closed-shell $4f^0$ (La^{III} , Ce^{IV}), $4f^{14}$ (Lu^{III}), and $5f^0$ (Th^{IV} , Pa^{V} , and U^{VI}) electronic configurations, as others typically feature paramagnetic metal centers and thus different physics of nuclear shielding. In these closed-shell configurations, the f-elements have formally empty, low-lying valence (n-1)d and/or (n-2)f shells. Hence, the deshielding $\sigma^*_{\text{HA-LA}} \leftrightarrow \text{n}^*_{\text{HA}}$ coupling mechanism dominates, similar to the p^0 and d^0 cases (**Figure 23**).^{97,100,137,199} A relatively small deshielding $\delta^{\text{SO}}(^1\text{H}) \approx +5$ ppm, has been calculated for La^{III} and Lu^{III} hydrides.¹⁰⁰ This is comparable to 5d^0 transition-metal hydrides, which may reach $\delta^{\text{SO}}(^1\text{H})$ values up to ca. + 10 ppm (e.g., Hf^{IV} , Ta^{V} , W^{VI} , and Re^{VII} , **Figure 26**).

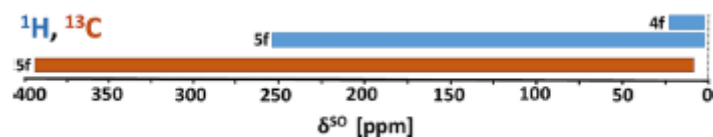


Figure 31. Computed ranges of the ^1H and ^{13}C SO-HALA shifts in 4f and 5f complexes (LA bonded directly to the HA).

A larger deshielding effect of $\delta^{\text{SO}}(^1\text{H}) \approx +20$ ppm was predicted for a Ce^{IV} hydride, see below. The ranges of the SO-HALA ^1H and ^{13}C shifts in 4f and 5f complexes that have been predicted are summarized in **Figure 31**.

The availability of low-lying 5f-orbitals and the involvement of the 5f-shell in chemical bonding is decisive for the $5f^0$ systems. Moderately deshielding SO-HALA effects (5–12 ppm), comparable to $5d^0$ systems, are found for Th^{IV} complexes^{137,200} because 6d and 7s orbitals dominate Th^{IV} bonding with only minor involvement of the relatively diffuse 5f orbitals.^{137,200} A protactinium model hydride complex $[\text{HPaF}_5]^-$ has been predicted to have $\delta^{\text{SO}}(^1\text{H}) > +50$ ppm, which indicates that 5f-orbitals which are more available can strongly enhance the deshielding SO-HALA effects.¹² This effect is further enhanced for U^{VI} hydride complexes with $\delta^{\text{SO}}(^1\text{H})$ predicted to be well over +200 ppm in model hydrides and $\delta^{\text{SO}}(^{13}\text{C})$ of nearly +400 ppm for carbon atoms directly bound to the U^{VI} centers in organometallic complexes (see below).^{95,97,201}

The oxidation state again plays a potentially important role in the size and sign of the SO-HALA effects, as it does for the d- and p-block elements. In contrast to the large deshielding $\delta^{\text{SO}}(\text{LA})$ in $5f^06d^0$ U^{VI} complexes, a strongly shielding $\delta^{\text{SO}}(^1\text{H})$ of -37 ppm has been predicted for a hypothetical closed-shell $5f^26d^0$ U^{IV} complex. While this $5f^2$ model system is unlikely to reflect any real U^{IV} ground-state complex, the computations confirm that the general mechanism outlined above (SO shielding due to LPs at the HA)¹⁰⁰ can also be applied to 5f actinide systems. The δ^{SO} of this hypothetical closed-shell U^{IV} complex is not included in **Figure 31** because no closed-shell $5f^2$ complexes are known to exist.

4.4.2. Selected Examples and Applications

SO-HALA effects in lanthanide complexes have, until now, been investigated only very sparsely, probably due to a limited number of known closed-shell species.^{100,199} Very small SO-HALA effects (<1 ppm) were computed for the nitrogen atoms of a phenanthroline ligand bound directly to lanthanum, probably due to the highly ionic La-N bonding.¹⁹⁹ On the other hand, a large ¹H SO-HALA deshielding ($\delta^{\text{SO}} = +20$ ppm, $\delta^{\text{tot}} \approx +31$ ppm) has been predicted for a Ce^{IV} hydride¹⁰⁰ and rationalized by the involvement of formally vacant Ce 4f orbitals in the Ce-H bonding and thus also in the $\sigma^*_{\text{HA-LA}} \leftrightarrow n^*_{\text{HA}}$ deshielding mechanism, in analogy to U^V, see **Figure 32**. However, neither this prediction for Ce^{IV} nor the U^{VI} case described below has been confirmed experimentally.

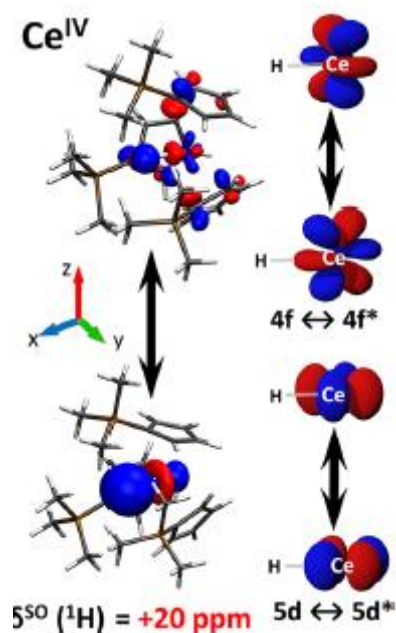


Figure 32. Example of the orbital magnetic coupling in a Ce^{IV} hydride complex (top) and schematic representation of the AOs contributing to the SO deshielding (bottom). Adapted from **ref 100**. Copyright 2018 American Chemical Society.

The NMR shifts of closed-shell actinide complexes have been studied extensively over the years. Early relativistic DFT computations of the ¹⁹F shifts in U^{VI} fluoride complexes gave modest SO-HALA shifts up to about 30 ppm^{41,202} because the low fluorine 2s-character in the U—F bond disfavors the FC mechanism. Much of the early work focused on the challenges of computing the NMR shifts for actinide complexes, e.g., choosing the sizes of the ECP cores and the exact-exchange admixtures to use in the DFT functionals.^{97,137,201} The calculation of ¹⁹F NMR shifts in actinide systems has been reviewed critically.²⁰³

A two-component ZORA study of the ¹H shifts in U^{VI} hydride complexes¹³⁷ was aimed explicitly at investigating potentially large SO-HALA shifts. The results indeed suggested giant deshielding of more than +100 ppm in some of the model systems studied. As no experimental NMR data for such species are yet available (the only known U^{VI} hydride complex, H₂UO₂, has been studied only by matrix-isolation IR spectroscopy),²⁰⁴ selecting a suitable functional to make valid predictions required that other reference data be available. These were the ¹³C NMR shifts of some U^{VI}-bound carbon atoms in organometallic complexes. Except for the system discussed in the next paragraph, comparison with the available experimental ¹³C data suggested the use of a hybrid functional with 40% exact-exchange

admixture. Notably, this was due to the absence of an exchange-correlation kernel in the 2-component ZORA implementation used at the time.^{96,97,153} A systematic reinvestigation of the ¹H and ¹³C NMR shifts in U^{VI} complexes including the exchange-correlation kernel (in comparison with 4-component results)⁹⁷ suggested that functionals with a lower exact-exchange admixture (20–25%) are more appropriate. Nevertheless, the giant SO-HALA shifts were confirmed.

The one ¹³C case for which the predictions of **ref 137** disagreed starkly with the available experimental data was an unusual U^{VI}-hexaalkyl complex. Here the uranium-bound methylene ¹³C NMR shift had been assigned originally to a signal at +34 ppm, which was likely a contaminant in the in situ spectrum,²⁰⁵ while the computations suggested values closer to 400 ppm because of the extremely large SO-HALA shifts. Such shifts are completely outside the usual expectations for an alkyl carbon atom, and consequently the original measurements had been restricted to a range between –50 and +130 ppm. A new measurement with a larger spectral range gave a value of 434 ppm,²⁰¹ in line with the computational predictions, and confirming the existence of giant SO-HALA shifts of more than +300 ppm. The predictive quality of the computational methods suggested a blind test of computed and measured ¹³C NMR shifts for a newly found tetraalkyluranyl complex. The computed shift of +250 ppm agreed excellently with the independently measured value of +243 ppm, again with sizable SO-HALA contributions of about +177 ppm.²⁰¹

These results were still obtained with 40% exact-exchange admixture and without a kernel in the perturbation treatment. The above-mentioned reinvestigation of **ref 97** with a kernel and other functionals confirmed overall the large SO-HALA shifts also for these cases while providing some corrections to the quantitative data. That study also gave further predictions, in particular an extension of the range of U^{VI}-bound ¹³C NMR shifts up to +550 ppm ($\delta^{\text{SO}} = +390$ ppm) for organometallic model complexes, and it suggested the positions of missing signals in experimentally characterized complexes.⁹⁷ Systematic analyses correlated the SO-HALA shifts with the covalency of the U–C bond and the position of the LA in the complex. For example, atoms opposite to strong n-donors (e.g., in uranyl complexes) were found to have smaller SO-HALA shifts than nuclei positioned trans to less π -donating ligands, e.g., in the above-mentioned hexaalkyl complex.⁹⁷

Covalency was also studied in rare actinide-chalcogen Th^{IV} and U^{VI} complexes by ⁷⁷Se and ¹²⁵Te NMR.²⁰⁶ Curiously, selenium and tellurium constitute the “LA” in these systems, and their chemical shifts include SO-HALA effects arising from the actinide center. The $\delta^{\text{SO}}(^{77}\text{Se})$ and $\delta^{\text{SO}}(^{125}\text{Te})$ were found to increase linearly with the covalency of the actinide–chalcogen bond ($R^2 = 0.92$ – 0.99) expressed as the delocalization index. In one of the U^{VI} complexes studied, a ⁷⁷Se NMR shift of 4900 ppm was measured, which extends the known chemical shift range for this nucleus in diamagnetic systems from the previous record of 3300 ppm. Even larger ⁷⁷Se shifts, up to 8000 ppm, have been predicted computationally.²⁰⁶

Uranyl 17O NMR chemical shifts have been investigated recently²⁰⁷ by combined experimental and computational approaches. The ab initio calculations revealed that the 17O resonances were very sensitive to the local environment, a fact which could be used to provide better understanding of the structure and crystal packing of such compounds in the solid state. A thorough evaluation of the DFT approaches to calculating various properties of uranium complexes, including computation of the relativistic NMR shift, has been reported recently.²⁰⁸

4.5. Superheavy Elements (SHEs) as Has

Given the short half-lives of SHEs, the chances for experimental NMR studies of their compounds are slim at best. Therefore, computational studies have also been almost nonexistent. So far, only one set of computations (done at four- and two-component levels) is available for a number of postactinide complexes with $6d^6$, $6d^8$, and $6d^{10}$ HA configurations.²⁰⁹ Interestingly, the SOHALA shifts in the $6d^6$ complexes are slightly smaller or only marginally larger (in absolute value) than in their $5d^6$ analogs. This is due to greater ligand-field splitting (caused by the improved bonding interactions of the relativistically expanded $6d$ -orbitals) counteracting the larger SO matrix elements.¹¹³ The SO-shifts in $6d^8$ complexes are somewhat larger than in their $5d^8$ analogs. Notably, the ligand-field effects do not apply to the d^{10} configuration, and in consequence the deshielding SOHALA shifts are notably enhanced in the $6d^{10}$ hydrides compared to their $5d^{10}$ analogs, e.g. + 23.7 ppm for [HRg(NHC)] vs +3.3 ppm for [HAu(NHC)] (NHC is the simplest possible imidazolium-based N-heterocyclic carbenemodel ligand, Rg is roentgenium) or +33.1 ppm for [HCnPh] (Cn is copernicium) compared to +9.0 ppm for [HHgPh].²⁰⁹ All data given are predictions based on two-component SOZORA computations.¹³⁴

4.6. Weak Interactions and "Through-Space" SO-HALA Effects

The above-mentioned studies concentrated mostly on SO-HALA effects at an LA chemically bound to the HA (or involved in a covalent bonding network including the HA). However, in the same way as the FC mechanism of J-coupling operates via the polarization of the spin density even in the absence of "chemical bonds" ("through-space" J-coupling),²¹⁰ one can expect this to hold also for the SO-HALA chemical shifts, see **section 3.1.5**.

The possibility of "through-space" propagation of SO-HALA effects in pyridinium halide ionic liquids has been investigated computationally.²¹¹ Using various computational models, $\delta^{SO}(^{13}\text{C})$ up to +3 ppm was predicted at the pyridinium carbon atoms when pyridinium was involved in an ion pair with I_3^- , but this effect vanished with the Cl_3^- analog. The authors concluded that it may be challenging to find experimental evidence to support these computational predictions, owing to the short lifetime of the investigated ion pairs in a liquid environment. Notably, in contrast to typical shielding SO-HALA effects for bonded halogen substituents, the through-space SO-HALA contribution from X_3^- to the pyridinium carbon nuclei was found to be deshielding. This would correspond to an IHD, and the authors argued that the spin polarization is transmitted via the n-system.

Spectroscopic and computational evidence of an intramolecular $\text{Au}^{\text{I}}\cdots\text{H}-\text{N}$ hydrogen bond in a gold carbene complex was reported recently.²¹² While the SO-HALA effect can propagate only via an $\text{Au}\cdots\text{H}$ hydrogen bond, δ^{SO} values of -6 ppm and -0.1 ppm were predicted for the ^{15}N and ^1H nuclei, respectively, involved in the $\text{Au}^{\text{I}}\cdots\text{H}^+-\text{N}$ hydrogen bond. The SO-EDD⁹⁹ calculated for this system is shown in **Figure 33**. The low stability of the molecule in solution prohibited detailed experimental NMR investigations.

During the revision of this review, solid-state ^1H NMR and DFT study of a series of 4-(dimethylamino)pyridinium with Cl, Br, and I counteranions has been reported.²¹³ Discrepancy between the experimental and theoretical NMR shifts was attributed to an absence of the SO effects in the calculations of hydrogen-bonded ion pairs at the SR DFT level. However, agreement between the theoretical and experimental NMR data was significantly improved at the SO level that demonstrated propagation of the SO effects through hydrogen bonding which resulted in "through-space" SO-HALA shifts.

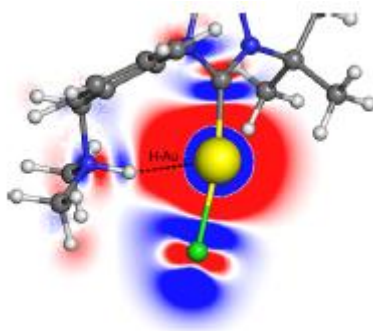


Figure 33. SO-EDD⁹⁹ for an intramolecular Au^I...H—N hydrogen bond in a gold carbene complex.²¹² The SO-induced increase and decrease in the electron density, which correspond to the sign of SO-HALA shift, are shown in blue and red, respectively.

The involvement of the HA in weak interactions may also indirectly influence the δ^{SO} at a bonded LA. As heavier halogens, particularly iodine, induce considerable (shielding) δ^{SO} at an adjacent LA, their involvement in halogen bonding modulates the size of δ^{SO} in analogy to the TLI reported for transition-metal complexes (see above), thus providing another tool to investigate halogen bonding.²¹⁴ Already in 2004,²¹⁵ following still earlier work,^{216,217} the effect of halogen bonding on the ^{13}C NMR chemical shifts of Ca in haloarenes in different solvents was studied. The authors noted that nonrelativistic deshielding of 6–8 ppm at C_α caused by the formation of a halogen bond was compensated by an induced SO-HALA shielding of similar size. One might thus mistakenly assume the absence of halogen bonding based on the total observed $^{13}\text{C}_\alpha$ NMR chemical shift.

Recently, a multinuclear solid-state NMR study investigated halogen bonding in various cocrystals.²¹⁸ The carbon atoms attached to a heavy halogen ($^{13}\text{C}_\alpha$) were found to be deshielded by +6 ppm when iodine derivatives were involved in halogen bonding. Two-component relativistic SO-ZORA calculations showed that modulation of both the paramagnetic and SO-HALA contributions to the $^{13}\text{C}_\alpha$ chemical shifts was the main cause of the observed deshielding. The relativistic ^{13}C NMR chemical shift was proposed as a possible indicator of halogen bonding, although the exact mechanism was not investigated. The calculated deshielding correlated with increasing C—I and C—Br bond lengths, as confirmed by other studies.²¹⁹ We speculate that the main cause of the observed deshielding is a decrease of the p-character/covalency of the C—X bond upon formation of the halogen bond,^{114,132} which in turn weakens the SO/FC propagation of the SO-HALA effect.¹¹⁴

4.7. Emerging Applications

In **Section 4**, we have explained and summarized how the SO-HALA shifts relate to the electronic structure of the heavy atom across the Periodic Table, that is, the periodic trends in SO-HALA effects. We hope the examples provided show that applications of SO-HALA shifts are not limited to merely aiding the assignments of experimental spectra or to improving the agreement between experimental and computational data. As demonstrated in **sections 3** and **4**, the SO-HALA shifts sensitively reflect—and thus can be used to study—various chemical phenomena, such as the structural trans and cis influences, the covalency of the HA—LA bond, molecular conformation and isomerism, and weak supramolecular interactions. The SO-HALA shifts also provide insights and links to chemical reactivity and may guide experimental efforts by revealing new and exotic ranges of NMR chemical shifts. A

thorough understanding of the SO-HALA shift thus represents a powerful tool for probing the structure and chemical properties of heavy-element compounds.

5. SUMMARY AND PROSPECT

Relativistic effects can influence the neighbor-atom NMR shifts in heavy-element compounds appreciably, with substantial and often analytically characteristic consequences for the NMR spectra. Relativistic neighbor-atom effects on NMR shifts are typically dominated by spin-orbit and magnetically induced spin polarization arising at the heavy atom and propagating to the spectator nucleus via a Fermi-contact-type interaction. This phenomenon, generally known as the spin-orbit heavy-atom effect on the light-atom NMR shift (SO-HALA shift), has been known for some time but is still underappreciated in the NMR community. Significant progress in our understanding of these effects across the Periodic Table since the last general review in 2004 and the recent availability of powerful MO-by-MO analysis and interpretative tools rooted in third-order perturbation theory called for a new and comprehensive exposition and critical overview of the theoretical background of SO-HALA shifts, of the conceptual tools available, and of the trends observed throughout the Periodic Table of the Elements.

Throughout this review we have compared both second-order perturbation theory based on relativistic molecular spinor pairs and third-order perturbation theory based on nonrelativistic (or scalar relativistic) MOs. The latter offers a more fine-grained analysis of SO-HALA shifts, in particular regarding the question of the sign of the effect—shielding vs deshielding. Provided a perturbational treatment of the SO effects does not cause too large errors, the PT3 treatment gives the clearer picture. It has been central to clarifying many of the concepts laid out in this overview. The terms obtained in the PT3 framework for the SO/FC mechanism of SO-HALA shifts can be connected directly to the bonding and electronic structure of the given system and can be displayed in a pictorial representation based on triangles linking the MOs and their energetics, as well as the perturbation operators. Further graphical insights can be provided by comparisons to the spin—orbital and magnetically induced spin density (SOM-ISD) and to changes in charge density induced by spin—orbital coupling (spin—orbital electron deformation density, SO-EDD). Together, these analyses and graphical tools allow for chemically intuitive interpretations of the SO effects on the neighbor-atom NMR shifts. This understanding is expected to greatly assist experimental chemists and NMR spectroscopists in estimating the ranges of the NMR shifts for unknown compounds, in the identification of intermediates in catalysis or other processes, in analyzing conformational aspects or intermolecular interactions, and in the prediction of trends in series of compounds throughout the Periodic Table.

Given the substantial progress made since the 2004 review referred to in **section 1** and the fast-growing literature with ever more examples of relativistic neighbor-atom effects on NMR shifts and their utilization in many fields of chemistry, it seems safe to expect further insights and a further widening of this topic over the coming years.

6. TECHNICAL AND COMPUTATIONAL DETAILS

To have a consistent data set on which to base our discussion, and to illustrate the concepts in **Section 3**, new data were calculated using the methods given below.

6.1. Optimization of Structure

Method 1: The structures were optimized using the Turbomole program (releases 6.3 or 7.3).²²⁰ The PBE0 functional,²²¹ scalarrelativistic effective core potentials (ECPs) for the HA, and def2-TZVPP basis sets were used.

Method 2: The structures were optimized using the ORCA 4.1 program.²²² The scalar-relativistic all-electron DKH approach, the PBE0 functional, and def2-TZVPP basis sets were employed.

6.2. Molecular orbital and bonding analysis

6.2.1. Natural Bonding Orbital (NBO) Analysis

Contributions of the AOs (e.g., d orbitals) to the HA—LA bond were calculated using the NBO 3.1²²³ module as implemented in Gaussian16.²²⁴ The PBE0 functional, an ECP for the HA, and def2-TZVPP basis sets were used.

6.2.2. Energy Decomposition Analysis-Natural Orbitals for Chemical Valence (EDA-NOCV).²²⁵

Charge and energy analysis of orbital contributions to the binding energy was performed in the ADF 2014 program.²²⁶ The computational setup was based on the ZORA/PBE0/TZP level of theory.

6.3. Calculation of SO-HALA Shifts

The SO-HALA data calculated for this work were obtained as the difference between four-component relativistic DFT calculations of NMR shifts⁷³ and calculations neglecting spin-orbit coupling (scalar-relativistic values - the contribution of the SO operator was down-scaled to 0),¹¹⁰ as implemented in the ReSpect program.^{93,154} The Dirac-Kohn—Sham (DKS) approach was used with the PBE0^{221,227} functional, Dyall-vtz basis sets^{228–230} for the HA, and pcS-2 basis sets^{231,232} for the other atoms (DKS/PBE0/Dyall-vtz/pcS-2 level).

6.4. Calculation and Visualization of the SO-and-Magnetically Induced Spin Density (SOM-ISD) and the Spin—Orbit Electron Deformation Density (SO-EDD)

The SOM-ISD maps¹⁰⁰ were calculated as implemented in the ReSpect program.^{93,154} The SO-EDD maps⁹⁹ were obtained as differences between the 3D electron density maps calculated at four-component and scalar-relativistic levels (to obtain scalar-relativistic values, the contribution of the SO operator was down-scaled to 0).¹¹⁰

6.5. Analysis of SO-HALA Shifts

6.5.1. Second-Order Perturbation Analysis (PT2)

The SO-HALA shifts were obtained as the difference between 2c-ZORA and 1c-ZORA values calculated in the ADF program. The analysis of MO ↔ MO and MSP ↔ MSP couplings was used as implemented in the ADF program.¹³⁴ The composition of 2c MSPs in terms of 1c-ZORA MOs was determined by

employing standard fragment analysis.¹³⁴ The graphical display of MSPs used only one real function of the complex, transformed spinor of a given Kramers pair.

6.5.2. Third-Order Perturbation Analysis (PT3)

The SO-HALA shifts were calculated and analyzed using the PT3 approach as implemented⁹⁹ in the ReSpect program.^{93,154} This implementation follows the third-order response theory of **ref 107** for the static (perturbation-free) case. The applied analysis considers only the one-electron contributions to the SO/FC NMR shielding and neglects all HF and DFT kernels. Assuming the presence of a single heavy atom in the system allows us to approximate the SO operator as $\sum_{N=1}^{nuc} Z^N r_N^{-3} \hat{t}_u^N \cong Z^{HA} r_{HA}^{-3} \hat{t}_u^{HA}$, see **section 2.3.3**. The unperturbed wave function has been calculated at the PBE/Dyall-vtz/ pcS-2 level.

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